

Extrapolation of Treatment Effect Estimates Across Contexts
and Policies:
An Application to Cash Transfer Experiments

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Two extrapolation approaches

- Evidence-based policymaking is challenging
 - External validity not always guaranteed
 - From which evidence to extrapolate?
- 1. Extrapolation across contexts (within policies)
 - Policy A in context X \Leftarrow Policy A in **context Y**
- 2. Extrapolation across policies (within contexts)
 - Policy A in context X \Leftarrow **Policy B** in context X
- **Do two extrapolations result in different predictions?**
 - No theory & limited empirical evidence
 - Comparative analysis using **cash transfer experiments**

Cash transfer experiments

- Conditional cash transfers (CCTs) on school enrollment rates
 - Common version: conditional on regular school attendance
 - Popular anti-poverty policy (e.g. PROGRESA, Bolsa Familia, RPS)
 - Abundant empirical evidence showing **positive effects**
- Varying cost-effectiveness across programs
 - Heterogeneity in effect size ▶ Effect size by transfer amount
- Data: two RCTs in Malawi & Morocco
 - CCTs implemented in both RCTs
 - “Unconditional” cash transfers in Moroccan RCT

Overview



- Predict average effect of Moroccan CCTs on school enrollment rates
 - CCTs: cash transfers if school attendance $>$ threshold
 - LCTs: cash transfers $\perp\!\!\!\perp$ school attendance
- Compare predictions with actual treatment effect estimate
 - Predictions via **standard** method (Data-driven vs Structural)
 - Predictions via **same** method (Structural vs Structural)
- Identify source of prediction differences through structural model

Preview of findings

- **Moroccan LCTs** make more accurate predictions than **Malawi CCTs**
 - Estimated effect = 5.7 ppt: **5.9 ppt** vs **21.2 ppt**
 - Statistically significant difference only for **across-contexts**
 - Relative performance unchanged when using same method
- **(Perceived) returns to schooling** explain prediction differences
 - Key parameters in schooling decisions: cost today vs return tomorrow
 - Estimated cost of schooling: similar for **same policy**
 - Estimated returns to schooling: similar for **same context**
 - Discussion on varying perceived returns to schooling across contexts

Contributions to literature

- **Empirical investigation of out-of-sample predictions**
 - Pritchett and Sandefur (2015); Gechter et al. (2018)
 - Prediction performance of across-policies extrapolation
 - Comparative analysis of two extrapolation approaches
- Structural estimation with RCTs in development economics
 - Todd and Wolpin (2006); Attanasio et al. (2012)
 - Identification of flexible model about schooling
- New identification of dynamic discrete choice model
 - Scott (2014); Kalouptside et al. (2021)
 - No rational expectations assumption
 - First application to schooling decisions

Two cash transfer experiments

- Malawi (Baird et al., 2011)
 - Treatment: CCTs
 - Target: **girls at secondary school ages** (13 - 22 years old)
 - Teenage pregnancy & marriage as main driver of dropout
- Morocco (Benhassine et al., 2015)
 - Treatment: CCTs and LCTs (Labeled Cash Transfers)
 - Target: **boys and girls at primary school ages** (6 - 15 years old)
 - Various reasons to drop out: school quality, financially, domestic work
 - LCTs \neq UCTs due to **endorsement effects**

Treatment effect estimates on school enrollment rates

	Malawi	Morocco	
	CCTs	CCTs	LCTs
Treatment	0.0369* (0.0200)	0.0567*** (0.0106)	0.0726*** (0.0107)
Control mean	0.896*** (0.0154)	0.894*** (0.00951)	0.893*** (0.00833)
Obs.	1490	4982	3018

*** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- Estimated effects greater (not statistically)
 - for LCTs within contexts
 - for Morocco within policies

Across-context: linear projection

- Heterogeneous treatment effect approach
 1. Estimate linear regression with Malawi CCTs data

$$d_i = W_i' \beta^{\text{HTE}} + \beta_0^{\text{HTE}} \text{Treatment}_i + \sum_{k=1}^K \gamma_k^{\text{HTE}} \text{Treatment}_i \times w_{ik} + \omega_i$$

2. Predict d_i in Moroccan CCTs data using estimated linear model
3. Estimate treatment effect via OLS

$$\hat{d}_i = \alpha_0^{\text{HTE}} + \alpha_1^{\text{HTE}} \text{Treatment}_i + \text{Stratum}_i + \nu_i^{\text{HTE}}$$

