

Monte Carlo Models of Dense Star Clusters

Sourav Chatterjee

MODEST 18, Firá, Santorini
June 26, 2018



Hénon-type Monte Carlo

N-body model



spread all masses in spherical shells (E, J)



approximate the total effects of many weak fly-bys by a super encounter between neighbors



update E, J; calculate new orbits

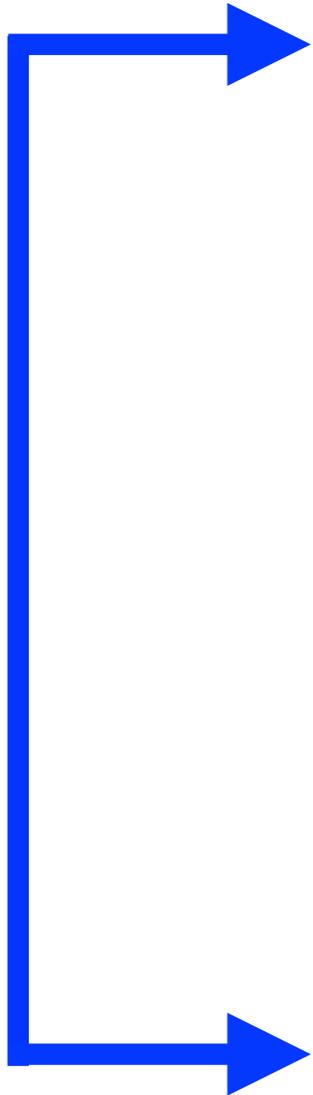


Monte Carlo new positions and velocities in these orbits to get back new N-body model



add physics (e.g., strong scattering, stellar evolution, tides, etc.)

2-body relaxation

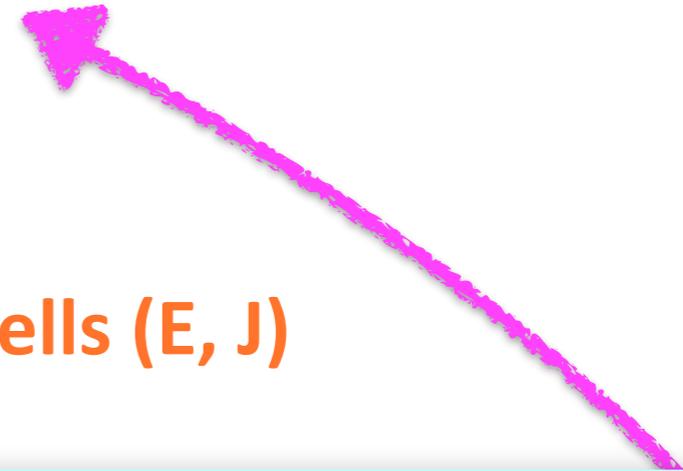


Hénon-type Monte Carlo

N-body model



spread all masses in spherical shells (E, J)



Mon. Not. R. Astron. Soc. **000**, 1–10 (2002)

Printed 24 November 2014

(MN L^AT_EX style file v2.2)

Michel Hénon's contributions to collisional stellar systems

Douglas C. Heggie¹

¹ *University of Edinburgh, School of Mathematics and Maxwell Institute for Mathematical Sciences, King's Buildings, Edinburgh EH9 3JZ, UK; d.c.heggie@ed.ac.uk*

24 November 2014

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add physics (e.g., strong scattering, stellar evolution, tides, etc.)

World's Only DMP Parallel Monte Carlo Code

CMC

- Two-body relaxation (Joshi et al. 2000)
- Strong interactions: physical collisions, binary-mediated interactions (Fregeau & Rasio 2007)
- Galactic tidal stripping (Joshi et al. 2001; Chatterjee et al. 2010)
- Stellar evolution using BSE (Hurley et al. 2000, 2002; Chatterjee et al. 2008, 2010)
- Central IMBH with loss-cone physics (Umbreit et al. 2012)
- Parallelized using MPI & CUDA (Pattabiraman et al. 2012)
- Rate-based 3-Body binary formation (Morscher et al. 2015)
- Up to 2.5 PN GR effects for all strong encounters (Rodriguez et al. 2018; Antognini et al. 2014; Amaro-Seoane et al. 2016)

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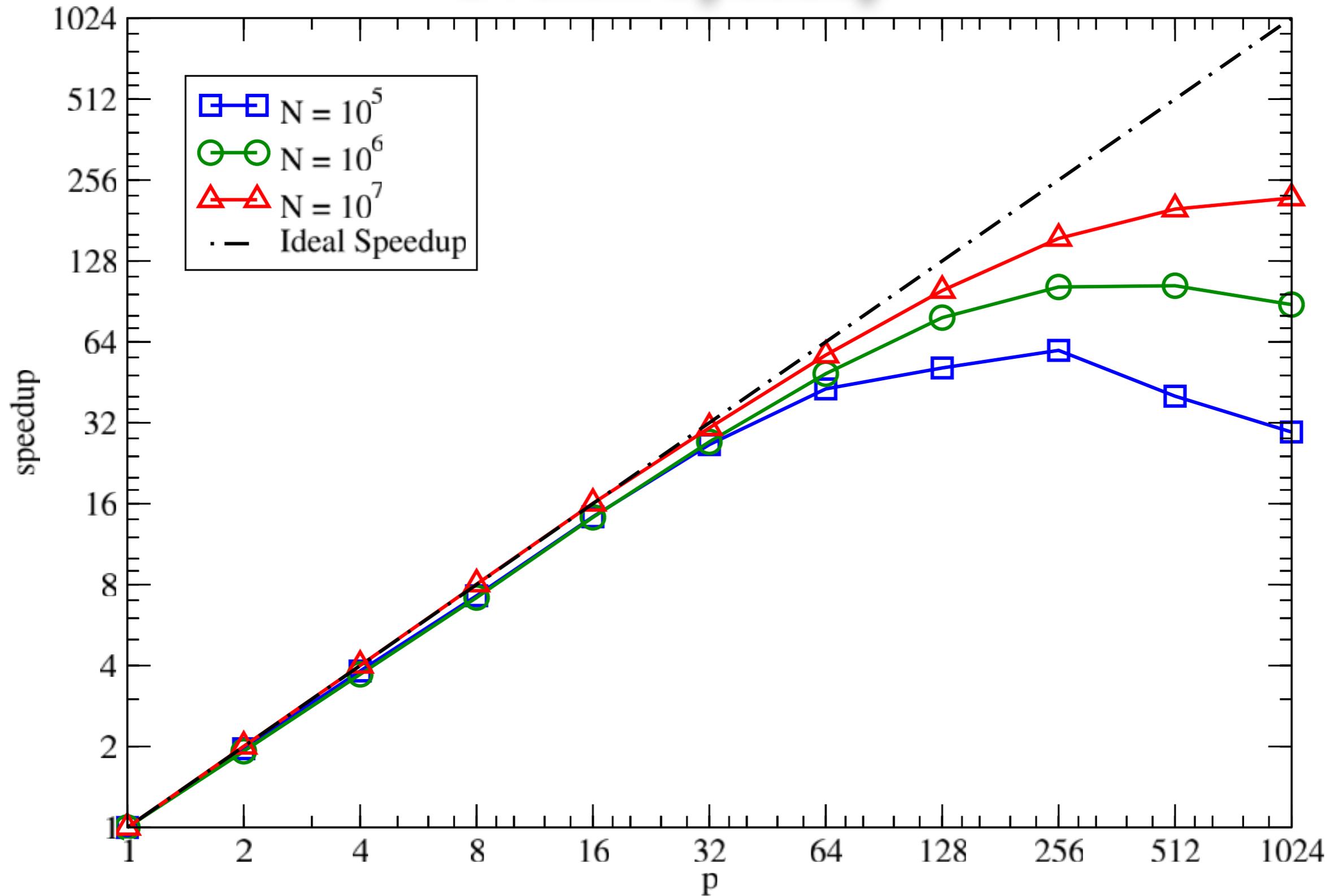
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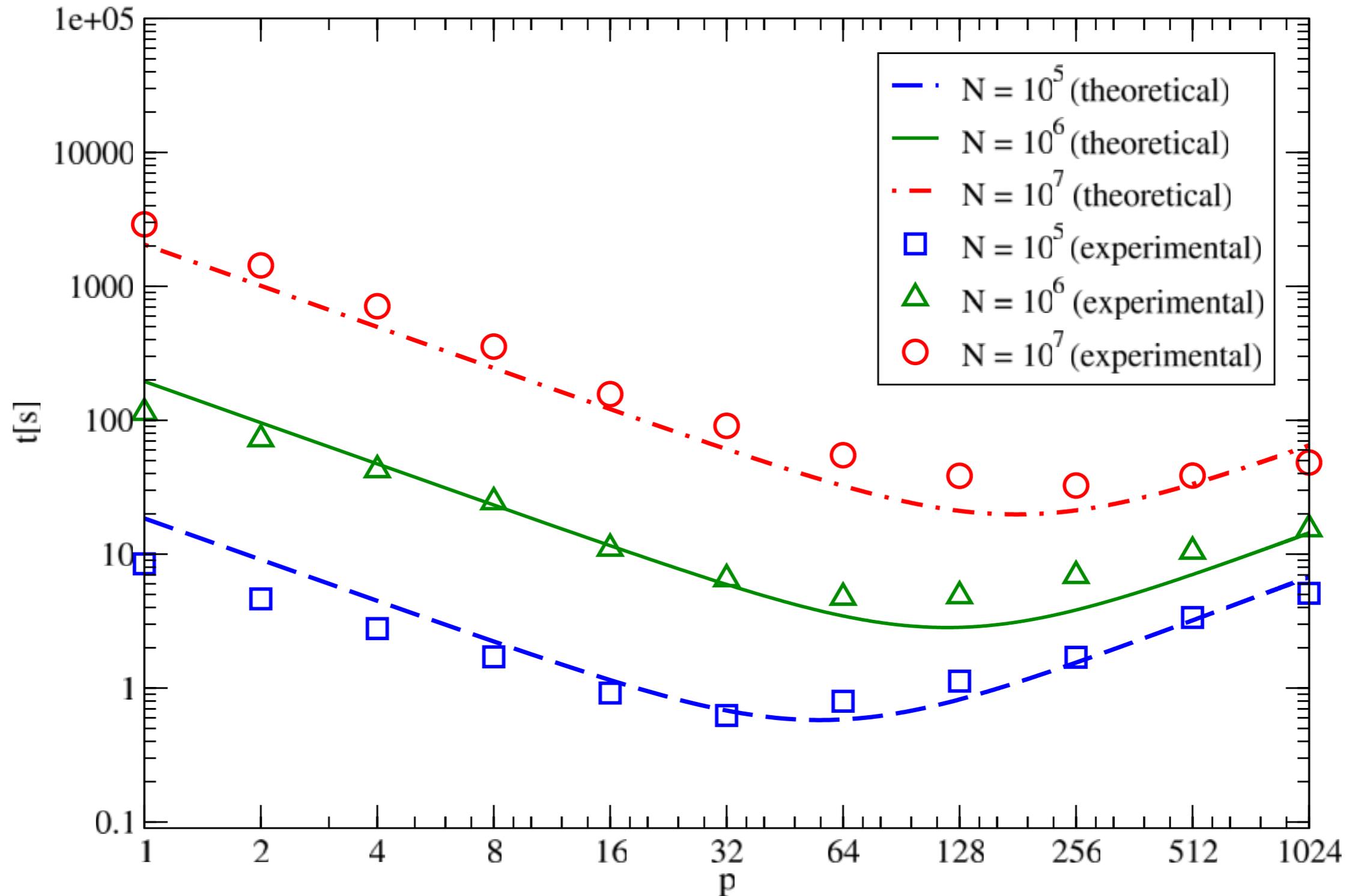
Performance of Parallel CMC

