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Have We Seen the Largest Earthquakes in Eastern North America?

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**24 Abstract**

25 The assumed magnitude of the largest future earthquakes,  $M_{max}$ , is crucial in assessing seismic  
26 hazard, especially for critical facilities like nuclear power plants. Absent any theoretical basis,  
27 estimates are made using various methods and often prove far too low, as for the 2011 Tohoku,  
28 Japan, earthquake. Estimating  $M_{max}$  is particularly challenging within tectonic plates, where large  
29 earthquakes are infrequent compared to the length of the available earthquake history, vary in  
30 space and time, and sometimes occur on previously unrecognized faults. For example, it is  
31 unclear whether the largest earthquakes along the eastern U.S. seaboard and eastern Canada have  
32 occurred. We explore this issue by generating synthetic earthquake histories and sampling them  
33 over a few hundred years. The maximum magnitudes appearing most often in the simulations are  
34 essentially those observed, and smaller than the simulation maxima. Future earthquakes along  
35 both coasts may thus be significantly larger than those observed to date.

36

**37 Introduction**

38 The 2011 Virginia earthquake that shook much of the northeastern U.S. showed that earthquakes  
39 large enough to cause significant damage occur in eastern North America [Wolin *et al.*, 2012]  
40 (Fig. 1). Assessing the hazard of such earthquakes poses major unresolved issues. Hazard maps,  
41 giving the maximum shaking expected in an area with a certain probability in some time period  
42 [Cornell, 1968], require assuming where and when large earthquakes will occur and how large  
43 they will they be. However, the recent Tohoku, Haiti, and Wenchuan earthquakes illustrate that  
44 highly destructive earthquakes can occur in areas predicted to be relatively safe [Geller, 2011;  
45 Gulkan, 2013; Kerr, 2011; Peresan and Panza, 2012; Stein and Okal, 2011; Wyss *et al.*, 2012].

46 This situation arises because parameters required to reliably estimate the hazards are often poorly  
47 known [Stein *et al.*, 2012].

48

49 A crucial parameter is  $M_{max}$ , the magnitude of the largest earthquake expected on a fault or in an  
50 area [Stein *et al.*, 2012]. The Tohoku, Haiti, and Wenchuan earthquakes were more damaging  
51 than expected because they were much larger than the  $M_{max}$  assumed. Unfortunately, no  
52 theoretical basis exists to infer  $M_{max}$ . Even where we know the long-term rate of motion across a  
53 plate boundary fault, or the deformation rate across an intraplate zone, neither predict how strain  
54 will be released.

55

56 As a result, quite different  $M_{max}$  estimates can be made [Kagan and Jackson, 2013; Kijko, 2004;  
57 U.S Nuclear Regulatory Commission, 2012]. Because all one can say with certainty is that  $M_{max}$   
58 is at least as large as the largest earthquake in the available record, one could use that magnitude  
59 or add an increment. However, because catalogs are often short relative to the average recurrence  
60 time of large earthquakes [McGuire, 1977], larger earthquakes than anticipated often occur.  
61 Another approach is to identify faults and use relations between fault length and earthquake  
62 magnitude [Wells and Coppersmith, 1994] to infer  $M_{max}$ . Other approaches extrapolate from  
63 current catalogs [Kijko, 2004] or combine areas presumed to be geologically similar to sample  
64 more large earthquakes [Kagan and Jackson, 2013; U.S Nuclear Regulatory Commission, 2012].

65

66 Estimating  $M_{max}$  is challenging at plate boundaries, where known plate motion rates can be  
67 compared to earthquake records on known faults to infer the slip in, and thus magnitude of, large  
68 earthquakes. The situation is more complicated within plates, where deformation rates are poorly

69 known, large earthquakes are rarer and variable in space and time, and often occur on previously  
70 unrecognized faults [*Camelbeeck et al.*, 2007; *Crone et al.*, 2003; *Liu et al.*, 2011].

71

72 We explore this issue for eastern North America. Notable events along the U.S. coast include the  
73 1755 Cape Ann Massachusetts and 1886 Charleston earthquakes. Larger earthquakes are known  
74 along the Canadian coast, notably the 1929 Grand Banks and 1933 Baffin Bay events. Thus this  
75 passive continental margin has a modest level of seismicity [*Stein et al.*, 1979; *Wolin et al.*,  
76 2012] as do others [*Schulte and Mooney*, 2005; *Stein et al.*, 1989].

77

78 A challenge in assessing the earthquakes' hazard is that we know little about their causes, partly  
79 because they are relatively rare due to the slow deformation at such margins. They may reflect  
80 reactivation of faults created by previous continental collision and breakup, given that passive  
81 margins are often reactivated [*Cloetingh et al.*, 2008]. Geodynamic modeling predicts stresses  
82 from variations in topography and crustal structure across the margin, combined with  
83 sublithospheric mantle flow [*Ghosh et al.*, 2013].