- $W_i =$ (age, education, per-capita income, school costs, transfer amount)
- Key assumption: **cond. on W_i , potential outcomes $\perp\!\!\!\perp$ contexts**

Across-policies: dynamic model of schooling

- Child i makes binary schooling decisions over finite time horizon
 - Schooling ($d_i = 1$): pay school costs (s_i), add 1 year of education
 - Non-schooling ($d_i = 0$): consume (per-capita) income (y_i)
 - Flow utility function: $u(c) = \theta \ln(c_i)$
- At terminal period T , child receives lump-sum returns
 - Returns are a function of education: $R_i = R(e_{i,T}) = R\left(e_{i,t} + \sum_{\tau=t}^{T-1} d_{i,\tau}\right)$
- Cash transfers (z_i) relax budget constraints exogenously
 - Budget constraint: $c_i = y_i - d_i \times s_i$
 - CCTs lower school costs: $s_i = s_i - z_i$ if i in treatment group
 - LCTs increase income: $y_i = y_i + z_i$ if i in treatment group

► Formal representation

Prediction with θ & $R(e_{i,T})$

- Predict prob. of schooling under Moroccan CCTs

$$\hat{P}(d = 1 | e_{i,2}, y_{i,2}, s_{i,2}) = \frac{\exp\left(\hat{\theta} \ln\left(\frac{y_{i,2} - s_{i,2}}{y_{i,2}}\right) + \beta \widehat{\Delta R}(e_{i,2})\right)}{1 + \exp\left(\hat{\theta} \ln\left(\frac{y_{i,2} - s_{i,2}}{y_{i,2}}\right) + \beta \widehat{\Delta R}(e_{i,2})\right)}$$

- Estimate treatment effect via OLS

$$\hat{P}(d = 1 | e_{i,2}, y_{i,2}, s_{i,2}) = \delta_1 + \delta_2 \text{Treatment}_i + \text{Stratum}_i + \nu_i$$

Structural estimation: sketch

1. Compute probability of schooling in all possible state values
 - Frequency estimator or **parametric to smooth across states**
2. Consider two hypothetical paths for each individual
 - (Baseline, Midline) = (Schooling, Non-schooling), (Non-schooling, Schooling)
 - Same years of education in next period after Midline
 - **Continuation values after Midline fixed**
3. Compare changes in probability of schooling across these paths
 - Differences only in flow utilities between Baseline and Midline
 - **Δ in prob $\Leftrightarrow \Delta$ in flow utility, shifted by cash transfers**
 - Size of Δ in flow utility different across CCTs and LCTs

► Formal derivation

Identification of θ using cash transfers

$$\underbrace{\ln \frac{P_{it}^1}{1 - P_{it}^1} - \beta \ln \frac{P_{i,t+1}^2}{1 - P_{i,t+1}^3}}_{\text{Change in prob. of schooling across paths}} = \theta \underbrace{\left\{ \ln \left(\frac{y_{it} - s_{it}}{y_{it}} \right) - \beta \ln \left(\frac{y_{i,t+1} - s_{i,t+1}}{y_{i,t+1}} \right) \right\}}_{\text{Change in flow utility of schooling across paths}} + \underbrace{\beta (\eta_{it}(1) - \eta_{it}(0))}_{\text{Expectation errors at baseline (Unobservable)}}$$

- **Endogeneity: expectation errors correlated with income levels**
 - e.g.) information friction, ability to forecast
- **Treatment assignment as an IV**
 - Relevance: cash transfers (only) shift school costs (\downarrow) or income (\uparrow)
 - Exclusion: assignment $\perp\!\!\!\perp$ baseline expectation

Identification of $R(e; x)$

- Identification of terminal payoffs depends on time horizon
- Set terminal period at one period after Midline ($T = 3$)
- Expand prob. of schooling at Midline ($t = 2$)

$$\underbrace{\ln \frac{P_{i,2}^1}{1 - P_{i,2}^1}}_{\text{Odds of schooling}} = \underbrace{\theta \ln \left(\frac{y_{i,2} - s_{i,2}}{y_{i,2}} \right)}_{\text{Flow utility of schooling}} + \beta \underbrace{(R(e_{i,2} + 1; x_{i,2}) - R(e_{i,2}; x_{i,2}))}_{\equiv \Delta R(e_{i,2}; x_{i,2})}$$