Overall Speedup

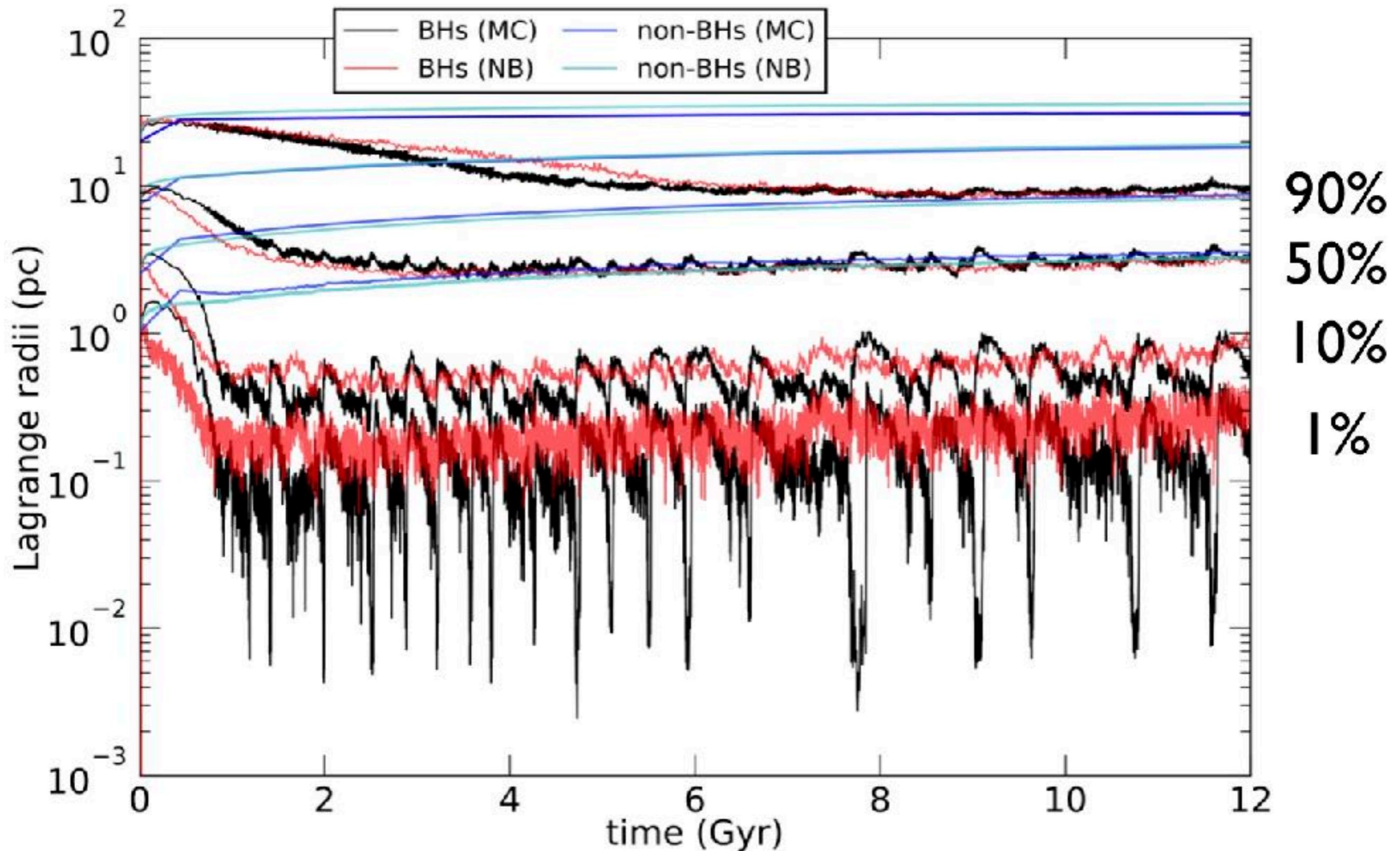


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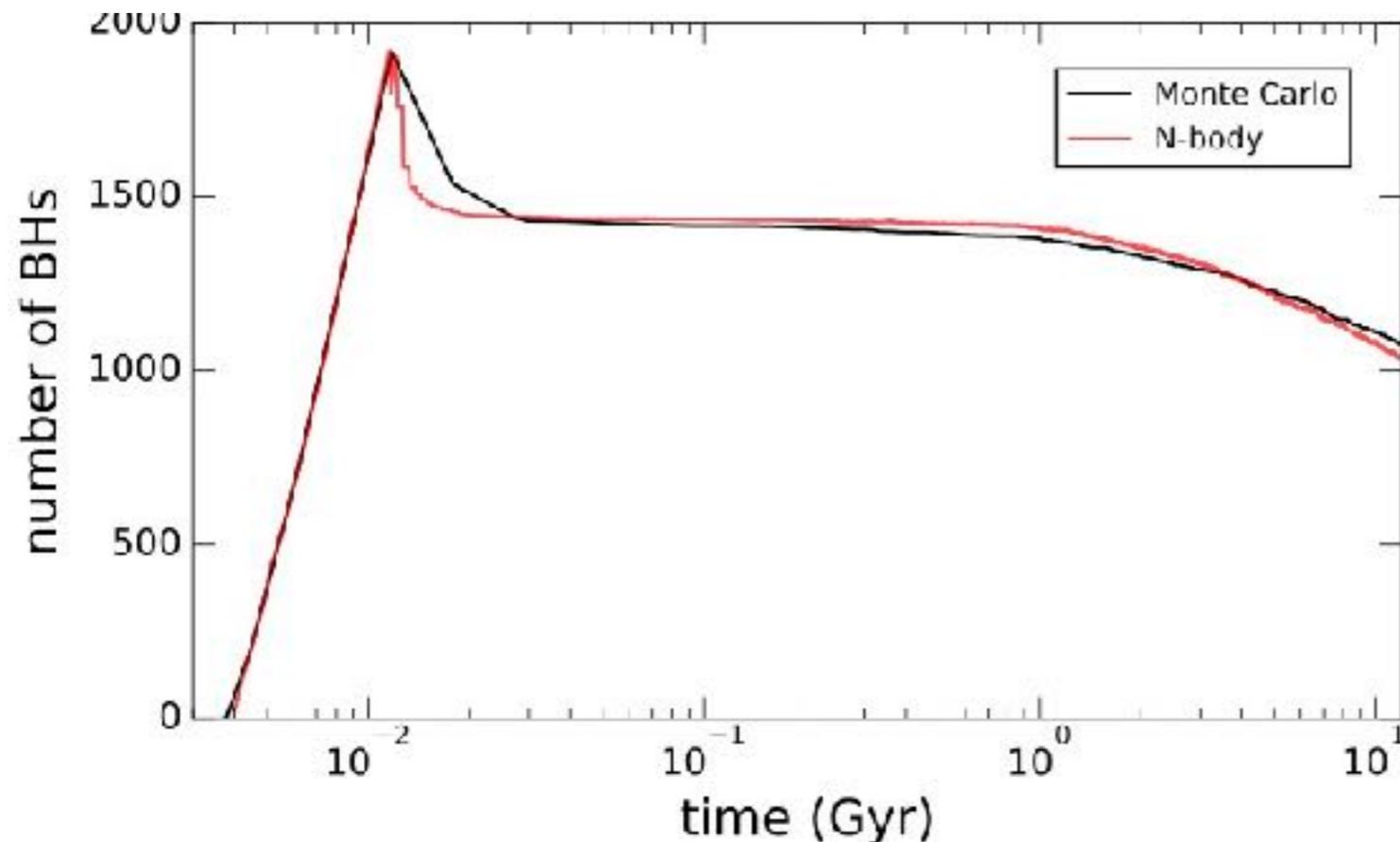
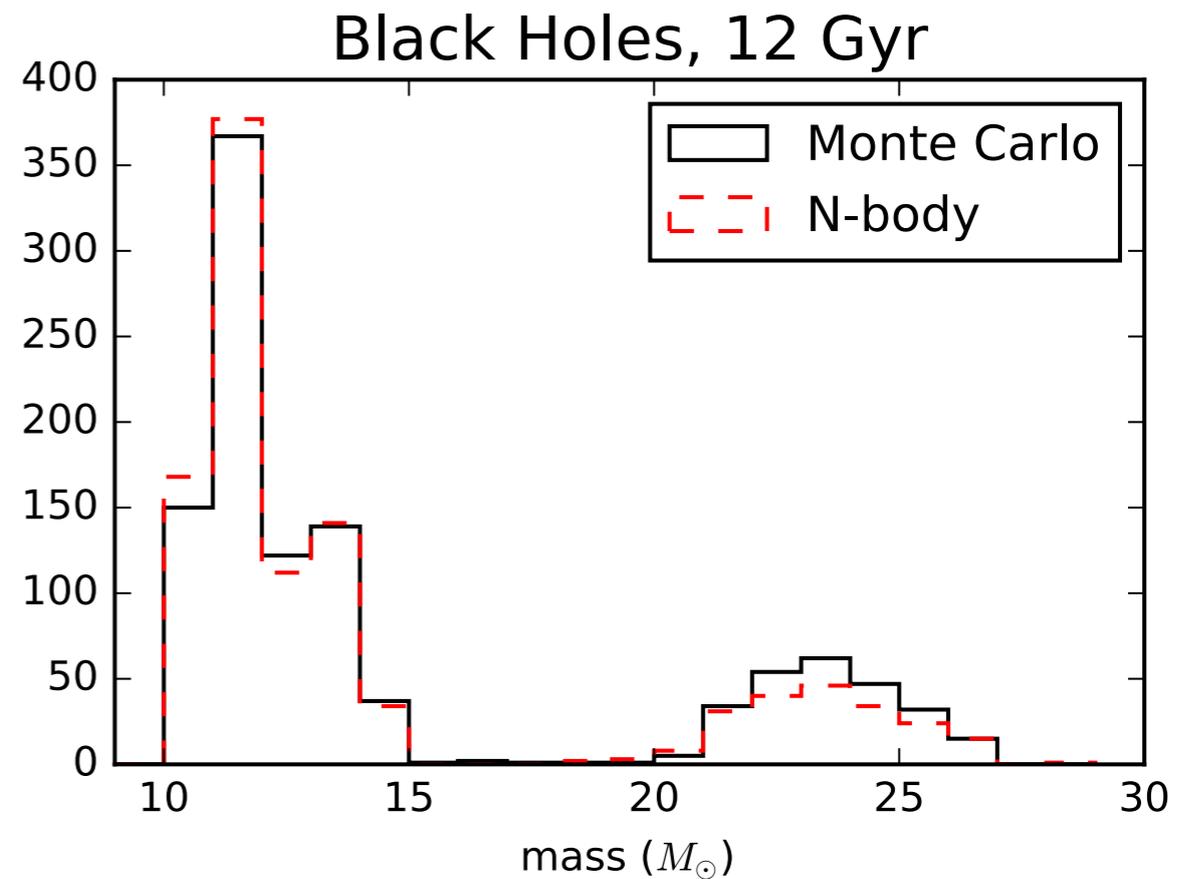
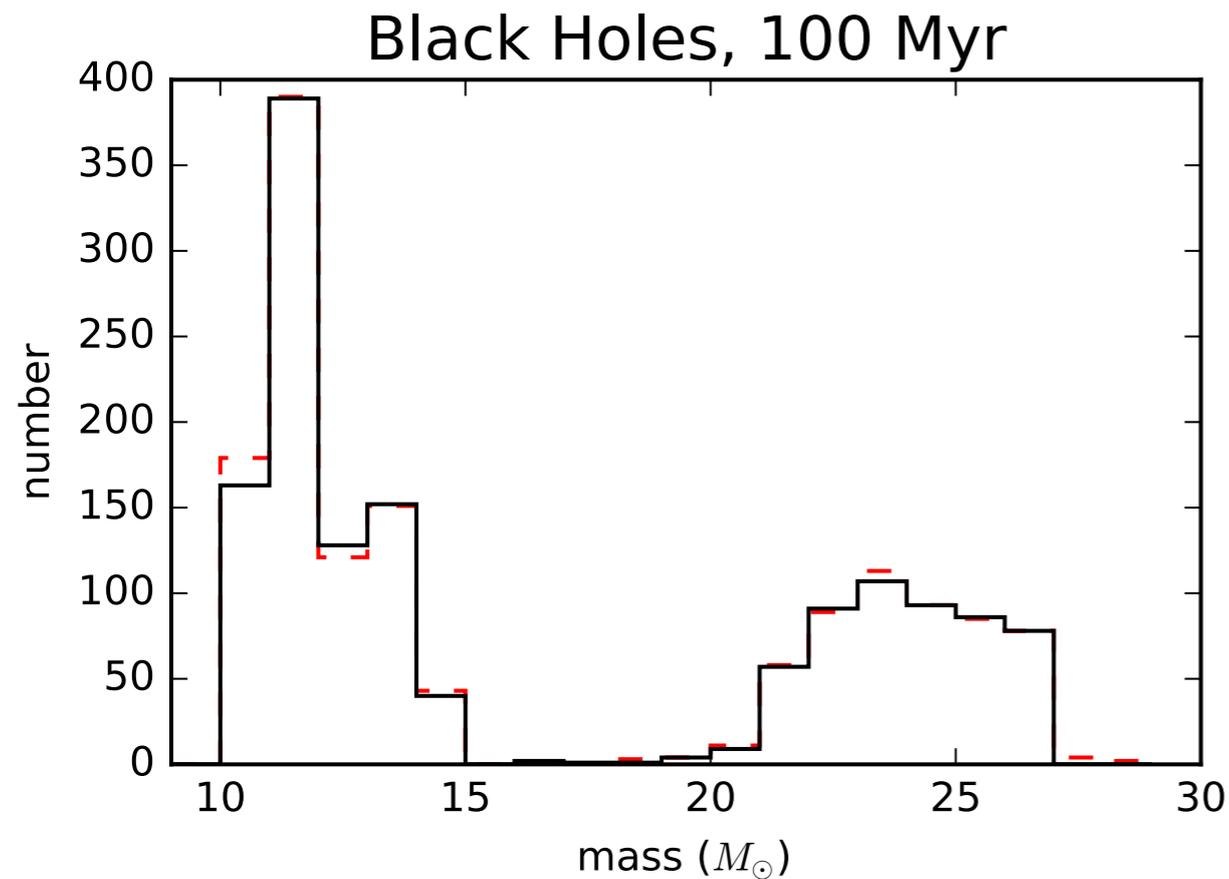
Speedup for the Sorting Module



Comparison to Direct *N*-body (Dragon) Results



Comparison to Direct N-body (Dragon) Results



CMC and Direct N-body cluster models with $N=10^6$

- NBODY6++GPU: about 0.5 year on 160 CPUs & 16 K20m GPUs!
- CMC: 2.5 days on 48 CPUs

Research Highlights Using CMC

In the era of GAIA, LIGO, & LISA

PRL 115, 051101 (2015)

PHYSICAL REVIEW LETTERS

week ending
31 JULY 2015

Binary Black Hole Mergers from Globular Clusters: Implications for Advanced LIGO

Carl L. Rodriguez,¹ Meagan Morscher,¹ Bharath Pattabiraman,^{1,2} Sourav Chatterjee,¹
Carl-Johan Haster,^{1,3} and Frederic A. Rasio¹

¹*Center for Interdisciplinary Exploration and Research in Astrophysics (CIERA) and Department of Physics and Astronomy, Northwestern University, 2145 Sheridan Rd, Evanston, Illinois 60208, USA*

²*Department of Electrical Engineering and Computer Science, Northwestern University, Evanston, Illinois 60208, USA*

³*School of Physics and Astronomy, University of Birmingham, Birmingham B15 2TT, United Kingdom*

(Received 2 May 2015; published 30 July 2015)

The predicted rate of binary black hole mergers from galactic fields can vary over several orders of magnitude and is extremely sensitive to the assumptions of stellar evolution. But in dense stellar environments such as globular clusters, binary black holes form by well-understood gravitational interactions. In this Letter, we study the formation of black hole binaries in an extensive collection of realistic globular cluster models. By comparing these models to observed Milky Way and extragalactic globular clusters, we find that the mergers of dynamically formed binaries could be detected at a rate of ~ 100 per year, potentially dominating the binary black hole merger rate. We also find that a majority of cluster-formed binaries are more massive than their field-formed counterparts, suggesting that Advanced LIGO could identify certain binaries as originating from dense stellar environments.

