SEISMOLOGY & EARTH STRUCTURE

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Mars is too cold Earth is just right Venus is too hot



PROBING THE DEEP EARTH



MODELS OF EARTH'S COMPOSITION, TEMPERATURE, & INTERNAL PROCESSES TODAY & OVER TIME



Figure 1.1-1: Schematic geometry of a seismic experiment.



STUDY BOTH SOURCE AND MEDIUM

One seismologist's signal is another's noise

SEISMIC WAVES

DISTURBANCES AS FUNCTION OF SPACE & TIME THAT TRAVEL THROUGH SOLID EARTH

LIKE SOUND WAVES, LIGHT (ELECTROMAGNETIC) WAVES, OR WATER WAVES

USE SEISMIC WAVES TO "SEE" INSIDE EARTH

LIKE LIGHT (VISION, XRAYS) OR SOUND (ULTRASOUND, SONAR, DOLPHINS, BATS)







SEISMIC WAVES TRAVEL THROUGH EARTH

> Use to study earthquakes & structure of the earth











"every rock and tree and creature has a life, has a spirit, has a name..."



Figure 1.1-5: Demonstration of the seismic reflection method.

Figure 1.1-6: Example of a seismic reflection survey.



Figure 2.2-1: Tensions on a string segment.



Discarding the higher Taylor series terms:

$$\tau \left(\frac{\partial u(x,t)}{\partial x} + \frac{\partial^2 u(x,t)}{\partial x^2} \, dx - \frac{\partial u(x,t)}{\partial x} \right) = \tau \, \frac{\partial^2 u(x,t)}{\partial x^2} \, dx = \rho \, dx \, \frac{\partial^2 u(x,t)}{\partial t^2}$$

Wave equation:

$$\frac{\partial^2 u(x, t)}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 u(x, t)}{\partial t^2}$$

where $v = (\tau/\rho)^{1/2}$



Х

" If I have seen further it is by standing on the shoulders of giants." 1676



where $f^{''}$ is the second derivative of f

WAVE FIELD COUPLES SPACE AND TIME



Harmonic (sinusoidal) function:

$$u(x, t) = Ae^{i(\omega t \pm kx)} = A\cos(\omega t \pm kx) + Ai\sin(\omega t \pm kx)$$

gives $v = \omega/k$

| Table 2.2-1 Relationships Between Wave Variables | | |
|--|------------------------|--|
| QUANTITY | UNITS | |
| Velocity | distance/time | $\mathbf{v} = \boldsymbol{\omega}/k = f \lambda = \lambda/T$ |
| Period | time | $T = 2\pi/\omega = 1/f = \lambda/v$ |
| Angular Frequency | time ⁻¹ | $\omega = 2\pi/T = 2\pi f = k\mathbf{v}$ |
| Frequency | time ⁻¹ | $f = \omega/(2\pi) = 1/T = v/\lambda$ |
| Wavelength | distance | $\lambda = 2\pi/k = v/f = vT$ |
| Wavenumber | distance ⁻¹ | $k = 2\pi/\lambda = \omega/v = 2\pi f/v$ |



Figure 2.2-4: Harmonic wave, $u = A \cos (\omega t - kx)$.





POINT IN TIME, FUNCTION OF SPACE



SEISMIC WAVES OCCUR BECAUSE AN APPLIED FORCE MAKES ROCK DEFORM ELASTICALLY & THEN RETURNS TO ORIGINAL SHAPE

COMPRESSION - VOLUME CHANGES

SHEAR- DISTORTION: SHAPE CHANGES



Force

FIGURE 5.3 Two different ways of straining a rock (illustrated with a sponge): compression and shear. F represents the applied force. The shear strain is $\theta/2$, which is half the angle by which right angles change after shearing.

Davidson 5.3

Figure 2.4-3: Displacements for *P* and *S* waves.