84

85 A crucial issue is how much to rely on past large earthquakes, as illustrated by Geological  
86 Survey of Canada hazard maps [*Wolin et al.*, 2012]. The 1985 map concentrates hazard at the  
87 sites of the Grand Banks and Baffin Bay earthquakes, assuming these are especially hazardous.  
88 The 2005 map assumes that similar earthquakes can occur anywhere along the margin.

89

90 The observed seismicity being an imperfect sample of more uniform seismicity is plausible  
91 geologically and suggested by seismicity between the Grand Banks and Baffin Bay, some of

92 which may be aftershocks of prehistoric earthquakes [Wolin *et al.*, 2012]. Simulations with short  
93 catalogs yield apparent concentrations and gaps that are artifacts of the sampling [Swafford and  
94 Stein, 2007]. Similarly, although seismicity onshore is patchy, geological observations show  
95 evidence of slow long-term deformation [Pazzaglia *et al.*, 2010] and the present seismicity  
96 occurs in areas that are not geologically or geomorphologically different from nearby areas that  
97 appear aseismic.

98

99 A related question is whether the larger earthquakes and higher seismicity along the Canadian  
100 coast represent a real difference. The difference could be real, perhaps due to stresses associated  
101 with deglaciation, [Mazzotti *et al.*, 2005; Sella *et al.*, 2007; Wolin *et al.*, 2012] or reflect the short  
102 earthquake record.

103

#### 104 ***Results and Analysis***

105 Absent reliable ways of assessing  $M_{max}$ , we use synthetic earthquake histories to explore what  
106  $M_{max}$  values would be observed in a short catalog. We assume earthquakes satisfy a Gutenberg-  
107 Richter frequency-magnitude relation,  $\log_{10} N = a - bM$ , where  $N$  is the annual number of  
108 earthquakes with magnitude  $\geq M$ ,  $a$  defines the seismicity rate, and  $b$  is the slope of the line  
109 relating the rates of small and large earthquakes. The recurrence interval between events for each  
110 magnitude is described by a Gaussian distribution about the predicted mean rate. Thus events  
111 with magnitude  $\geq M$  have average recurrence time  $T_{rM} = 10^{-(a-bM)}$  years, with a standard deviation  
112 of  $0.4T_{rM}$ . Each simulation has a specified  $M_{max}$  above which no earthquakes occur.

113

114 For the U.S. coast we use  $a=4.24$  and  $b=0.92$ , calculated from recent seismicity, corresponding  
115 to a  $M \geq 7$  earthquake on average every  $\sim 150$  years. We generate four sets of 10,000 histories,  
116 assuming that  $M_{max}$  is 7.0, 7.2, 7.4, and 7.6. We take a 300-year sample of each history,  
117 corresponding to the period over which all large ( $M \geq 6$ ) earthquakes are likely to be known.  
118 Samples start 5000 years into the simulation to ensure that 'now' has no significance.

119

120 Fig. 2 illustrates three representative histories. These are long enough to adequately represent the  
121 rates of small earthquakes, which define a line corresponding to the parent distribution.  
122 However, because the 300-year sampling interval corresponds to the recurrence interval of  
123  $M=7.3$  earthquakes, larger events are undersampled.

124

125 As a result, two biases can arise. In one, the largest "observed" earthquake is smaller than in the  
126 parent distribution, so  $b$  is biased upward, underestimating the rate of large earthquakes. In the  
127 other, the largest earthquakes are "observed", but their recurrence interval and thus  $b$  are  
128 underestimated. Hence the short history causes us to either underestimate  $M_{max}$  when  
129 earthquakes of this size do not appear, or correctly estimate it but conclude that such earthquakes  
130 are more common than they really are [*Stein and Newman, 2004*]. These effects can be visualized  
131 by considering the parent distribution of recurrence times. Records shorter than the mean  
132 recurrence time of the largest events are likely to not contain these events. If they contain such  
133 events, these have recurrence times shorter than the mean, implying that they are more common  
134 than actually the case.

135

136 Fig. 2 also illustrates different ways of inferring the Gutenberg-Richter distribution's parameters.  
137 If short sampling causes the rate of large earthquakes to deviate from that extrapolated from  
138 small ones, least-squares fitting characterizes larger magnitudes better and thus may not match  
139 the rate of the smaller ones well. Maximum likelihood estimation [Aki, 1965; Weichert, 1980]  
140 weights the more populous lower magnitudes heavily and thus can misfit larger magnitudes.  
141 Analyses seeking to estimate  $b$  typically use maximum likelihood, as discussed in the  
142 supplemental information. The two methods give different  $b$  values and hence different  
143 recurrence time predictions for large events.

144

145 Fig. 3 shows  $M_{max}$  values "observed" for the U.S. east coast earthquake histories. The most  
146 common values vary depending on the assumed  $M_{max}$ , but is  $\sim 7.3$  for simulations with large  
147  $M_{max}$ , corresponding to 300-year sampling. Even when  $M_{max}$  is significantly larger, it rarely  
148 appears. For example,  $M_{max}=7.6$  occurs in only 10% of the simulations. The most common  
149 "observed" value is close to that inferred for the Charleston earthquake.