- $\Delta R(e_{i,2}; x_{i,2})$: Perceived relative returns to schooling
 - **Schooling unexplained by contemporaneous effects of cash transfers**
 - Consequences of schooling decisions after RCTs
 - Heterogenous across state values

Across-contexts (reduced-form) vs Across-policies (structural)

	Target	Across-contexts	Across-policies
Treatment	0.0567*** (0.0106)	0.212*** (0.00442)	0.0590*** (0.00545)
Control mean	0.894*** (0.00951)	1.127*** (0.00373)	0.941*** (0.00531)
Obs.	4982	4982	4982
= Target TE		0.000	0.674
= Target control mean		0.000	0.000

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- **Across-contexts**: significantly overpredict
- **Across-policies**: numerically and statistically accurate

Across-contexts (structural) vs Across-policies (structural)

	Target	Across-contexts	Across-policies
Treatment	0.0567*** (0.0106)	0.0431*** (0.00465)	0.0590*** (0.00545)
Control mean	0.894*** (0.00951)	0.702*** (0.00390)	0.941*** (0.00531)
Obs.	4982	4982	4982
= Target TE		0.004	0.674
= Target control mean		0.000	0.000

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- **Across-contexts**: slightly but statistically significantly underpredict

▶ How to extrapolate $\Delta R(e; x)$

▶ Why improvement via structural method?

Comparison of θ and $\Delta R(e; x)$

- Comparative analysis at model parameter level
 - Structural model estimated for each intervention (including Moroccan CCTs)
 - Comparison of parameter estimates across interventions
 - Identification of varying DGP if model is true ▶ Check model fit
- Two parameters that determine schooling decisions
 - Flow utility cost of schooling: $\theta \ln(y - d \times s)$
 - Perceived relative returns to schooling: $\Delta R(e; x)$

Comparison of θ

	Malawi	Morocco	
	CCTs	CCTs	LCTs
θ	1.008*** (0.256)	2.670*** (0.454)	38.90*** (11.30)
Obs.	1479	4981	3016
1st stage F statistics = target θ	113.011	3843.510	25.483
	0.000		0.001

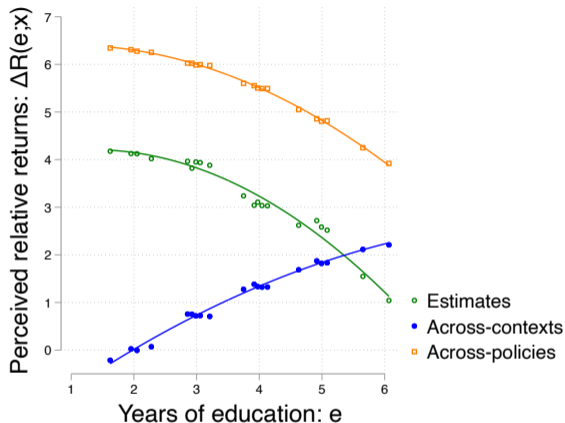
Note: I report the Kleiberg-Paap F statistics for weak identification. *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- Numerically closer estimates if [same policy](#)

► Compare elasticity

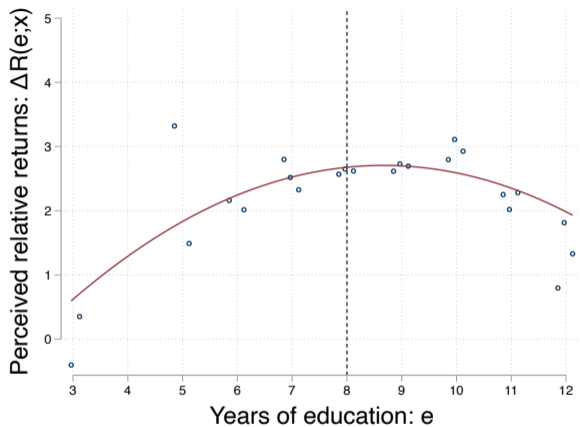
► Replace with estimated values

Comparison of $\Delta R(e; x)$



- Estimate of $\Delta R(e; x)$: downward sloping due to increasing opportunity costs
- $\Delta R(e; x)$ from Moroccan LCTs: parallel to target values
- $\Delta R(e; x)$ from Malawi CCTs: opposite direction

Why extrapolation of $\Delta R(e;x)$ from Malawi CCTs wrong?