S waves: ground motion is perpendicular to wave direction

P waves: ground motion is parallel to wave direction

P OR <u>COMPRESSIONAL</u> WAVES - VOLUME CHANGES MATERIAL COMPRESSED OR EXPANDED IN DIRECTION WAVE PROPAGATES **S** OR <u>SHEAR</u> WAVES -DISTORTION WITHOUT VOLUME CHANGES -MATERIAL SHEARED IN DIRECTION PERPENDICULAR TO WAVE PROPAGATION SEISMIC WAVE SPEED (VELOCITY)

DEPENDS ON ELASTIC CONSTANTS (MODULI) & DENSITY OF MATERIAL

K - BULK MODULUS - LARGER K IS HARDER TO COMPRESS

 μ - SHEAR MODULUS - LARGER μ **IS HARDER TO SHEAR**

0

ρ- DENSITY

COMPRESSIONAL (P) WAVE SPEED V_P DEPENDS ON BOTH MODULI <u>BUT</u> SHEAR (S) WAVE SPEED V_s DEPENDS ON ONLY SHEAR MODULUS

P WAVES TRAVEL FASTER (ABOUT 1.7x) THAN S WAVES

S WAVES CANNOT TRAVEL THROUGH LIQUID ($\mu = 0$) LIKE OUTER CORE

IN CRUST, V_P ABOUT 5.5 km/s - 12,375 miles/hr



Time (min.)

Figure 2.4-9: Seismograms recorded 64 km from a small, shallow earthquake.



MNV September 24, 1982 07:40:24

For close distances (horizontal propagation):

 $t_s = x/3.2$ $t_p = x/5.5$

$$t_s - t_p = x(1.0/3.2 - 1.0/5.5) = x/7.6$$

THREE COMPONENTS OF GROUND MOTION P & S waves appear differently

Figure 2.4-8: Seismograms at two Japanese stations above an earthquake.



Figure 2.4-4: Displacements for *P*, *SV*, and *SH*.



RADIAL & TRANSVERSE HORIZONTAL COMPONENTS





$$\begin{pmatrix} u_R \\ u_T \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} u_{EW} \\ u_{NS} \end{pmatrix}$$



Figure 2.4-7: Seismic spectrum for various studies.

electromagnetic spectrum









(AND IS USED IN LENSES, EYEGLASSES, ETC. FOR LIGHT)

TRAVELLING BETWEEN MEDIA OF DIFFERENT VELOCITIES, WAVES BEND AND CHANGE AMPLITUDE

Figure 2.5-4: Change in wave front and direction during refraction.







Snell's law:

$$c_x = \frac{\alpha_1}{\sin i_1} = \frac{\beta_1}{\sin j_1} = \frac{\alpha_2}{\sin i_2} = \frac{\beta_2}{\sin j_2}$$

FROM FASTER TO SLOWER MATERIAL- REFRACTED WAVES BENDS TOWARDS VERTICAL

FROM SLOWER TO FASTER MATERIAL- REFRACTED WAVES BENDS TOWARDS HORIZONAL





$$T(x) = \frac{(a^2 + x^2)^{1/2}}{v_1} + \frac{((b - x)^2 + c^2)^{1/2}}{v_2}$$

$$\frac{dT(x)}{dx} = \frac{x}{v_1 (a^2 + x^2)^{1/2}} - \frac{(b - x)}{v_2 ((b - x)^2 + c^2)^{1/2}} = \frac{\sin i_1}{v_1} - \frac{\sin i_2}{v_2} = 0$$

Snell's law:
$$\frac{\sin i_1}{v_1} = \frac{\sin i_2}{v_2}$$

SNELL'S LAW DESCRIBES OTHER FAMILIAR EFFECTS

DIFFERENT COLORS (WAVELENGTHS) OF LIGHT TRAVEL AT DIFFERENT SPEEDS IN WATER OR GLASS, SO REFRACTED AT DIFFERENT ANGLES

RAINDROPS CAUSE THE RAINBOW.

THIS IS WHY YOU ONLY SEE A RAINBOW WHEN THE SUN IS BEHIND YOU





2004 Sumatra Earthquake 010 min



TSUNAMI SPEED IN DEEP WATER of depth d $c = (gd)^{1/2}$ g = 9.8 m/s² d = 4000 m c = 200 m/s = 720 km/hr =450 mph In open ocean, wavelength long (~100 km), amplitude small (~50 cm) As wave slows in shallow water, wavelength decreases & amplitude grows Maximum amplitude radiated at right angle to fault

staff.aist.go.jp/kenji.satake/animation.gif



RAYS BEND AS WATER DEPTH CHANGES

FIND WHEN WAVES ARRIVE AT DIFFERENT PLACES

DENSITY OF WAVES SHOWS FOCUSING & DEFOCUSING



Figure 2.8-9: Ray paths for tsunami generated by the 1960 Chile earthquake.