150

151 Fig. 3 shows analogous results for eastern Canada for  $a=4.44$  and  $b=0.94$ , calculated from recent  
152 seismicity, corresponding to an earthquake with  $M \geq 7.2$  on average every 212 years. Histories for  
153  $M_{max}=7.4, 7.6, 7.8,$  and  $8.0$  are sampled for 100 years, the period over which all large ( $M \geq 6$ )  
154 earthquakes are likely to be known. The most common  $M_{max}$  values "observed," about 6.8, reflect  
155 the sample length even when the parent distribution  $M_{max}$  is significantly larger. For example,  
156  $M_{max}=8.0$  appears in only  $\sim 2\%$  of the runs. The most common "observed" value is lower than the  
157 Grand Banks and Baffin Bay earthquakes, but observing  $M=7.4$  like Baffin Bay's is not  
158 extraordinarily rare.

159 **Discussion**

160 Hence future earthquakes along both coasts may be larger than observed to date. Some of the  
161 higher Canadian seismicity rate may reflect aftershocks [Wolin *et al.*, 2012] of recent large  
162 earthquakes.  $M_{max}$  for both coasts may be the same, although if the higher seismicity in Canada is  
163 real rather than a sampling artifact, large events would be more common there.

164

165 More generally, these simulations demonstrate that  $M_{max}$  cannot be reliably estimated from  
166 earthquake catalogs. The largest earthquake observed likely reflects the length of the history  
167 used, even if larger earthquakes occur (Fig. 4). Although the precise fraction depends on the  
168 distribution of recurrence times, a catalog shorter than an earthquake's mean recurrence time is  
169 likely to not contain an event of that size.

170

171 This effect is significant within plates where large earthquakes are infrequent, as in northwestern  
172 Europe [Leonard *et al.*, 2013] or Australia [Camelbeeck, 2007]. However, as recent examples  
173 illustrate, it also arises at plate boundaries for earthquakes larger than observed in the record  
174 used. We can lengthen the record with paleoseismology and use geodesy to infer the size of  
175 future events. Even so, although various plausible assumptions about  $M_{max}$  can be made, the only  
176 certainty is that it is at least as large as that observed to date, as in the adage "anything that did  
177 happen, can happen."

178

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184 Foundation for supporting his stay at the University of Gottingen, where much of the writing was  
185 done.