- Increase during primary education
- Start decreasing at which school dropout becomes more realistic
- Naive extrapolation: use increasing part to predict in target context

What explains variation in perceived returns across contexts?

- Perceived relative returns to schooling are key for prediction accuracy
 - Negative correlation bet. estimates and extrapolation across contexts
- To what extent differences in $\Delta R(e; x)$ explained by observables?
 1. Normalize years of education of Malawi sample
 2. Restrict sample by age and sex

Normalization of years of education

	Target	Across-contexts		
Treatment	0.0567*** (0.0106)	0.0431*** (0.00465)	0.0150*** (0.000788)	0.0147*** (0.00265)
Control mean	0.894*** (0.00951)	0.702*** (0.00390)	0.903*** (0.000674)	0.875*** (0.00221)
Obs.	4982	4982	4982	4982
Normalization			✓	✓
Sample restriction				✓
= Target TE		0.004	0.000	0.000
= Target control mean		0.000	0.000	0.000

Note: *** p<0.01 ** p<0.05 * p<0.1

- Extrapolation using decreasing part of $\Delta R(e; x)$
- Treatment effect still underpredicted (while overall prediction improved)

Heterogeneity by sex of Moroccan sample

	Target		Across-contexts	
	Boys	Girls	Boys	Girls
Treatment	0.0479*** (0.0130)	0.0681*** (0.0144)	0.0151*** (0.00109)	0.0148*** (0.00129)
Control mean	0.912*** (0.0115)	0.871*** (0.0129)	0.902*** (0.000913)	0.903*** (0.00112)
Obs.	2666	2313	2666	2313
= Target TE			0.000	0.000
= Target control mean			0.000	0.000

Note: *** p<0.01 ** p<0.05 * p<0.1

- Prediction separately by sex of Moroccan sample
- No additional improvement

Heterogeneity by age for Malawi Sample

	Target		Across-contexts	
	Boys	Girls	Boys	Girls
Treatment	0.0479*** (0.0130)	0.0681*** (0.0144)	0.00376*** (0.000254)	0.00402*** (0.000318)
Control mean	0.912*** (0.0115)	0.871*** (0.0129)	0.980*** (0.000211)	0.980*** (0.000270)
Obs.	2666	2313	2666	2313
= Target TE			0.000	0.000
= Target control mean			0.000	0.000

Note: *** p<0.01 ** p<0.05 * p<0.1

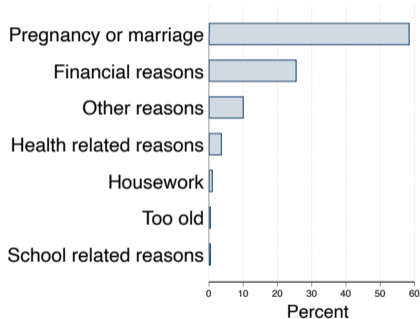
- Prediction based on young Malawi sample (age < 17)
- No additional improvement

Plausible explanations for no improvement

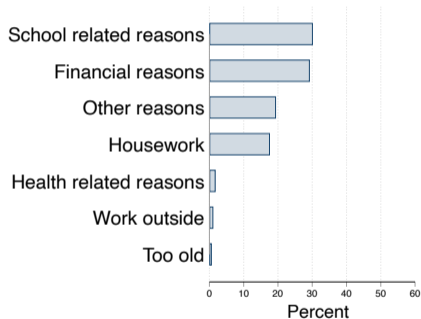
1. Two Moroccan cash transfers are more alike than two CCTs ▶ ATE estimates
 - **Endorsement effects** ▶ Within-intervention variation
 - Confusion about conditionality of Moroccan CCTs ▶ Under perfect knowledge
2. **Outside options are different across contexts**
 - $\Delta R(e; x)$ represents returns relative to **outside options**
 - Suggestive evidence by looking at primary reasons for school dropout

Varying outside options across contexts

Malawi CCTs



Moroccan CCTs



- Primary reasons for dropout differ across contexts
- Differential consequences of non-schooling