Okal, 1987



Total Internal reflection



OTHER APPLICATIONS- FIBER OPTICS- LIGHT "TRAPPED" IN A LOW VELOCITY FIBER

SOSUS $\alpha_2 > \alpha_1$ The "Secret Weapon" of Undersea Surveillance α_1 $\alpha_2 > \alpha_1$ **SOFAR CHANNEL** Velocity (ft/sec) Range (miles) 4850 4900 5000 5100 5100 5 10 15 35 0 20 25 30 40 Sound channel Depth (fathoms) 1000 2000 15.19 15.19

Figure 2.5-11: Propagation of waves in a low-velocity channel.

REFLECTION (R) AND TRANSMISSION (T) COEFFICIENTS



http://www.earth.northwestern.edu/people/seth/demos/STRING/string.html





TSUNAMI wave speed = (water depth x acceleration of gravity)^{1/2}

1 Earthquakes cause the ocean floor to collapse in places and rise elsewhere, displacing water and generating waves.



2 Initial waves, largely underwater, travel very fast toward the shore.



4 The tsunami reaches the shore, causing severe flooding and extreme currents.



KHAO LAK, THAILAND DECEMBER 26, 2004







Figure 2.4-10: Ground displacement from the 1989 Loma Prieta earthquake.


TRAVEL TIME CURVES

Figure 3.5-3: Travel time data and curves for the IASP91 model.



Figure 3.5-5: Illustration of various body wave phases.





Figure 3.5-1: Comparison of the J-B and IASP91 earth models.

SEISMIC RAY PATHS BEND AS VELOCITY INCREASES WITH DEPTH

Figure 1.1-2: Schematic ray paths for an increase in seismic velocity with depth.



Snell's law for spherical earth with velocity v at radius r

Ray turns to incidence angle i so ray parameter p is constant along the ray

$$p = \frac{r \sin i}{v}$$

Figure 3.4-5: Ray path effects for increasing velocity.



 $p = r \sin i / v$ = dT/ d Δ Depth

 $p = r \sin i / v = dT / d\Delta$

Rapid velocity increase causes triplication

Multiple rays at same distance

Velocity Distance (Δ) Time Distance (Δ)

are concentrated, and low amplitudes where rays are sparse.

Expect high amplitudes where rays

Mathematically, the concentration of rays is proportional to $di/d\Delta$, the range of incidence angles for the rays that arrive in a given distance.

$$\frac{d^2T}{d\Delta^2} = \frac{dp}{d\Delta} = \frac{d(r\sin i/v)}{d\Delta} = \frac{r}{v}\cos i\frac{di}{d\Delta}$$

The amplitude is proportional to the second derivative of the travel time curve, or the derivative of the $p(\Delta)$ curve.



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Figure 3.5-12: Ray paths for *P* waves through the upper mantle.



Figure 3.4-7: Ray path shadow-zone effects for a velocity decrease.

Distance (Δ)

Figure 3.5-7: Ray paths and travel times for major core phases.



HUYGEN'S PRINCIPLE

Treat every point on wave front as source of new circular wavefront

Figure 2.5-15: Huygens' generation of circular wave fronts. figure 2.5-15: Huygens' generation of circular wave fronts. t = 0





Figure 2.5-17: Derivation of Snell's law using Huygens' principle.



Figure 2.5-18: Single-slit diffraction.

DIFFRACTION: ENERGY ARRIVES WHERE THERE'S NO GEOMETRIC (SNELL'S LAW) PATH

Process is frequency dependent: long wavelengths (long periods) diffract more



Destructive interference when (for D >> d): $\lambda/2 = d \sin \theta \approx dx_0/D$

Actual diffraction pattern is: $\frac{\sin \zeta}{\zeta}$ where $\zeta = 2\pi dx/\lambda D$

Diffraction is described by Huygens' principle, but not geometric ray theory.