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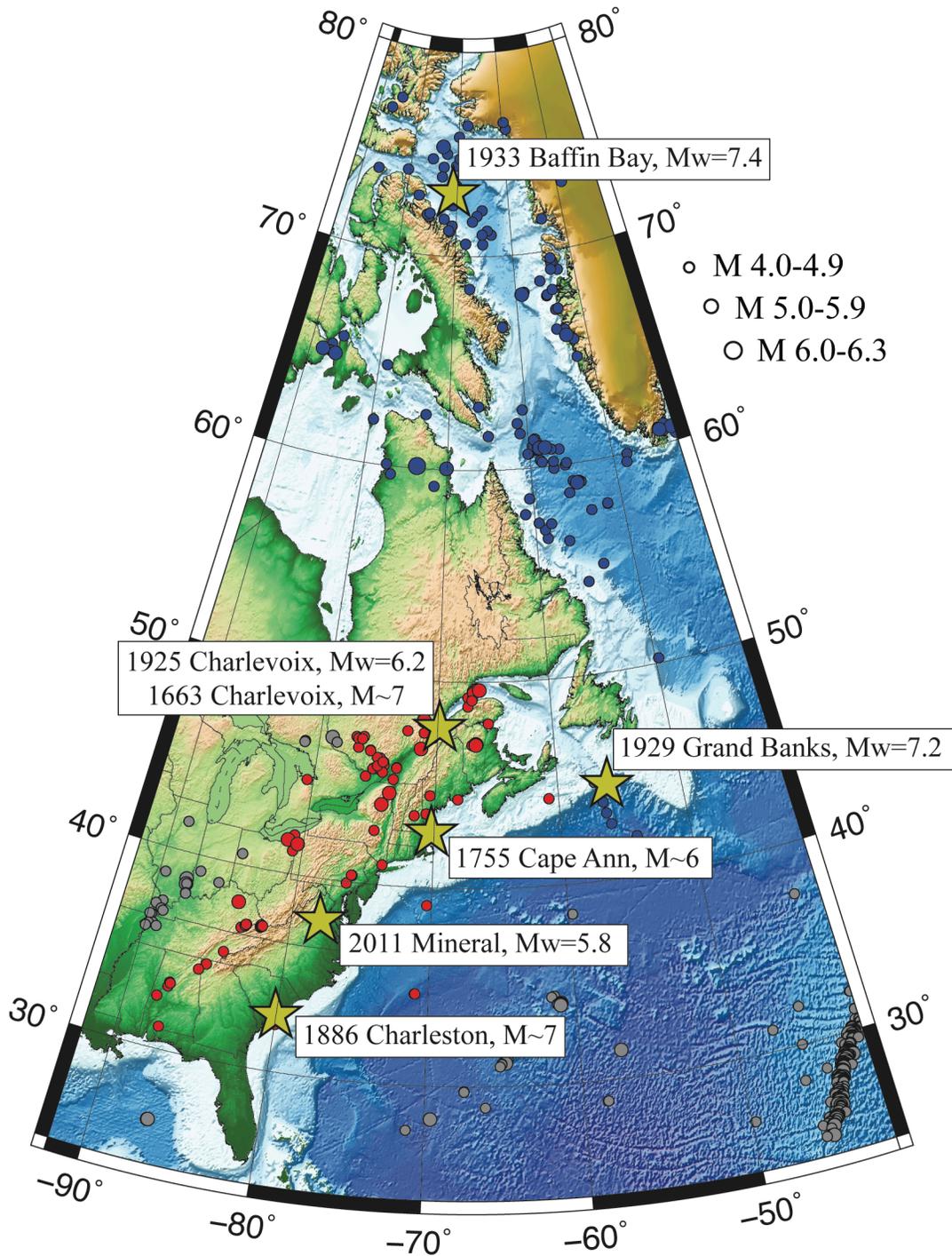
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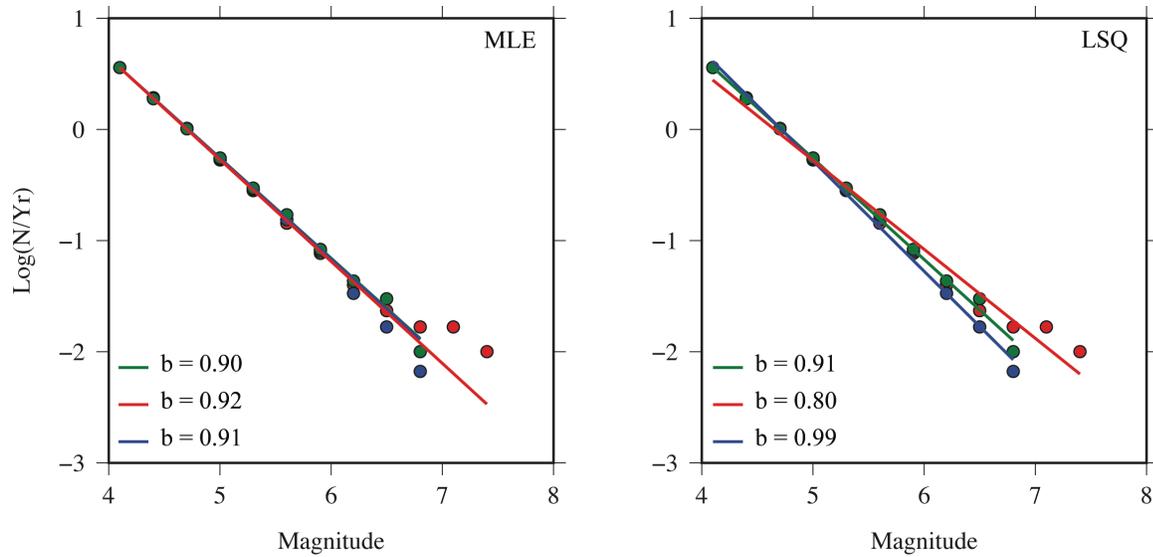
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293 Figure 1: Seismicity of the eastern North American continental margin taken from ANSS and

294 NEDB catalogs. Red and blue dots correspond to the U.S and Canadian margins respectively.

295 Major historical events are also shown. Modified from (8). Earthquake selection is discussed in

296 supplemental information.



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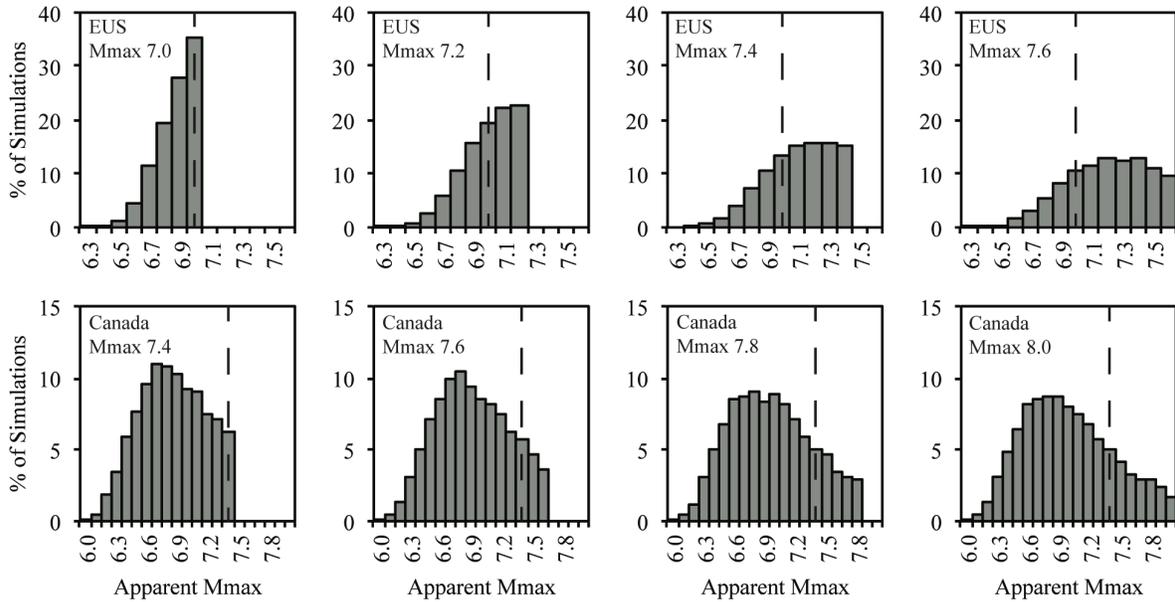
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299 Figure 2: Frequency-magnitude results for three of the histories (different colors) generated with  
300 the eastern U.S. simulations with  $M_{max}=7.6$ . These histories are long enough to adequately  
301 represent the rates of small earthquakes. However, because the 300-year sampling interval  
302 corresponds to the recurrence interval of magnitude  $\sim 7.3$  earthquakes, larger events with longer  
303 recurrence times are undersampled. As a result, maximum likelihood (MLE) and least-squares  
304 (LSQ) fits to the data differ.