DOI: [10.1103/PhysRevLett.115.051101](https://doi.org/10.1103/PhysRevLett.115.051101)

PACS numbers: 04.30.Db, 98.20.-d

Research Highlights Using CMC

In the era of GAIA, LIGO, & LISA

- 8 journal papers using CMC results since MODEST 17
- Clusters affecting production of stellar exotica: E.g., merging BBHs, BH XRBs, LISA sources from GCs, MSPs, Subsubgiants, Blue Stragglers
- Compact remnants affecting clusters: E.g., effects of BH retention on cluster's observable and dynamical properties, ways to detect BH retention

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XRBs, LISA sources from GCs, MSPs, Subsubgiants, Blue Stragglers

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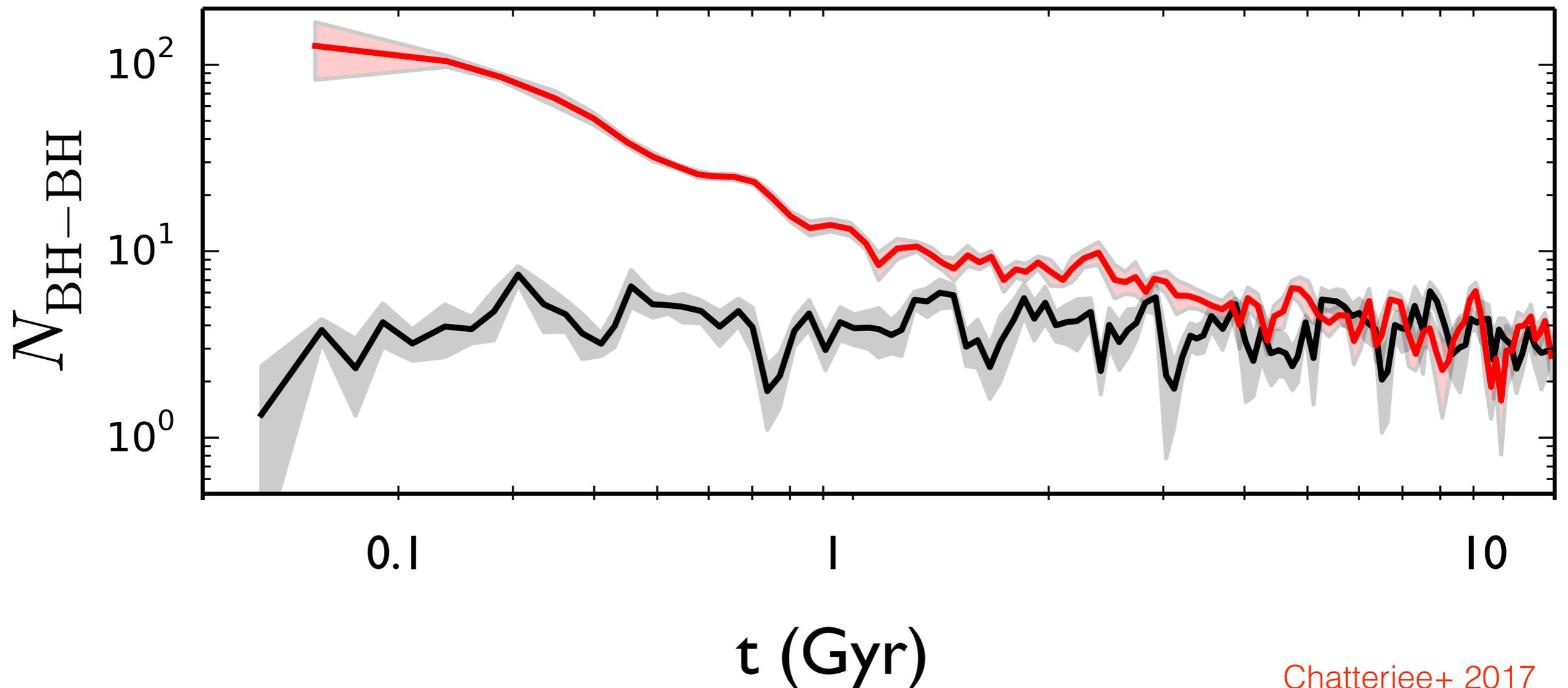
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- Critically question 'standard assumptions:'
 - E.g., Assumptions on BH natal kicks, initial binary properties, IMF, etc.
 - Metallicities and formation redshifts of massive clusters