Conclusion

- When across-contexts extrapolation does not work, what can we do?
 - Status-quo approach in out-of-sample predictions
 - Empirical evidence on limitation of across-contexts extrapolation
- This paper sheds light on potentials of across-policies extrapolation
 - Similar policy that resembles how target policy works
 - Cash transfers w/o regular school attendance for CCTs
 - Proof-of-concept analysis but relevant beyond CCTs
- Across-policies dominates across-contexts due to perceived returns to schooling
 - Perceived returns to schooling more context-dependent
 - Suggestive explanations: endorsement effects & outside options

Extensions

1. Can we generalize empirical findings in this paper?
 - Three ways to generalize: contexts, policies, and methods
 - Conditions for better predictions via across-policies extrapolation
2. What features are must-have for accurate predictions?
 - WTP for precise estimates of policy effects (e.g. Hjort et al. 2021)
 - Policy designs useful for future predictions
 - Any unintended consequences of such designs?
3. Can we aggregate evidence from multiple policies?
 - Recent development on aggregation for same policies (Meager, 2019, 2022)
 - e.g.) Better predictions by using Malawi CCTs and Moroccan LCTs?

Thank you very much! Feel free to email your comments!
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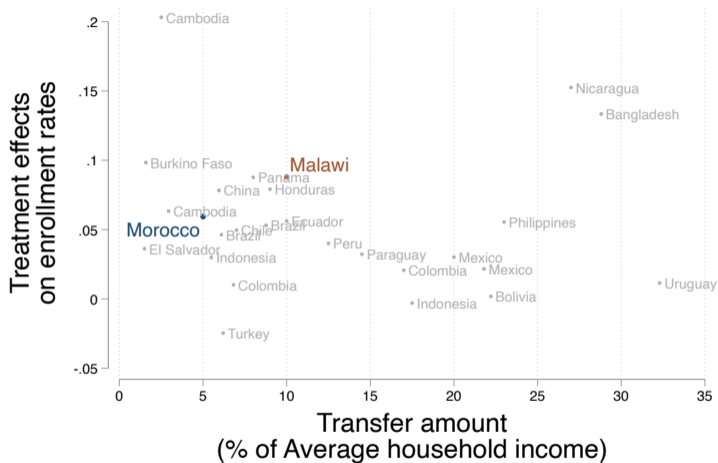
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Collection of CCTs effect estimates



Source: Baird et al. (2014)

Summary statistics at baseline

	Malawi		Morocco		
	Control	CCTs	Control	CCTs	LCTs
= 1 if enrollment	1.000	1.000	0.909	0.921	0.920*
Years of education	8.046	7.960	2.755	2.776*	2.764
Per-capita income (in 100 USD)	1.173	1.571	5.368	5.335	5.345
School costs (in 100 USD)	0.123	0.124	0.213	0.212	0.212
Cash transfers (in 100 USD)	NA	1.006	NA	1.054	1.057
=1 if girls	1.000	1.000	0.448	0.471*	0.486**
Age	14.964	14.740	9.889	9.910	9.912
Obs.	1145	412	1276	3706	1740
Joint F-test		0.153		0.250	0.106

Discussion on LCTs vs CCTs in Morocco

- Why LCTs and CCTs comparable?
 1. Endorsement effect driving cash transfer effects
 2. CCTs misperceived as unconditional
- Why LCTs more effective than CCTs?
 - LCTs compliers: children not confident about regular school attendance
- Do Moroccan CCTs differ from Malawi CCTs?
 - Endorsement effect attached to Malawi CCTs
 - Conditionality correctly understood in Malawi CCTs

Across-context: Reweighting

- Propensity score weighting (Stuart et al., 2011)
 1. Pool Malawi and Moroccan data
 2. Estimate propensity score of being in Malawi data via logit

$$\mathbf{1}\{i \in \text{Malawi CCTs}\} = W_i' \beta^{\text{PSW}} + \beta_0^{\text{PSW}} \text{Treatment}_i + u_i$$

3. Estimate ATE with Malawi data reweighted by inverse of propensity score

$$d_i = \alpha_0^{\text{PSW}} + \alpha_1^{\text{PSW}} \text{Treatment}_i + \text{Stratum}_i + \nu_i^{\text{PSW}}.$$

