1	Mantle flow beneath Arabia offset from the opening Red Sea
2	
3	Sung-Joon Chang ¹ , Miguel Merino ¹ , Suzan Van der Lee ¹ , Seth
4	Stein ¹ & Carol A. Stein ²
5	
6	¹ Department of Earth and Planetary Sciences
7	Northwestern University, Evanston, IL 60208, USA
8	
9	² Department of Earth and Environmental Sciences, University
10	of Illinois at Chicago, 845 W. Taylor Street Chicago, IL
11	60607-7059, USA
12	
13	Supplementary Material
14	Method
15	The new seismic tomographic image of velocity
16	structure used here is part of one of a much larger area
17	from the marginal region of the former Tethys Ocean, which

includes the Arabian Plate and the Red Sea, derived by joint 18 inversion of seismic wave travel times and waveforms [Chang 19 et al., 2010]. The data consist of global and regional data 20 21 sets of arrival times, body wave forms, regional multimode S and surface wave trains, surface wave group velocities, 22 and constraints on Moho depth from active source seismic 23 studies, gravity surveys, global geological and geophysical 24 interpretations, and receiver functions. 25

26 Of the regional wave trains fit in the joint inversion using the partitioned waveform inversion technique [Nolet, 27 1990; van der Lee and Nolet, 1997] about two and a half 28 thousand have wave paths traverse the current study region 29 of Arabia and the Red Sea. The data coverage is illustrated 30 by great-circle wave paths shown by the locations of events 31 and stations in Figure S1a. The waveform frequency content 32 is generally somewhere between 0.006 and 0.1 Hz. 33

34 Of the Rayleigh-wave group-velocity data used [Chang

35	et al., 2010; Pasyanos and Nyblade, 2007], with periods
36	ranging from 7 to 100 s, nearly four thousand paths traverse
37	the current study region. Great-circle wave paths for the
38	45-s period group-velocity data are shown in Figure S1b.
39	Of the high-resolution relative arrival times of
40	teleseismic S & SKS waves used, about four thousand were
41	derived by multi-channel cross correlation [vanDecar and
42	Crosson, 1990] for receivers in Ethiopia [Beniot et al.,
43	2006], Arabia [Park et al., 2007], and the Mediterranean
44	region [Schmid et al., 2004]. Almost thirteen thousand
45	additional, absolute S phase arrival times from the
46	reprocessed ISC database [Engdahl et al., 1998] came from
47	the current study region. Locations of stations and events
48	for each type of arrival time data are depicted in Figure
49	S1c.

Lastly, the study region here included over three 50 hundred of the independent Moho depth estimates used in the 51

joint inversion. These Moho depth constraints are shown in
Figure S1d.

54

55 S.2. Resolution tests

Because we focus here on velocity structure below the 56 Red Sea and Arabia, we investigated the resolving power of 57 joint inversion for this region with a number of 58 the different test structures using several resolution tests. 59 First, we tested a model with a low-velocity channel 60 along the Red Sea and one trending northward beneath Arabia, 61 as shown in the top-left panel of Figure S2. The resulting 62 synthetic data were generated by multiplying the sensitivity 63 64 kernels used in the inversion with the parameters of this test model. We contaminated these synthetic data with 65 Gaussian random noise with a standard deviation proportional 66 uncertainty of the estimated the actual data 67 to to investigate the resolving power of the joint inversion in 68

realistic cases. We estimate the uncertainty of the Moho 69 constraints as 2 km for receiver function results, 4 km for 70 active source seismic studies, and 6 km for gravity data 71 72 according to data quality. Uncertainties for other data sets are given in Chang et al. [2010]. Depth slices of the 73 inversion results at 50, 100, 150 km are shown in Figure S2. 74 Although the anomalies are recovered with weaker amplitude 75 than in the model, as is typical in seismic tomography, the 76 77 two anomalies are distinctly resolved with similar amplitude down to at least 100 km. At 150 km depth, although the low-78 velocity anomaly beneath the Red Sea is recovered weakly, we 79 can still discern both anomalies in their correct locations, 80 81 without overlap. Hence the offset of the anomaly from the 82 Red Sea is resolved. Moreover, the anomaly is recovered with relatively homogenous amplitude along the Red Sea, which 83 excludes the possibility that the absence of a low-velocity 84 anomaly beneath the northern Red Sea may be caused by poor 85

86 data coverage.