Results Insensitive to Model Assumptions

BH-BH binaries in the cluster

Initial $f_{b, \text{high-mass}} = 1$

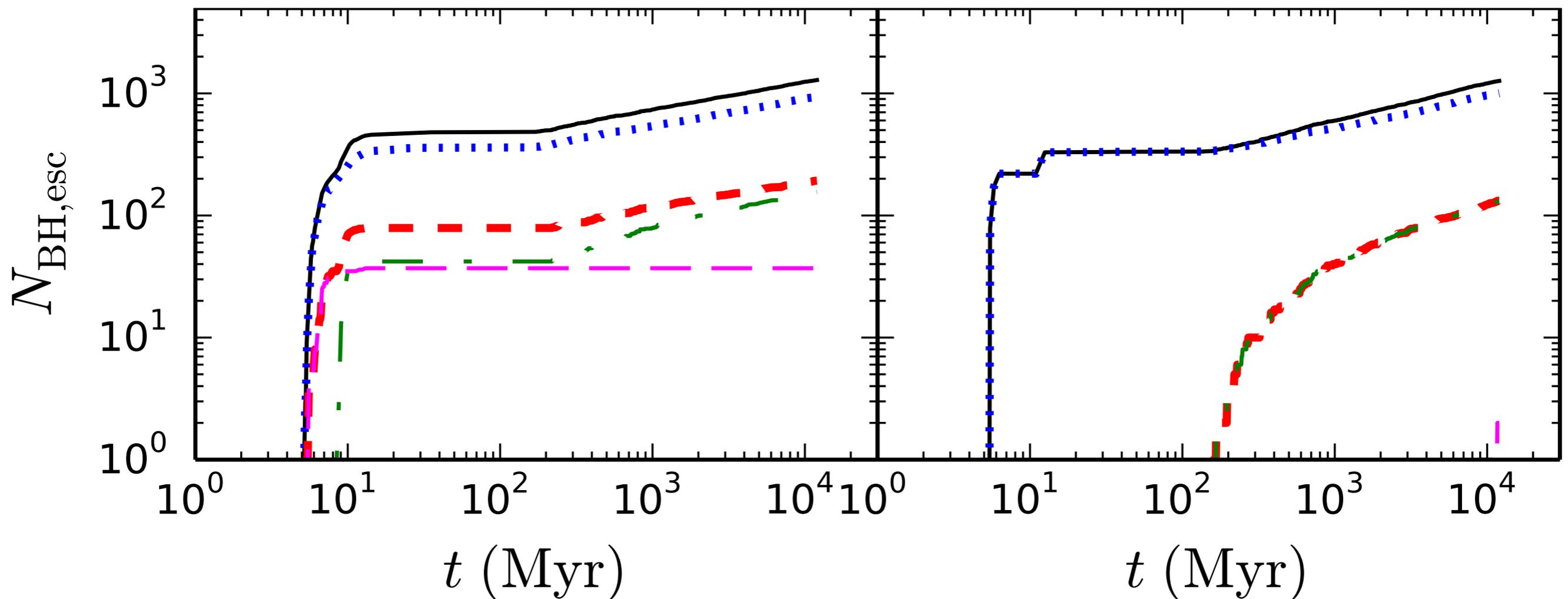
Initial $f_{b, \text{high-mass}} = 0$



Results Insensitive to Model Assumptions

Escaped BH-BH binaries

Chatterjee+ 2017



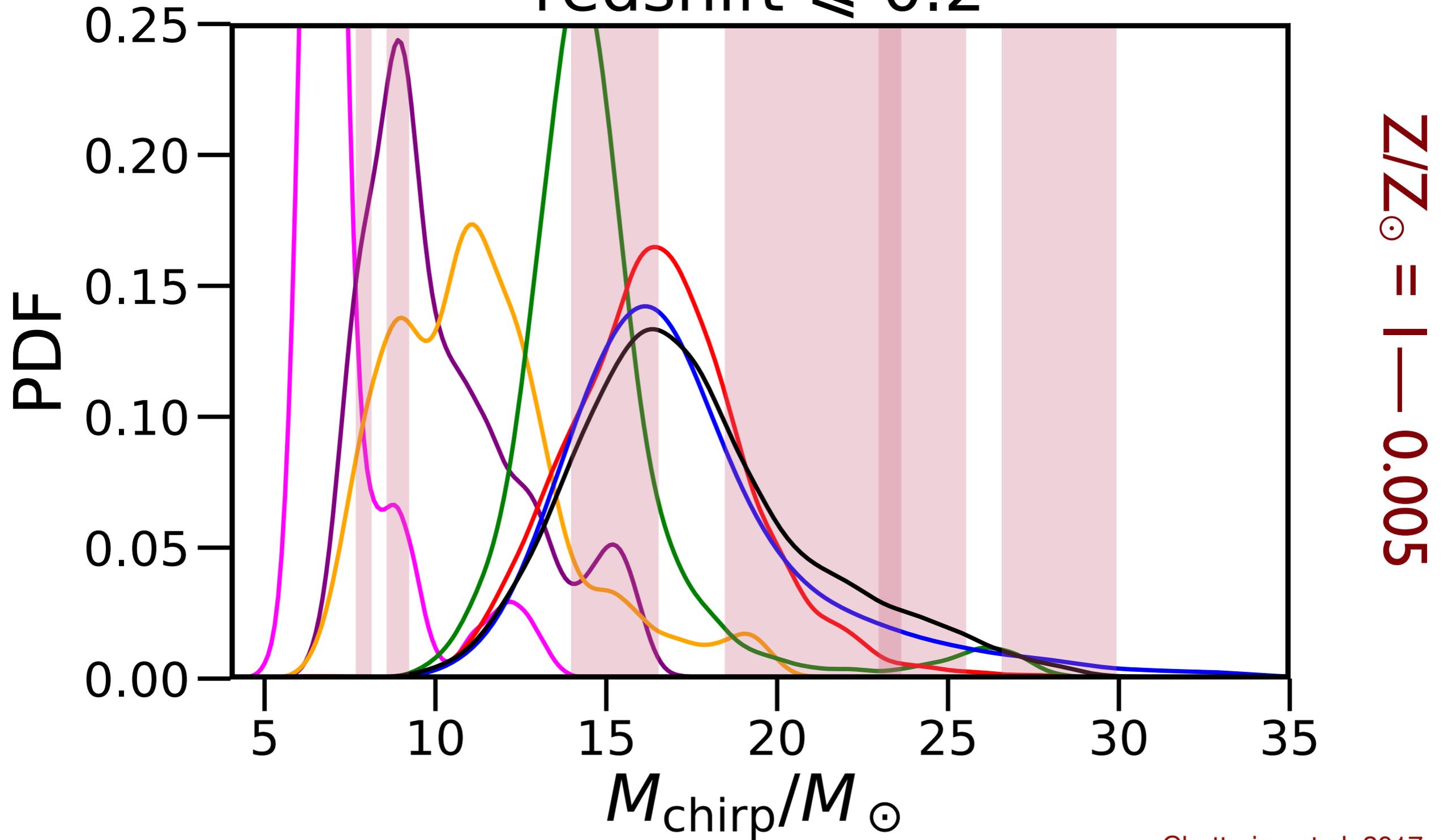
Initial $f_{\text{b, high-mass}} = 1$

Initial $f_{\text{b, high-mass}} = 0$

BH-BH Merger Properties as LIGO source

Masses

redshift ≤ 0.2



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 - Devised ways to detect BH retention in today's GCs
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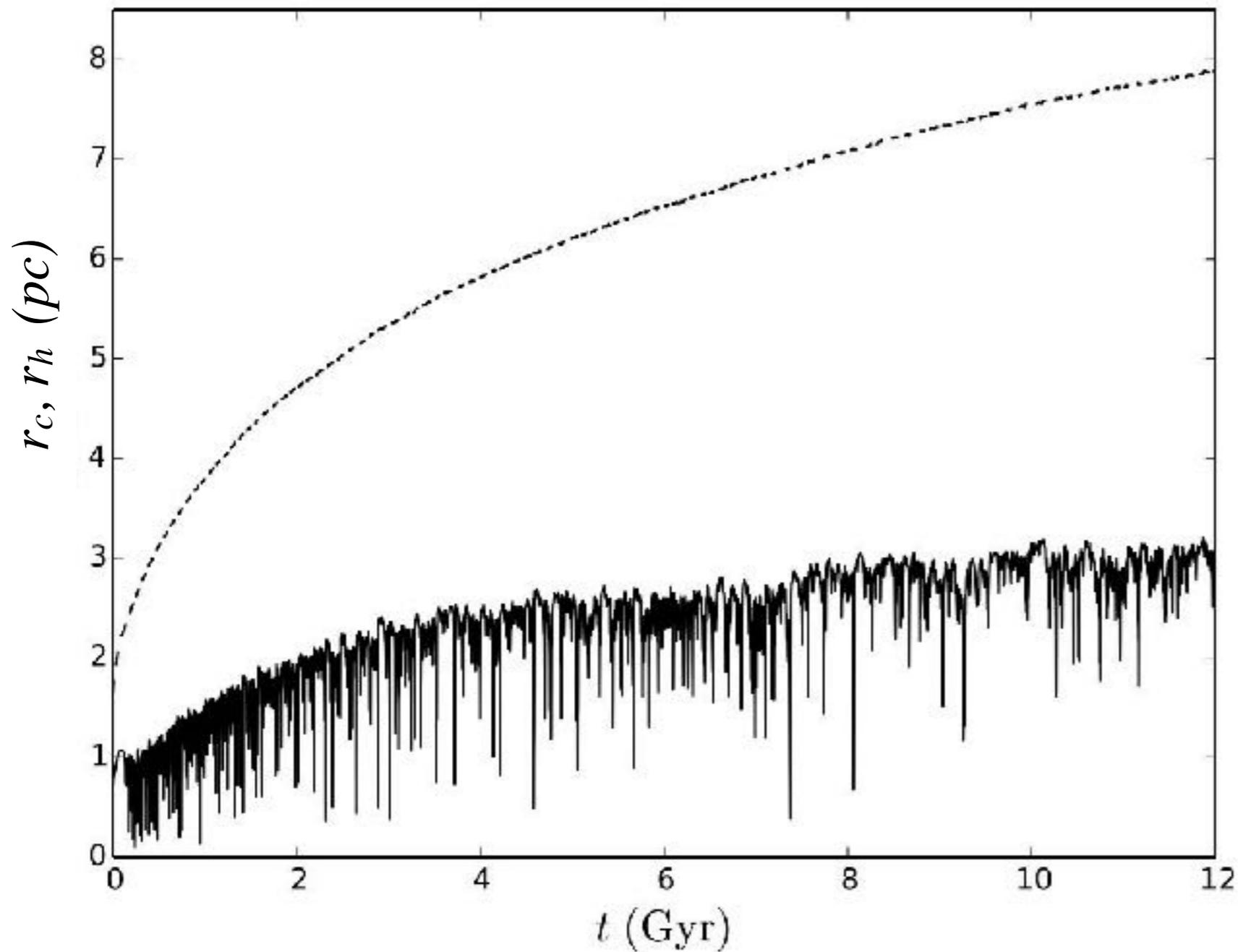


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Challenges in Measuring BH Retention