Figure 2.7-1: Seismograms recorded at a distance of 110°, showing surface waves.

Figure 2.7-2: Geometry for Love and Rayleigh wave motions.



Figure 2.7-3: Multiple surface waves circle the earth.



6

Time (hours)

2

0



Figure 2.8-3: Example of calculating Love wave group velocity dispersion.

Figure 2.7-10: Displacements of for Love waves in a layer over a halfspace.

The wave oscillates as $\cos(k_x r_{\beta_1} z)$ in the layer, but decays exponentially as $\exp(-k_x r_{\beta_2}^* z)$ in the half-space.

The vertical sensitivities of the modes are the eigenfunctions.



Love wave surface displacement

 $\beta_1 = 3.9 \text{ km/s}$ $\beta_2 = 4.6 \text{ km/s}$ $\rho_1 = 2.8 \text{ g/cm}^3$ $\rho_2 = 3.3 \text{ g/cm}^3$ h = 40 km

LONGER PERIODS HAVE LONGER WAVELENGTHS

AND SO "SEE" DEEPER INTO HIGHER VELOCITY MATERIAL

GEOMETRICAL DISPERSION DIFFERS FROM PHYSICAL DISPERSION (prism)





Figure 3.5-19: Snapshots of a synthetic SH wave field at various times.

TOMOGRAPHY ("SLICE PICTURE")

BEAMS TRAVEL THROUGH OBJECT AT MANY DIFFERENT ANGLES

COMBINE BEAMS FOR DETAILED PICTURE OF VARIATIONS INSIDE OBJECT

(CAT= COMPUTED AXIAL TOMOGRAPHY)

MEDICAL TOMOGRAPHY USES X-RAYS (ELECTROMAGNETIC RADIATION) TO "SEE" VARIATIONS IN ABSORPTION DUE TO BONES, TISSUE ETC







SEISMIC WAVES TRAVEL THROUGH THE EARTH ON MANY DIFFERENT PATHS

COMBINE PATHS FOR A DETAILED PICTURE OF VELOCITY VARIATIONS INSIDE

SEISMIC TOMOGRAPHY OF MIDOCEAN RIDGE HOT UPWELLING MAGMA HAS LOW VELOCITY



Forsyth et al, 1998

TOMOGRAPHY SHOWS THERMAL STRUCTURE OF SUBDUCTING PLATE (SLAB)

COLD (HIGH SEISMIC VELOCITY) OCEANIC PLATE SUBDUCTS INTO WARMER (LOWER SEISMIC VELOCITY) MANTLE

WARM REGION OF BACK ARC MELTING CAUSES VOLCANOES

SLAB HEATS UP SLOWLY (MILLIONS OF YEARS)



ANALYSES OF TRAVEL TIME CURVES GIVE VELOCITIES, COMPOSITIONS, AND CHANGES WITH DEPTH

4 MAJOR REGIONS:

CRUST, MANTLE, OUTER CORE, INNER CORE



Davidson 5.8

Earth's mass:

 $g = GM/a^2$

Because $g = 9.8 \text{ m/s}^2$, $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{kg}^{-2}$, and a = 6371 km,

we get $M_{Earth} = 5.97 \times 10^{24}$ kg.

The average density, ρ_o , is found by dividing the mass by the volume:

$$\rho_o = M / \left[(4/3)\pi a^3 \right] \approx 5.5 \text{g/cm}^3$$

This value is significantly higher than the density of the surface rocks (about 3 g/cm³). (Evidence for a core of denser material)

Because density varies with depth, the mass varies with depth as

$$M = 4\pi \int_{0}^{a} \rho(r)r^{2}dr$$

TRAVEL TIME CURVES GIVE VELOCITY AT DEPTH

TO DETERMINE COMPOSITION, NEED TO KNOW WHAT MATERIALS COULD EXIST AT THOSE DEPTHS (PRESSURES) AND TEMPERATURES THAT WOULD HAVE OBSERVED VELOCITIES