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309 Figure 3: Top: Results for four sets of 10,000 simulations for the eastern U.S coast, each with a  
 310 different  $M_{max}$ . Panels show the percentage of simulations in which a given apparent  $M_{max}$  is  
 311 observed. Dashed line represents the actual observed  $M_{max}$  of 7.0, corresponding approximately  
 312 to the Charleston earthquake. Bottom: Simulations for eastern Canada. Dashed line represents  
 313 the actual observed  $M_{max}$  of 7.4 from the Baffin Bay earthquake.

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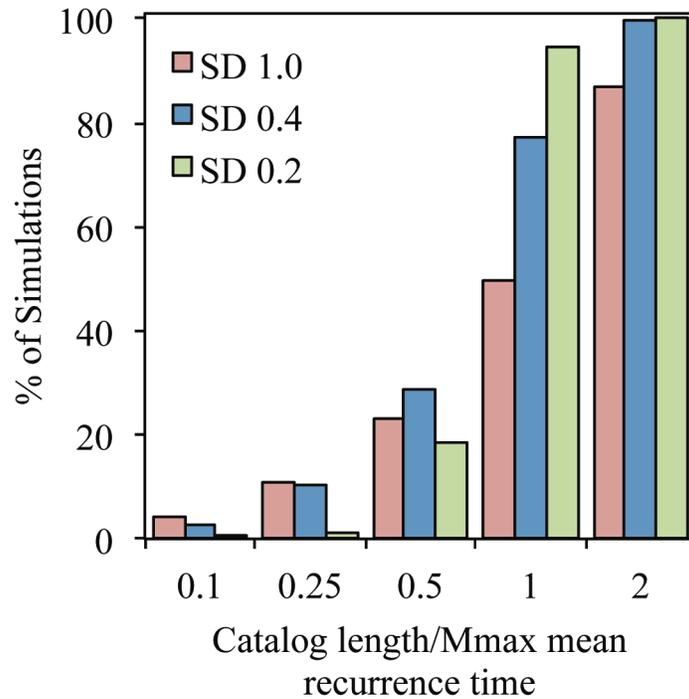
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323 Figure 4: Percentages of simulations that recover the input  $M_{max}$  for varying catalog lengths.

324 Catalog lengths are given as a fraction of the mean recurrence time for earthquakes with

325 magnitude  $M_{max}$ . Colors show results for Gaussian distributions of recurrence times with

326 standard deviation equal to the indicated fraction of the mean. A catalog shorter than an

327 earthquake's mean recurrence time is likely to not contain an event of that size.

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335 ***Supplementary Information***

336 The regional  $a$  and  $b$  values were estimated from the Advanced National Seismic System  
337 (ANSS) from 1985-2013 for the eastern U.S, and the Canadian National Earthquake Database  
338 (NEDB) from 1985-2013 for eastern Canada (Fig. 1). All earthquakes along the eastern  
339 Canadian coastline and near Hudson Strait were selected to be eastern Canada passive margin  
340 earthquakes. Eastern US earthquakes were selected by taking all earthquakes within  $6^\circ$  of the  
341 coast. Earthquakes near the historical Grand Banks earthquake are assigned to the eastern  
342 Canada catalog. The regional  $a$  and  $b$  values were calculated by the MLE method, which is  
343 sensitive to the completeness of the catalog, with a magnitude cutoff of 4.0 for eastern Canada  
344 and the eastern U.S (Fig. S1).