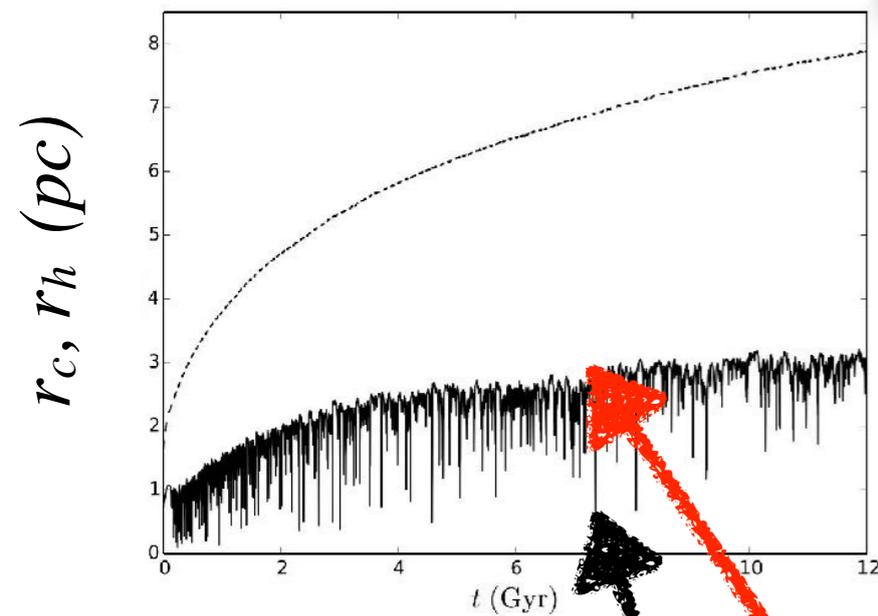


Repeated BH-driven collapse

Overall cluster expansion

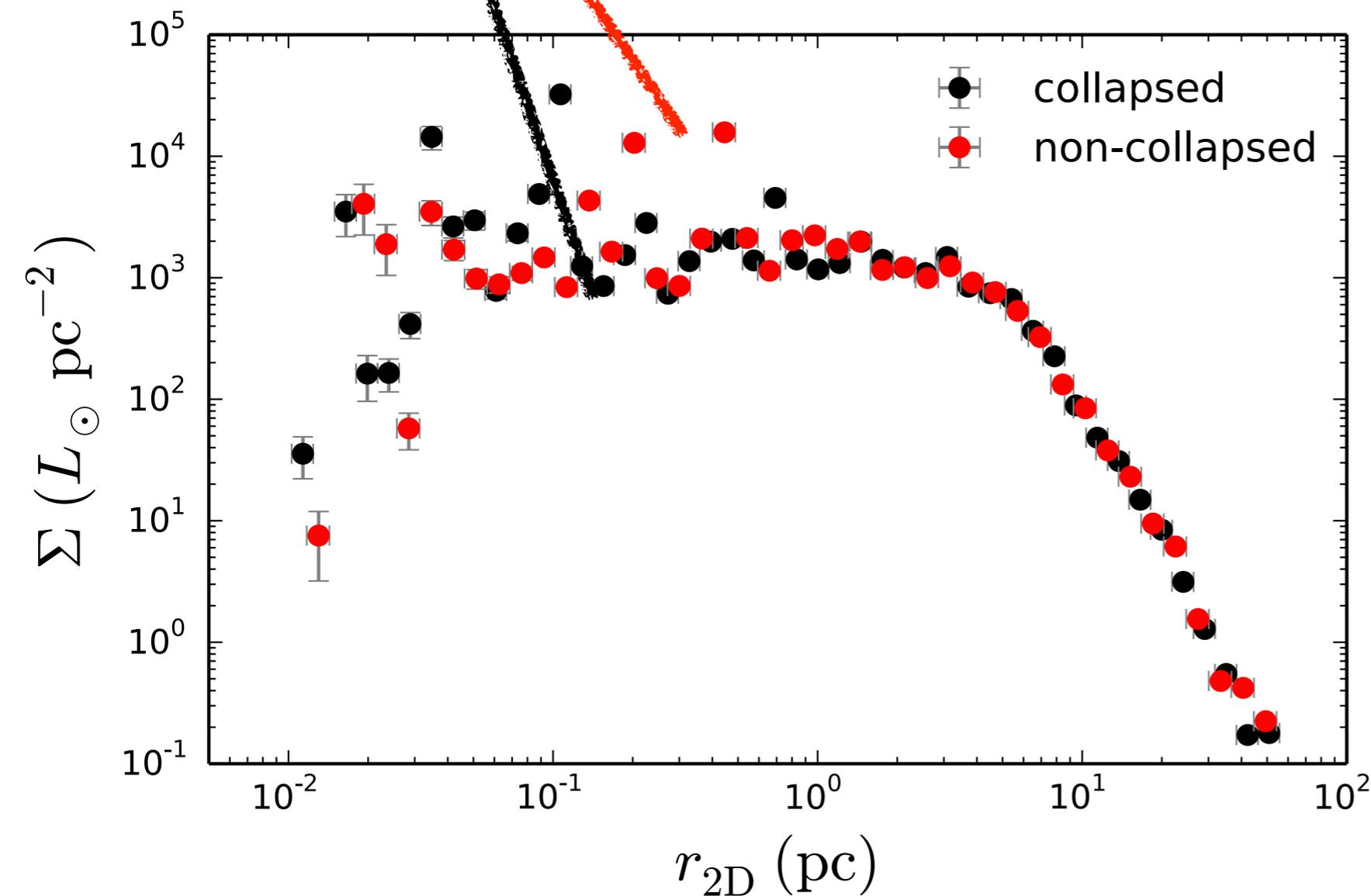
Challenges in Measuring BH Retention

little difference in SBP



Repeated BH-driven collapse

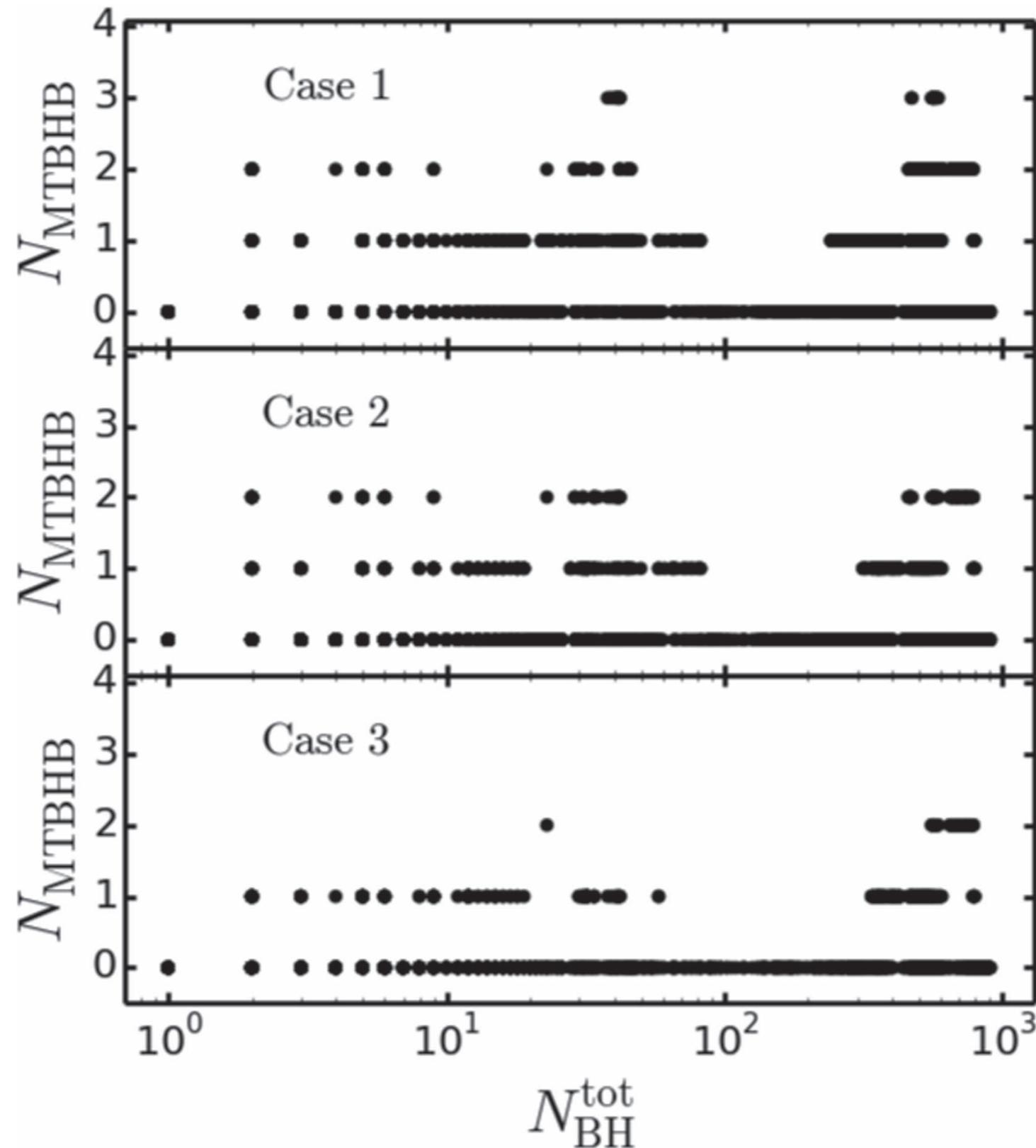