PRESSURE = DENSITY x DEPTH x ACCELERATION OF GRAVITY

SO PRESSURE INCREASES WITH DEPTH

3 km depth => 1000 ATMOSPHERES

400 km => 133,000 ATMOSPHERES, ~1500°C

CORE-MANTLE BOUNDARY (2900 km) => 1.3 million ATMOSPHERES, ~3700°C

CENTER OF EARTH (6371 km) => 3.5 million ATMOSPHERES, ~4200°C

MATERIALS BEHAVE VERY DIFFERENTLY AT THESE CONDITIONS THAN AT SURFACE

INCREASE OF PRESSURE WITH DEPTH HAS TWO EFFECTS

- STEADY COMPRESSION (SQUISHING) OF MATERIAL MAKES IT STRONGER AND DENSER AND SO INCREASES VELOCITY GRADUALLY WITH DEPTH IN UPPER (100-410 km depth) AND LOWER (660-2900 km depth) MANTLE

- AT APPROPRIATE PRESSURE AND TEMPERATURE CONDITIONS MINERALS TRANSFORM TO DENSER PHASES, CAUSING THE RAPID VELOCITY INCREASES (DISCONTINUITIES) AT 410 AND 660 km depth



SIMULATING EARTH'S INTERIOR

Lab experiments

Pressure = Force/Area



Figure 3.8-10: Crystal structures of a α olivine and γ -spinel.



phase change

8% denser

Spinel structure





Piston Cylinder - reach upper mantle conditions



Diamond cell - reach core conditions



TEMPERATURES IN THE EARTH - GEOTHERM

BELOW MELTING CURVE (SOLIDUS) IN MANTLE AND SOLID INNER CORE

ABOVE MELTING CURVE IN LIQUID OUTER CORE



Transition zone between upper & lower mantles bounded by 410 and 660 km discontinuities

Velocity increases due to mineral phase changes



Figure 3.8-11: Effect of phase changes on velocity structure.



SOLID INNER CORE FREEZES FROM OUTER CORE



Fractional crystalization as earth cools

Composition of inner & outer cores differ

Heat released by freezing and gravitational energy released as the denser solid sinks drive convection in the outer core and thus generate magnetic field

Figure 3.8-15: Geotherm and solidus for the core.





Figure 5.1-1: Cartoon of plate tectonics.

EARTH: A GIANT HEAT ENGINE

"Heat is the geological lifeblood of planets"







Plate tectonics makes Earth different

Seafloor topography and heat flow indicate Earth's heat loss primarily (~70%) by plate tectonics, with ~25% by conduction

Grossly similar sister planets, Mars and Venus, seem conduction-dominated: large-scale plate tectonics appears absent, at least at present

Mars may have had plate tectonics, now stopped, perhaps due to both cooling & loss of water (which reduces rock strength & thus may be needed for plate tectonics)

Venus may still be hot with episodic overturns rather than steady-state plate tectonics





Terrestrial (inner) planets may follow similar life cycle with stages including formation, early convection and core formation, plate tectonics, terminal volcanism, and quiescence.

Evolution driven by available energy sources as planets cool with time. Planets formed at about the same time but are at different stages in their life cycles. (Consider human and dog born on the same date).

Earth in middle age with active plate tectonics

Moon & Mars old, dead, inactive - "one plate planets"

DEAD MOON & MARS

Seismological & other data suggest moon now has a thick lithosphere and is tectonically inactive

Lost much of its heat, presumably because of small size, which favors rapid heat loss.

Expect the heat available from gravitational energy of accretion and radioactivity to increase as the planet's volume, whereas rate of heat loss should depend on surface area

remaining heat = available / loss ~ $(4/3)\pi r^3 / 4\pi r^2 = r/3$

Larger planets would retain more heat and be more active

Mercury and Mars, larger than the moon but smaller than earth, should have also reached their old age with little further active tectonics.


Remember, always, the words of Francis Birch (1952)



Ordinary language undergoes modification to a highpressure form when applied to the interior of the Earth. A few examples of equivalents follow:

High-pressure form

Ordinary meaning

certain undoubtedly positive proof unanswerable argument pure iron dubious perhaps vague suggestion trivial objection uncertain mixture of all the elements