345

346 As noted in the text (Fig. 2), a linear Gutenberg-Richter relationship can be fit to a set of  
347 frequency-magnitude data using either Maximum Likelihood (MLE) or Least Squares (LSQ)  
348 estimates, each with advantages and disadvantages. In general, a least-squares fit characterizes  
349 larger magnitudes better, but thus may not match the rate of the smaller ones well. Conversely,  
350 MLE weights lower magnitudes heavily and so gives more stable estimates of the distribution's  
351  $b$ -value (slope). Thus if one expects that the data come from a Gutenberg-Richter distribution,  
352 such that the deviations from the linear trend are artifacts of sampling or otherwise, MLE  
353 estimation is preferable. As a result, most seismic hazard analyses use MLE. Conversely, if one  
354 approaches the data without this expectation, LSQ can be viewed as a better characterization of  
355 the data themselves.

356

357 In our simulations, the “data” come from a population with a Gutenberg-Richter distribution. As  
358 a result, MLE recovers the distribution’s  $b$ -value (slope) better because it weights lower  
359 magnitudes heavily. Hence for any set of simulations,  $b$ -values estimated by MLE vary less than  
360 those inferred using LSQ.

361  
362 Fig. S2 illustrates this effect for the set of simulations for the eastern U.S with  $M_{max}$  of 7.6. The  
363 simulated catalogs are the same for the MLE and LSQ calculations. MLE yields tightly grouped  
364  $b$  values. In contrast, LSQ has a tradeoff between  $b$ -value and  $M_{max}$  because the line fits the larger  
365 magnitudes better. As a result, it is unlikely that it will recover the parameters of the parent  
366 distribution (dot) if the imposed  $M_{max}$  does occur.

367  
368 These differences in the  $b$ -value distributions are shown by the standard deviations in the eastern  
369 U.S simulations with an  $M_{max}$  of 7.6, which are 0.01 and 0.06 for MLE and LSQ, respectively.  
370 The  $b$ -values calculated by MLE and LSQ both have Gaussian distributions (Fig. S3, S4). Hence  
371 the 95% confidence range for a M7.6 earthquake’s recurrence interval  $Tr_M$  ranges from  
372 approximately 350 to 900 years, using for the MLE method. This  $\sim 2.5$  fold difference in  $Tr_M$   
373 would give an uncertainty in the estimated hazard. The combined uncertainties for the eight sets  
374 of simulations in Fig. 3 are illustrated in Fig. S5. As expected,  $b$ -values are recovered well  
375 whereas  $M_{max}$  is generally underestimated.