87 We also performed a resolution test for a model including a broad low-velocity anomaly covering the Red Sea 88 89 and the western half of Arabia, as shown in Figure S3. This test explored the possibility that limitations of resolving 90 power in the joint inversion might yield an apparent narrow 91 linear anomaly beneath Arabia. The inversion results show 92 that the broad anomaly is well recovered without generating 93 94 an artificial linear anomaly.

The first test also explored the depth resolution, as 95 shown in cross sections along the Red Sea and the Gulf of 96 Aden [Figure S4]. The model has low-velocity anomalies along 97 98 the Red Sea, the Gulf of Aden, and beneath Arabia extending to different depths. The inversion results show that these 99 anomalies are distinctly recovered, albeit with weaker 100 amplitude and some smearing, as is typical in seismic 101 tomography. 102

Based on these tests, we are confident that the low-103 velocity region beneath Arabia is a relatively narrow 104 channel rather than a broad regional anomaly, and that this 105 channel occurs below Arabia, not beneath the northern Red 106 Sea. 107

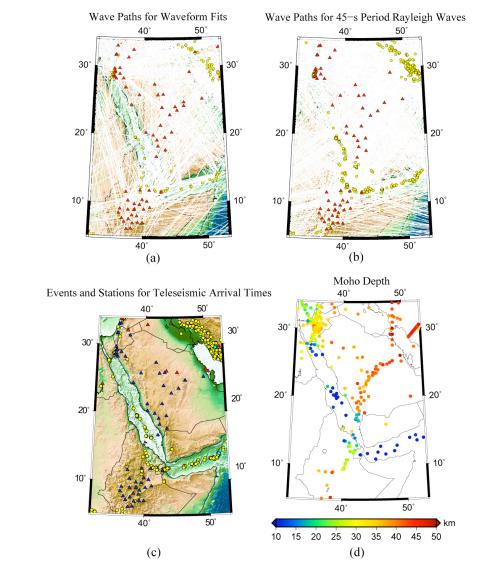
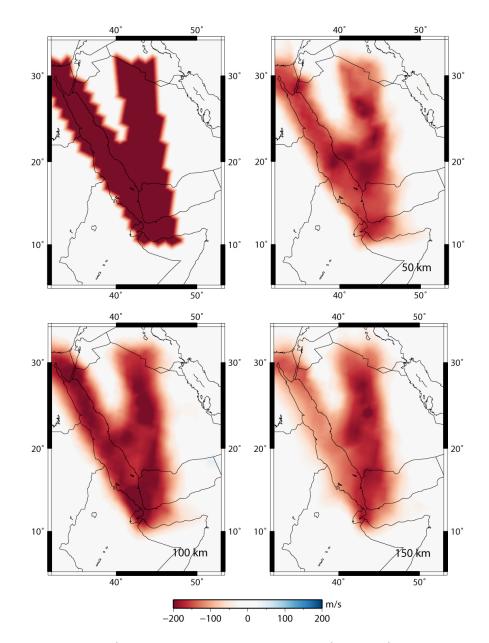


Fig. S1. Great-circle wave paths for (a) waveform fits and 109 Rayleigh 45-period Stations 110 (b) waves. and events are indicated in red triangles and yellow circles, respectively. 111 (c) Location of events and stations for teleseismic arrival 112 113 times. Stations and events from ISC database and multi-

channel cross-correlation technique are indicated by red 114 triangles, yellow circles, blue triangles and cyan circles, 115 respectively. (d) Moho depth variations. 116



117

118 Fig. S2. Resolution test for a model including two separate low-velocity anomalies. The starting model is shown in the 119 left-top panel, and inversion results are shown at 50, 100, 120 and 150 km depths. 121

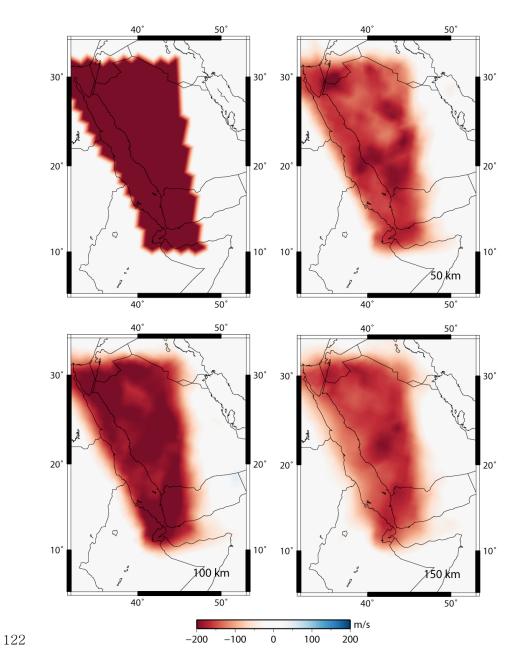


Fig. S3. Resolution test for a model including a broad lowvelocity anomaly covering the Red Sea and western Arabia. The model is in the left-top panel, and inversion results are shown at 50, 100, and 150 km depths.