Overall cluster expansion



Little observable difference in surface brightness profile *in* and *out* of collapse

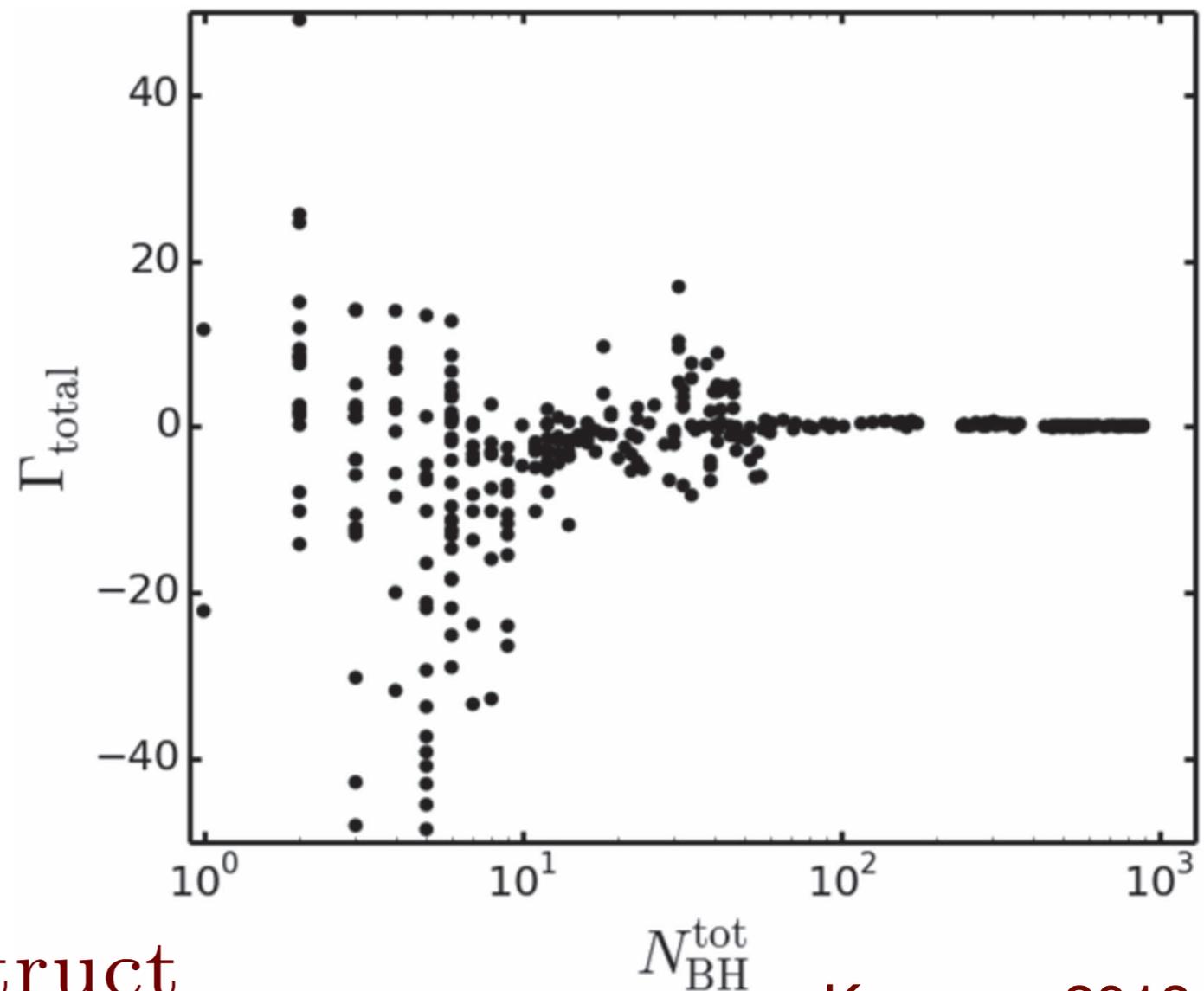
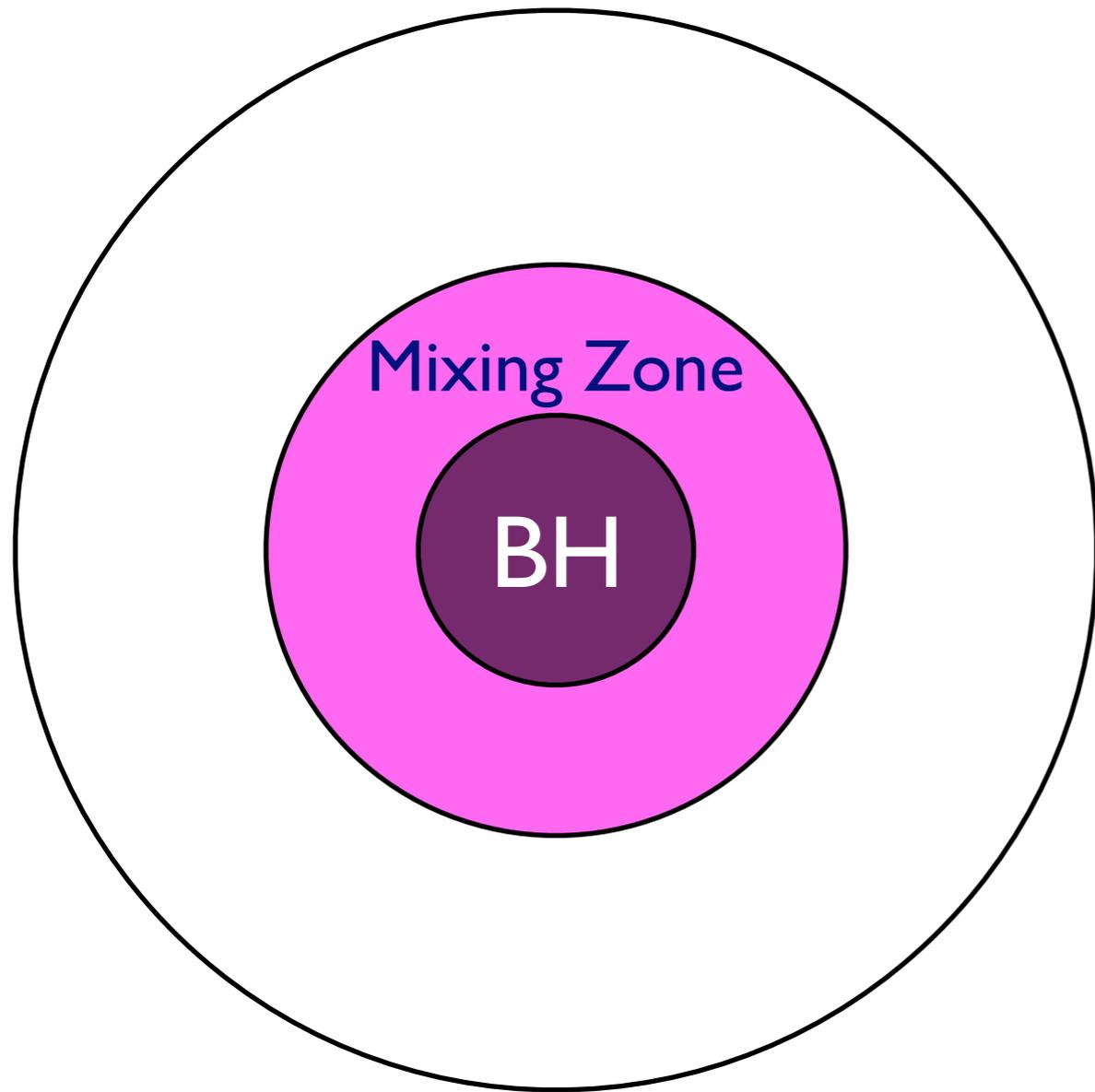
Challenges in Measuring BH Retention