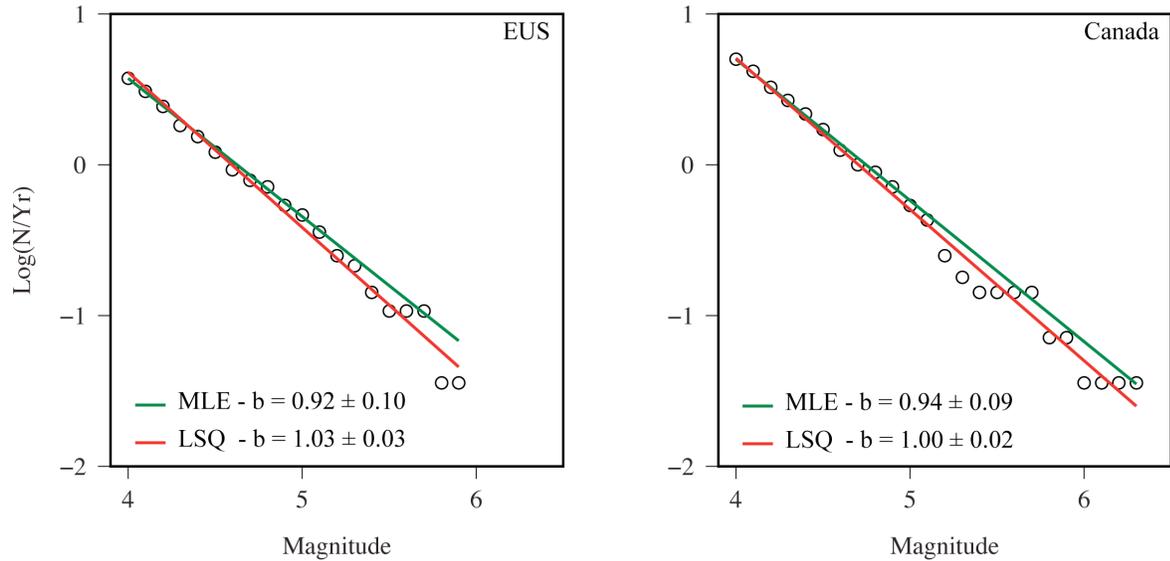
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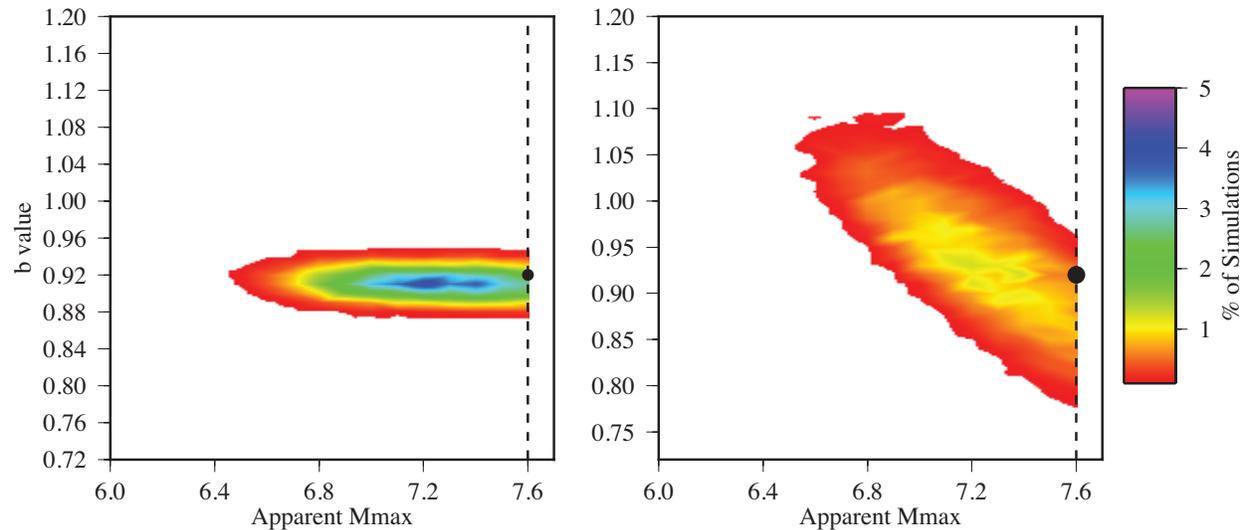
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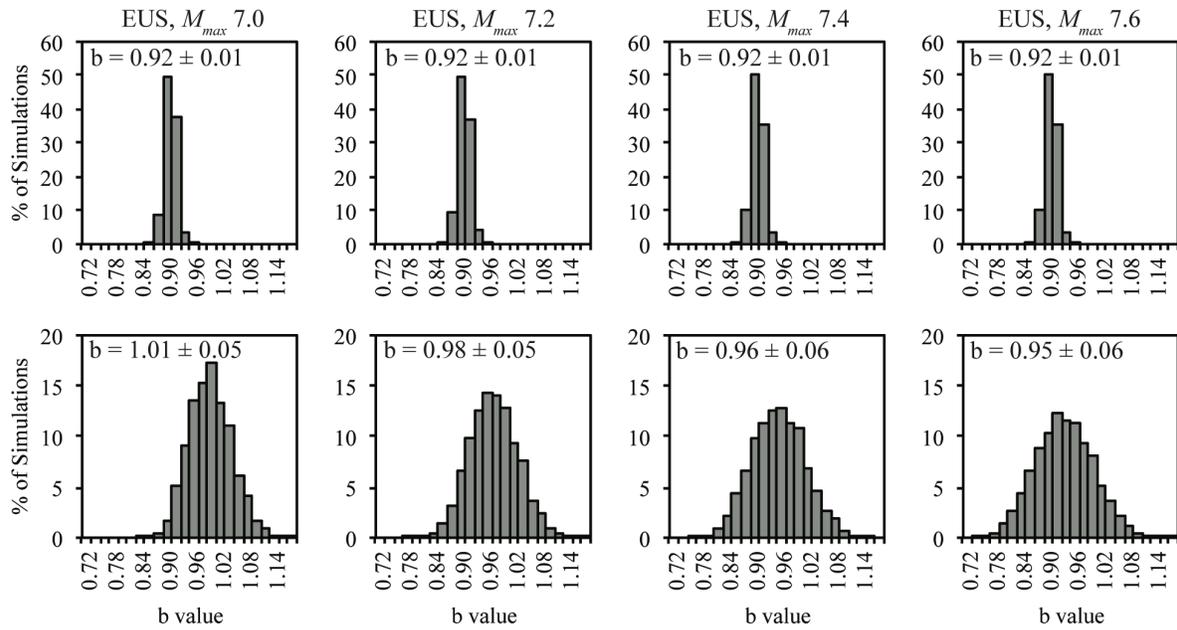
382 Figure S1: Frequency-magnitude relationships calculated for the eastern U.S (left panel) and  
 383 eastern Canada (right panel). Green line is for the MLE fit. Red line is for the LSQ fit. The MLE  
 384 results are used as inputs to the simulations.