- $W_i = (\text{age, education, per-capita income, school costs, transfer amount})$
- Key assumption: **cond. on W_i , potential outcomes $\perp\!\!\!\perp$ contexts**

$$\max_{\{d_{i\tau}\}_{\tau=t}^{T-1}} E \left[\sum_{\tau=t}^{T-1} \beta^{\tau-t} \{ \theta \ln(c_{i\tau}) + \varepsilon_{i\tau}(d_{i\tau}) \} + \beta^{T-t} R(e_{i,T}; x_{i,T}) \mid \Omega_{i\tau} \right]$$

s.t. $c_{i\tau} = y_{i\tau} - d_{i\tau} s_{i\tau}$

$e_{i\tau} = e_{i,\tau-1} + d_{i,\tau-1}$

- State variables ▶ How to construct

- e_{it} : Years of education
- y_{it} : Per-capita income
- s_{it} : School costs
- ε_{it} : Preference shocks
- $\Omega = \{e, y, s, \varepsilon\}$

- Parametric assumptions

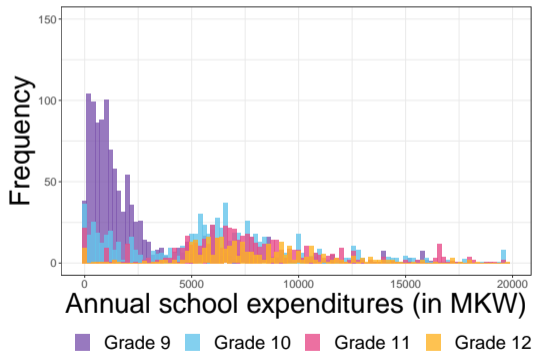
- Discount factor: $\beta = 0.95$
- Preference shocks: $\varepsilon \sim$ Type 1 extreme value, i.i.d across (t, i, d)

Variables construction

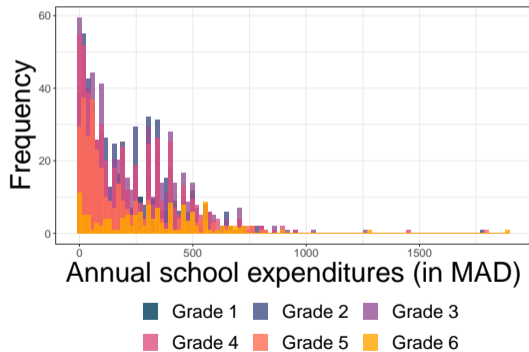
- Directly observe in data: (e_{it}, d_{it}, z_{it})
- Per-capita income: y_{it}
 - Income is unobserved or measured with errors
 - Use annual household expenditures
 - Divide by household size adjusted by OECD equivalence scale
 - If in LCTs, add cash transfer amount
- School costs: s_{it}
 - School costs that parents have to pay upfront
 - Use annual expenditures on school related stuff
 - Take median for schooling children in control group for each grade
 - If in CCTs, subtract cash transfer amount

Distribution of school costs

Malawi: secondary school



Morocco: primary school



Structural estimation: HM inversion

- Rewrite choice prob. at baseline using HM inversion ▶ How to estimate CCP

$$\underbrace{\ln \frac{P(d=1|e_{it}, x_{it})}{P(d=0|e_{it}, x_{it})}}_{\text{Odds of schooling}} = \underbrace{v(e_{it}, x_{it}, 1) - v(e_{it}, x_{it}, 0)}_{\text{Differences in conditional value functions}}$$

- Expand continuation values at baseline (Scott, 2014; Kalouptsi et al., 2021)

$$\begin{aligned} v(e_{it}, x_{it}, d) &= \theta \ln(y_{it} - d \times s_{it}) + \beta E_x \left[\bar{V}(e_{i,t+1}, x_{i,t+1} : \theta) | e_{it}, x_{it}, d \right] \\ &= \underbrace{\theta \ln(y_{it} - d \times s_{it})}_{\text{Flow utility}} + \beta \left(\underbrace{\bar{V}(e_{i,t+1}, x_{i,t+1} : \theta)}_{\text{Realized value function}} + \underbrace{\eta_{it}(d)}_{\text{Expectation errors}} \right) \end{aligned}$$