no correlation between N_{BH} and N_{BHMTB}



Challenges in Measuring BH Retention

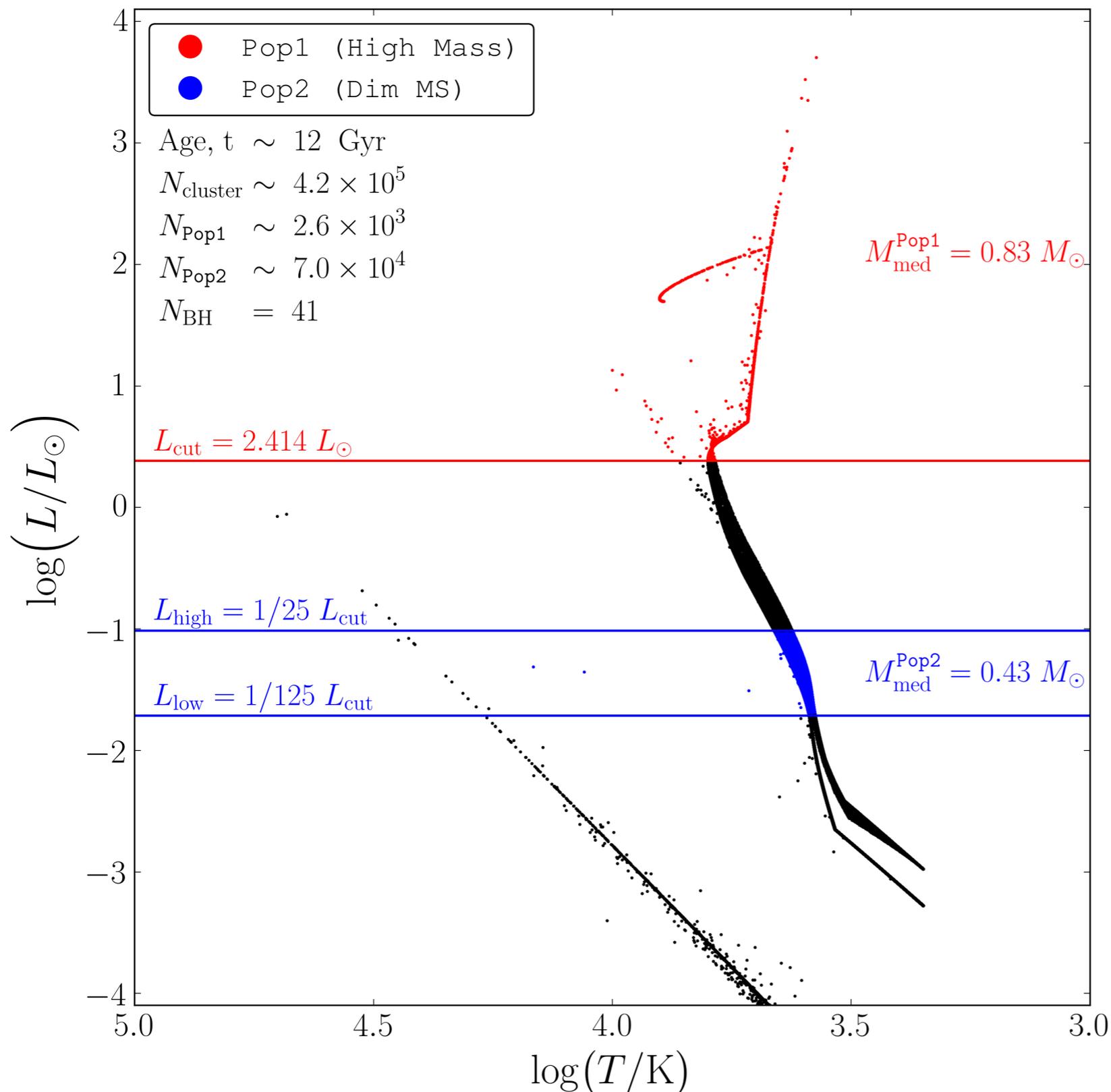
no correlation between N_{BH} and $N_{\text{BH-nonBH}}$



$$\Gamma_{\text{total}} \equiv \Gamma_{\text{form}} - \Gamma_{\text{destruct}}$$

Measuring BH Retention

Dynamical Signature e.g., Mass Segregation (Δ)

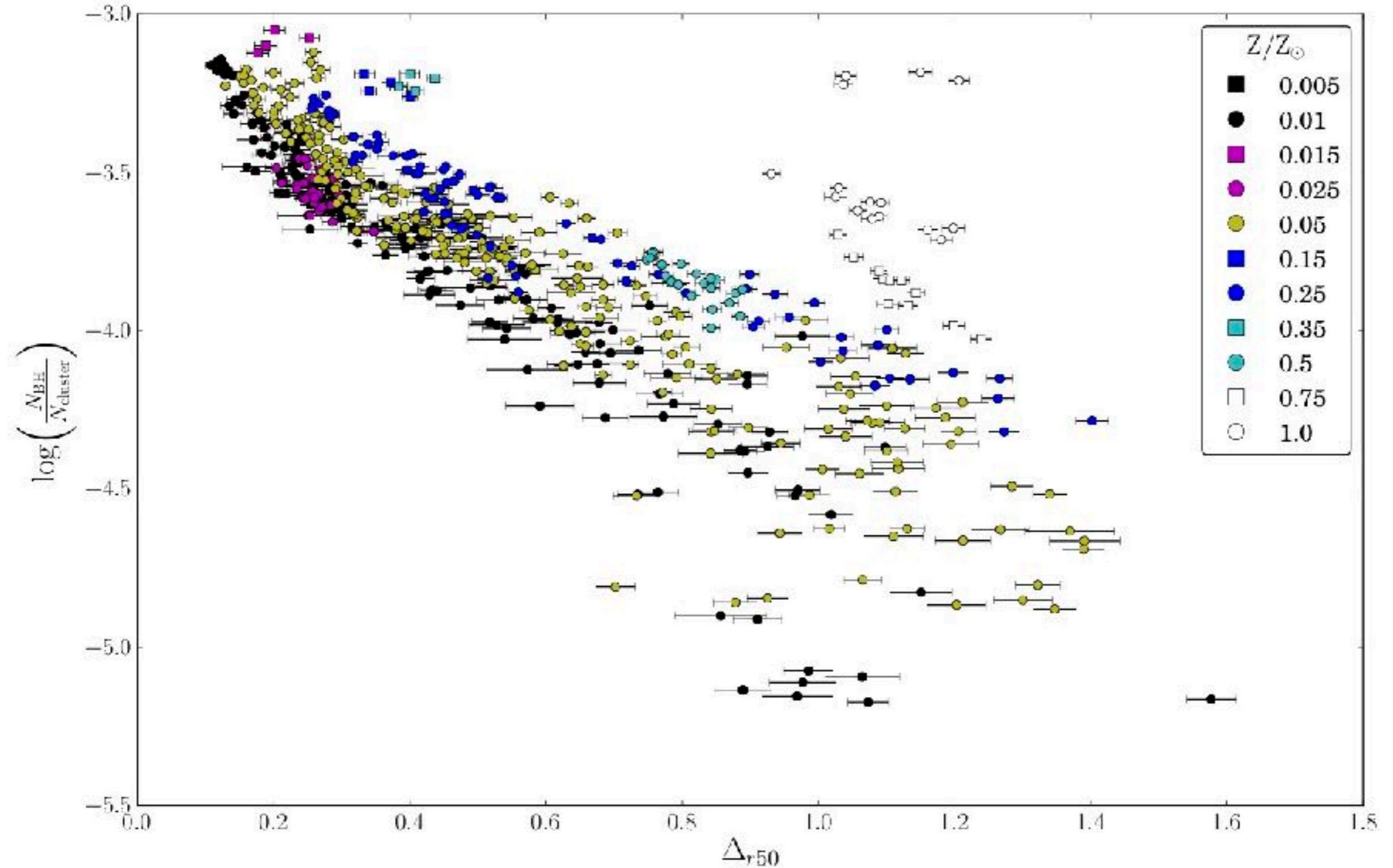


Requirements:

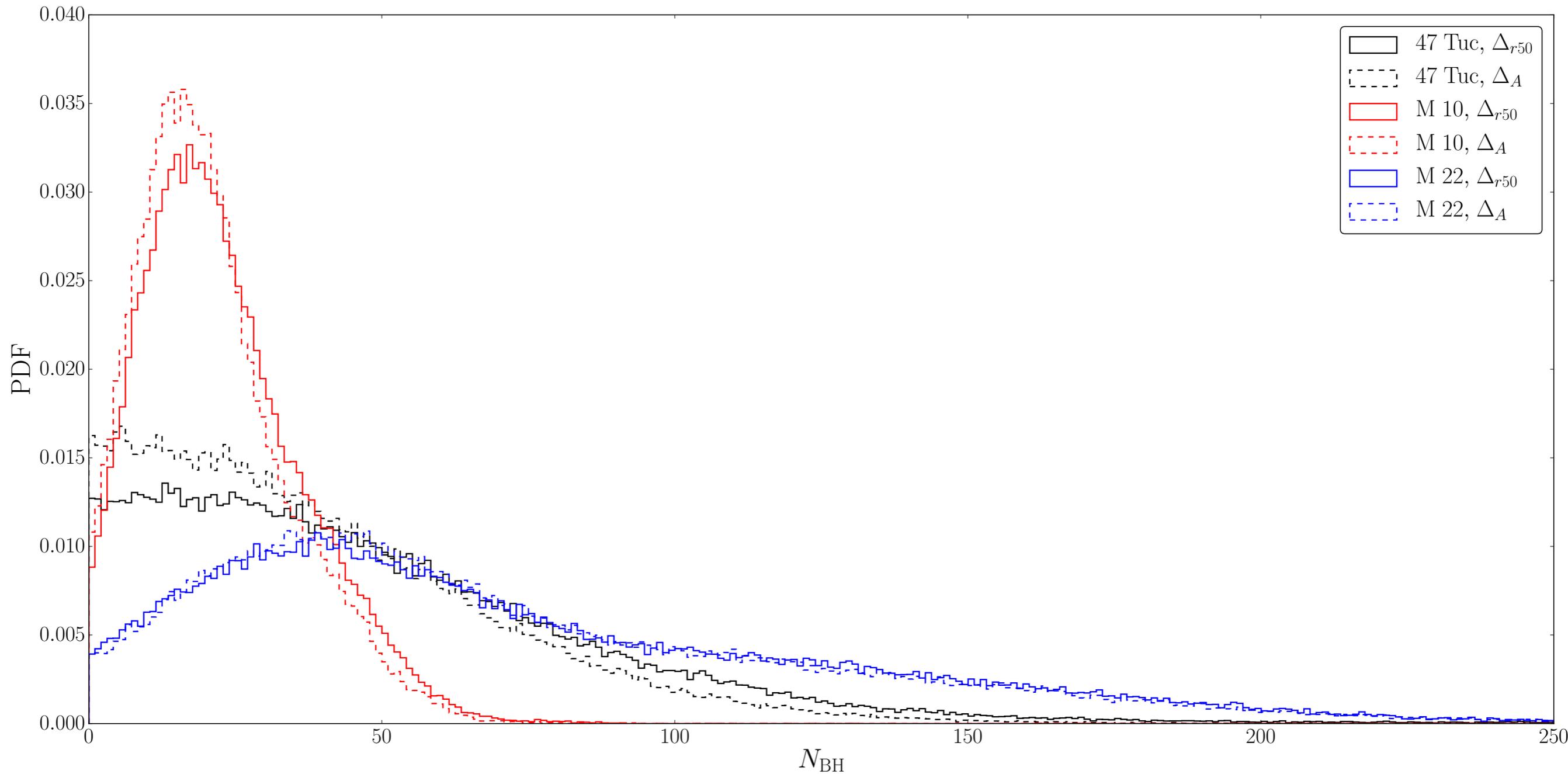
- Must be able to uniquely and consistently define groups in observed clusters and models
- Each group must have large memberships
- Need to be very careful about biases and incompleteness differences

Strong Anticorrelation:

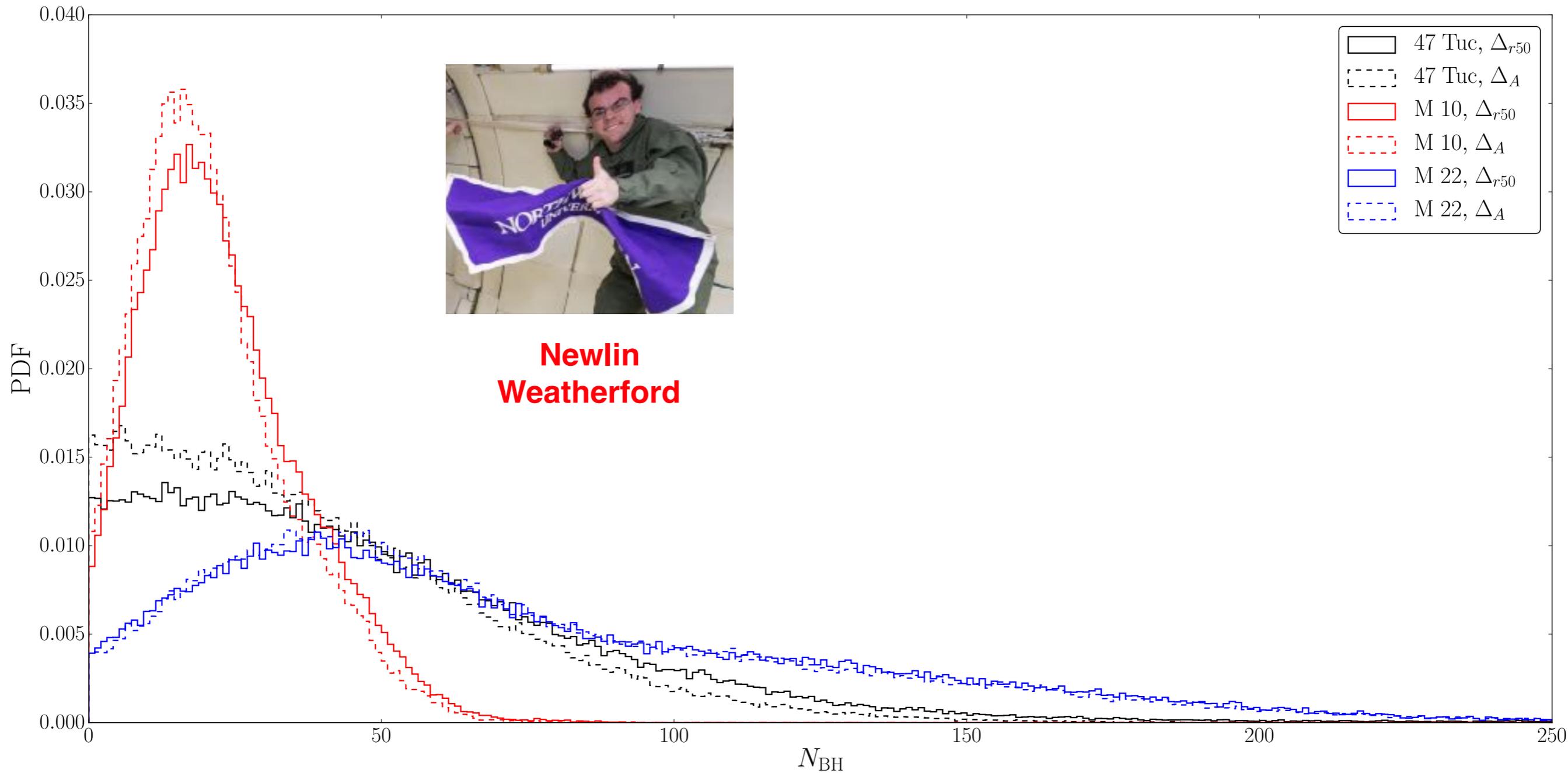
Δ vs N_{BH}



Strong Anticorrelation: Inferred N_{BH} from measured Δ



Strong Anticorrelation: Inferred N_{BH} from measured Δ



Upcoming Improvements to CMC

- We are now getting ready to create a grid of simulations using up to PN 2.5 terms and all code improvements (~ few months)
- State-of-the-art prescriptions for BHs, e.g., fallback modulated natal kicks, delayed supernova, Z -dependent maximum BH mass, etc.
- Addition of octuple-order effects from hierarchical triples (~ this year)
- Effects are expected to be small, but strange systems may form

Other Talks & Posters Using CMC

In the era of GAIA, LIGO, & LISA



Carl Rodriguez

Wed. Evening
PN effects &
Repeated BBH
Mergers in GCs



Kyle Kremer

Wed. Morning
BHs shaping the fate
& properties of GCs



Katie Breivik

Wed. Evening
LISA sources in GCs



Claire (Shi) Ye

Thu. Morning
Modeling MSPs in
GCs



**Newlin
Weatherford**

Predicting stellar-
mass BH
populations in
GCs



Katie Breivik

Revealing BH
binaries with GAIA

Talks

Posters