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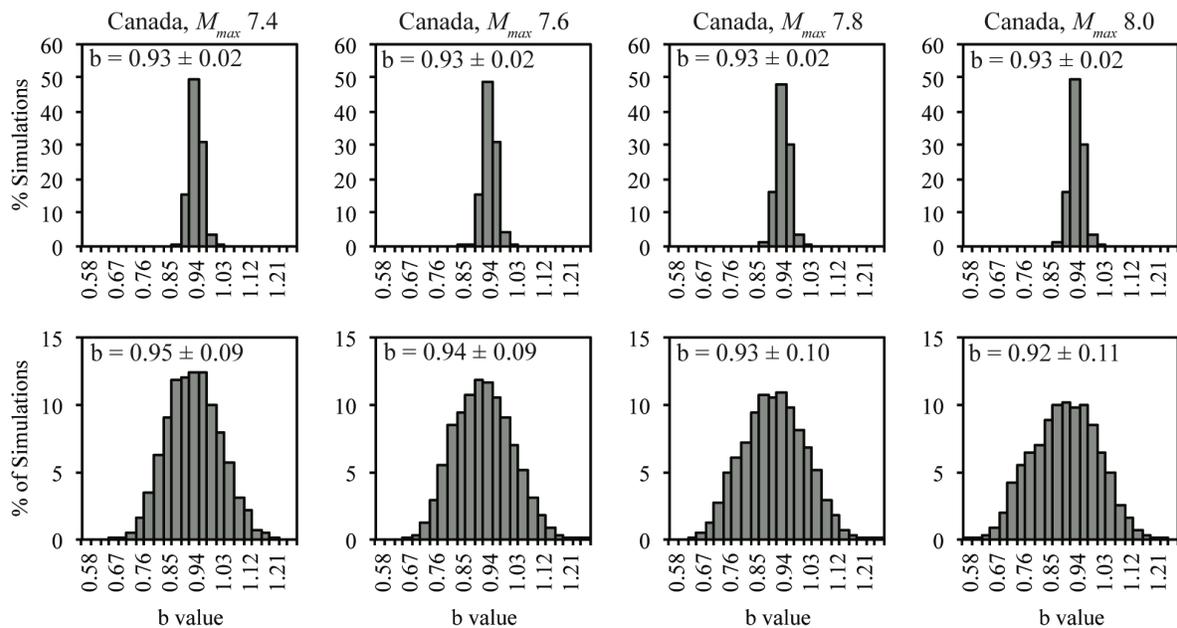
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387 Figure S2: Distribution of apparent  $M_{max}$  and  $b$ -value results for a set of simulations sampling a  
 388 parent distribution whose value is shown by the dot.



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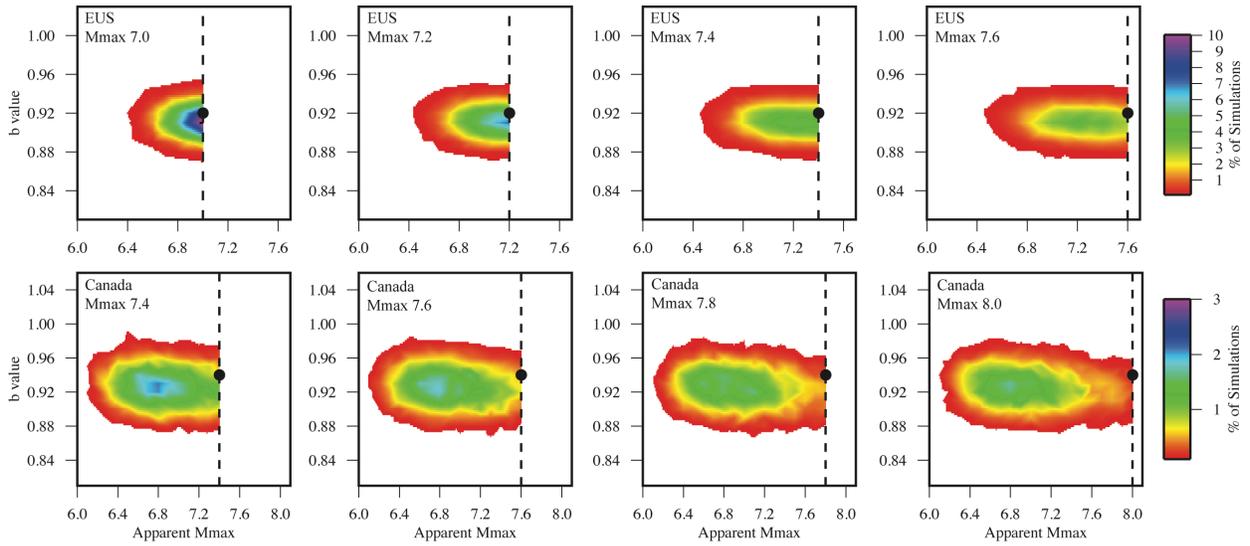
390 Figure S3: Top:  $b$ -value results for the four sets of 10,000 simulations for the eastern U.S coast,  
 391 each with a different  $M_{max}$ . Panels show the percentage of simulations in which a given  $b$  value,  
 392 calculated by the MLE method, is observed. Bottom: Results of the simulations for the eastern  
 393 U.S coast using the LSQ method to calculate  $b$  values.



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395 Figure S4: Same as in figure S3 for eastern Canada.

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398 Figure S5: Distributions of MLE estimates for the eight sets of simulations in Fig. 3. As  
399 expected,  $b$ -values are recovered well whereas  $M_{max}$  is generally underestimated.

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