Structural estimation: finite dependence

- Specify decisions after intervention to have $e_{i,t+2} = e_{i,t} + 1$ for everyone

$$\bar{V}(e_{i,t+1}, x_{i,t+1} : \theta) = \begin{cases} v(e_{it} + 1, x_{i,t+1}, 0) + \gamma - \ln P(d = 0 | e_{it} + 1, x_{i,t+1}) & \text{if } d_{it} = 1 \\ v(e_{it}, x_{i,t+1}, 1) + \gamma - \ln P(d = 1 | e_{it}, x_{i,t+1}) & \text{if } d_{it} = 0 \end{cases}$$

- Eliminate continuation values after intervention

$$v(e_{it} + 1, x_{i,t+1}, 0) = \theta \ln(y_{i,t+1}) + \beta E_x \left[\bar{V}(e_{it} + 1, x_{i,t+2} : \theta) | x_{i,t+1} \right]$$
$$v(e_{it}, x_{i,t+1}, 1) = \theta \ln(y_{i,t+1} - s_{i,t+1}) + \beta E_x \left[\bar{V}(e_{it} + 1, x_{i,t+2} : \theta) | x_{i,t+1} \right].$$

- Substitute back to HM inversion

CCP estimation

- Estimate probability of schooling at each state value
 - Needed to construct dependent variable in 2SLS regression
- Smooth probabilities across states by using a flexible logit
 - Ideally frequency estimates for each state
 - Practically no variation for some states
- Choose MLE or GMM to replicate treatment effects at this stage

▶ Back

Robustness to how to extrapolate across contexts

		Across-contexts	
	Target	HTE	PSW
Treatment	0.0567*** (0.0106)	0.212*** (0.00442)	0.00660 (0.0184)
Control mean	0.894*** (0.00951)	1.127*** (0.00373)	0.895*** (0.0128)
Obs.	4982	4982	1490
= Target TE		0.000	0.007
= Target control mean		0.000	0.927

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

Robustness to how to extrapolate $\Delta R(e; x)$

	Target	Across-contexts		Across-policies	
		Linear	RF	Linear	RF
Treatment	0.0567*** (0.0106)	0.0431*** (0.00465)	0.0412*** (0.00644)	0.0590*** (0.00545)	0.0577*** (0.00542)
Control mean	0.894*** (0.00951)	0.702*** (0.00390)	0.676*** (0.00556)	0.941*** (0.00531)	0.942*** (0.00529)
Obs.	4982	4982	4982	4982	4982
= Target TE		0.004	0.016	0.674	0.863
= Target control mean		0.000	0.000	0.000	0.000

Note: *** p<0.01 ** p<0.05 * p<0.1

Comparison of extrapolation methods

	Target	Across-contexts			
		HTE		PSW	
Treatment	0.0567*** (0.0106)	0.212*** (0.00442)	0.0308*** (0.00421)	0.00660 (0.0184)	-0.0459** (0.0202)
Control mean	0.894*** (0.00951)	1.127*** (0.00373)	1.111*** (0.00367)	0.895*** (0.0128)	1.000*** (0.00221)
Obs.	4982	4982	4982	1490	1490
= Target TE		0.000	0.000	0.007	0.000
= Target control mean		0.000	0.000	0.927	0.000
Normalization of s, y, z			✓		✓

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

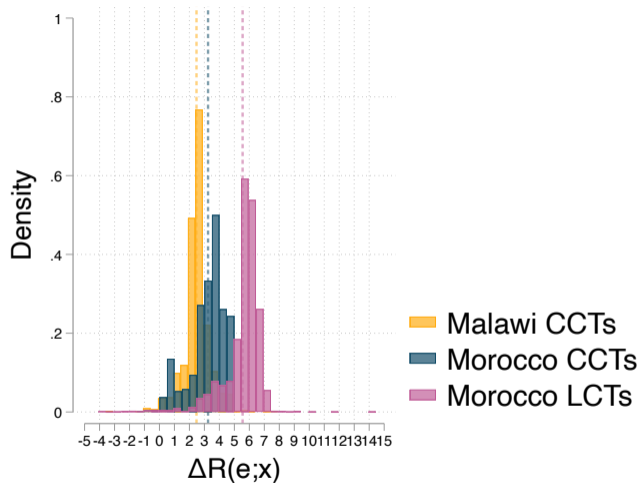
- Structural: school costs & cash transfers **relative to per-capita income**
- [Across-contexts](#) using relative values in reduced-form not improved