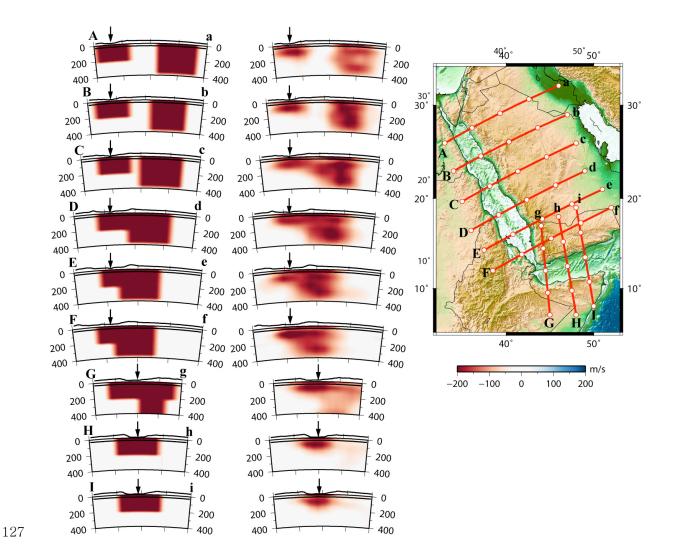


Fig. S4. Resolution test for cross sections along the Red Sea 128 129 and the Gulf of Aden. The models are shown on the left, and 130 the corresponding inversion results are given in the middle. Moho depth and surface topography are depicted in black solid 131 132 lines. Topography is exaggerated times. Black 10 arrows indicate location of ridge on each cross 133 section. Lines

corresponding to the cross sections are shown on the map on 134 the right. White circles on the great-circle paths correspond 135 to ticks in the cross sections. 136

Supplementary References 137

138	Benoit, M. H., A. A. Nyblade, T. J. Owens and G. Stuart
139	(2006), Mantle transition zone structure and upper mantle ${\it S}$
140	velocity variations beneath Ethiopia: Evidence for a broad,
141	deep-seated thermal anomaly, Geochem., Geophys., Geosys., 7,
142	Q11013, doi:10.1029/2006GC001398.
143	Chang, SJ., S. van der Lee, M. P. Flanagan, H. Bedle, F.
144	Marone, E. M. Matzel, M. E. Pasyanos, A. J. Rodgers, B.
145	Romanowicz, and C. Schmid (2010), Joint inversion for 3-
146	dimensional S-velocity mantle structure along the Tethyan
147	margin, J. Geophys. Res., 115, B08309,
148	doi:10.1029/2009JB007204.

Engdahl, E. R., R. Van der Hilst, and R. Buland (1998), 149 Global teleseismic earthquake relocation with 150 improved travel times and procedures for depth determination, Bull. 151 Seismol. Soc. Amer., 88, 722-743. 152

Nolet, G. (1990), Partitioned waveform inversion and 2-153

154	dimensional structure under the network of autonomously
155	recording seismographs, J. Geophys. Res., 95, 8499-8512.
156	Park, Y., A. A. Nyblade, A. J. Rodgers, and A. Al-Amri, A.,
157	(2007) Upper mantle structure beneath the Arabian Peninsula
158	and northern Red Sea from teleseismic body wave tomography:
159	Implication for the origin of Cenozoic uplift and volcanism
160	in the Arabian Shield, Geochem., Geophys., Geosys., 8,
161	Q06021, doi:10.1029/2006GC001566.
162	Pasyanos, M. E. & A. A. Nyblade (2007), A top to bottom
163	lithospheric study of Africa and Arabia, Tectonophysics, 444,
164	27-44.
165	Schmid, C., S. Van der Lee, and D. Giardini (2004), Delay
166	times and shear wave splitting in the Mediterranean region:
167	Geophys. J. Intern., 159, 275-290.
168	
169	Van der Lee, S. and G. Nolet (1997), Upper mantle S velocity
170	structure of North America, J. Geophys. Res. 102, 22,815-

22,838. 171

VanDecar, J. C. & R. S. Crosson (1990), Determination of 172 teleseismic relative phase arrival times using multi-channel 173 cross-correlation and least-squares, Bull. Seisol. Soc. 174Amer., 80, 150-169. 175