Estimates of elasticity of schooling

	Malawi	Morocco	
	CCTs	CCTs	LCTs
$E \left[\frac{\partial P_{i,2}^1}{\partial z_{i,2}} \frac{z_{i,2}}{P_{i,2}^1} \right]$	0.185	0.332	0.142

- $E \left[\frac{\partial P_{i,2}^1}{\partial z_{i,2}} \frac{z_{i,2}}{P_{i,2}^1} \right]$: average elasticity of schooling w.r.t cash transfers
- Across-contexts: difference in effective size of cash transfer
- Across-policies: substitution effects

Estimates of $\Delta R_i(e; x)$



- Dashed lines indicate $E[\Delta R(e; x)]$ under each experiment

Model fit

	Malawi	Morocco	
	CCTs	CCTs	LCTs
Treatment	0.0317*** (0.00495)	0.0554*** (0.00777)	0.0539*** (0.00954)
Control mean	0.895*** (0.00241)	0.894*** (0.00747)	0.900*** (0.00889)
Obs.	1490	4982	3018
= Target TE	0.290	0.869	0.051
= Target control mean	0.721	0.981	0.476

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

Extrapolation from Malawi CCTs with true θ or $\Delta R(e; x)$

	Target	Across-contexts		
Treatment	0.0567*** (0.0106)	0.0431*** (0.00465)	0.0953*** (0.00486)	0.0367*** (0.00721)
Control mean	0.894*** (0.00951)	0.702*** (0.00390)	0.688*** (0.00411)	0.901*** (0.00689)
Obs.	4982	4982	4982	4982
Replace θ			✓	
Replace $\Delta R(e; x)$				✓
= Target TE		0.004	0.000	0.006
= Target control mean		0.000	0.000	0.276

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

Within-intervention variation of $\Delta R(e; x)$

	$E[\theta \ln(y - s/y)]$		$E[\beta \Delta R(e; x)]$	
	Control	Treatment	Control	Treatment
Malawi CCTs	-0.292	0.594***	2.526	2.373*
Morocco CCTs	-0.117	0.409***	3.045	3.085
Morocco LCTs	-1.706	-1.390***	5.109	5.383***

*** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$ for difference across groups in each intervention.

- Within-intervention variation affects prediction of treatment effect
- Malawi CCTs: $\Delta R(e; x)$ **smaller** for treatment group
 - Children with lower perceived returns to choose schooling
- Moroccan CCTs: $\Delta R(e; x)$ **larger** for treatment group (if anything)
 - Same pattern for Moroccan LCTs

Reduced-form extrapolation with normalization

		Across-contexts		
	Target	Structural	HTE	PSW
Treatment	0.0567*** (0.0106)	0.0150*** (0.000788)	0.0352*** (0.00346)	0.0655*** (0.0140)
Control mean	0.894*** (0.00951)	0.903*** (0.000674)	0.894*** (0.00302)	0.920*** (0.0112)
Obs.	4982	4982	4982	1490
= Target TE		0.000	0.000	0.534
= Target control mean		0.000	0.833	0.022

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- HTE & PSW: $s/y, z/y$ & standardized e and age

Confusion about conditionality of Moroccan CCTs

- Moroccan CCTs sample largely misunderstood conditionality
 - 11% understood conditionality correctly
 - 14% thought CCTs were tied to school enrollment
 - More similar to Moroccan LCTs than Malawi CCTs
- If perfect understanding, [across-contexts extrapolation](#) more accurate?
- Compute counterfactual effect of Moroccan CCTs with no confusion
 - Estimate model under Moroccan CCTs with degree of confusion
 - Simulate model by assuming perfect knowledge

	Estimation		Across-contexts	Across-policies
	Original	Counterfactual	Linear	Linear
Treatment	0.0567*** (0.0106)	0.122*** (0.00836)	0.0431*** (0.00465)	0.0590*** (0.00545)
Control mean	0.894*** (0.00951)	0.868*** (0.00814)	0.702*** (0.00390)	0.941*** (0.00531)
Obs.	4982	4982	4982	4982
= Target TE			0.000	0.000
= Target control mean			0.000	0.000

Note: *** $p < 0.01$ ** $p < 0.05$ * $p < 0.1$

- Treatment effect becomes bigger under perfect knowledge
- Both extrapolations are statistically different from estimate