



# Age-of-Information: Definition, Analysis, and Applications

Igor Kadota

IEOR6706 Queueing Networks, November 10, 2020

# Outline

## 1. Introduction:

- Age-of-Information and Applications

## 2. Theoretical Results: scheduling policies with performance guarantees

- Using Renewal Theory, Stochastic Dominance, RMAB framework, and others.

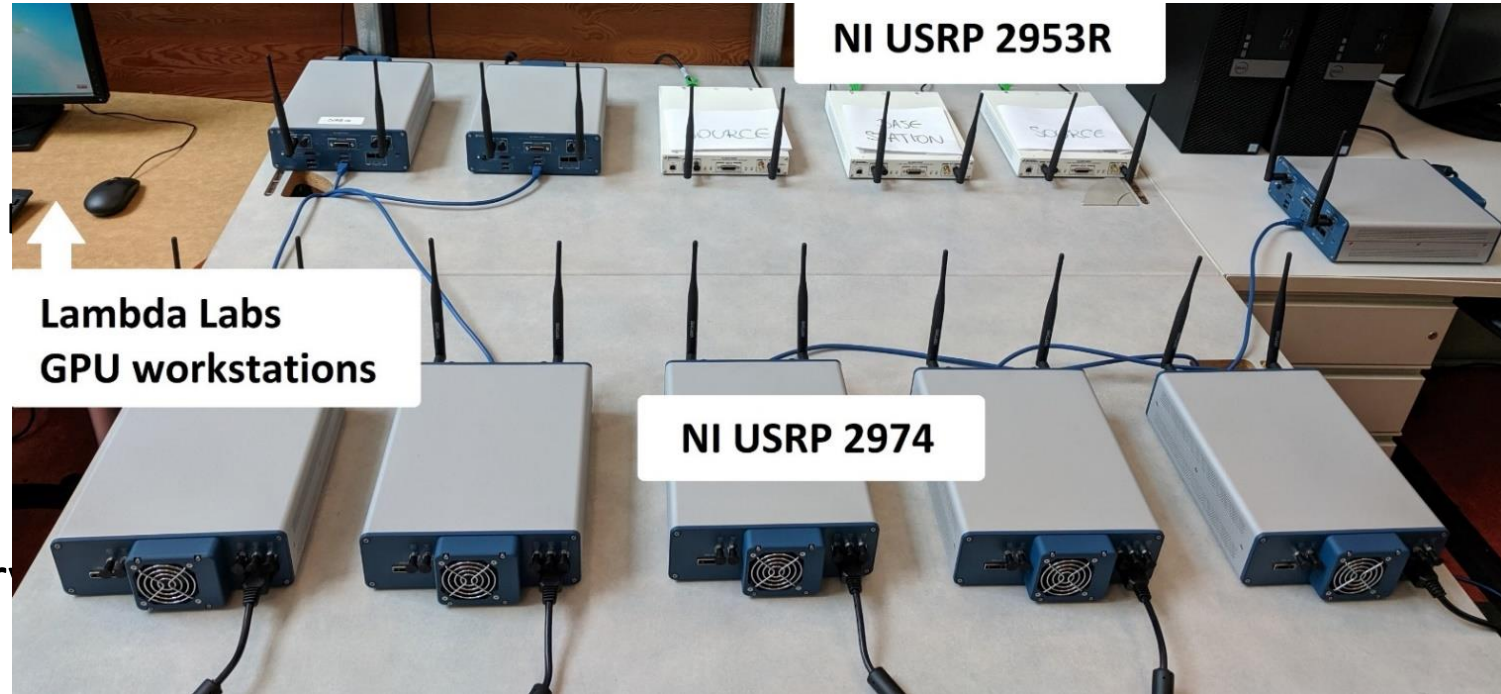
## 3. System Deployment: validation in real operating scenarios

- Using Software Defined Radios

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## 1. Introduction:

- Age-of-Information and



## 2. Theoretical Results:

- Using Renewal Theorem

## 3. System Deployment: validation in real operating scenarios

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- Age-of-Information and Applications

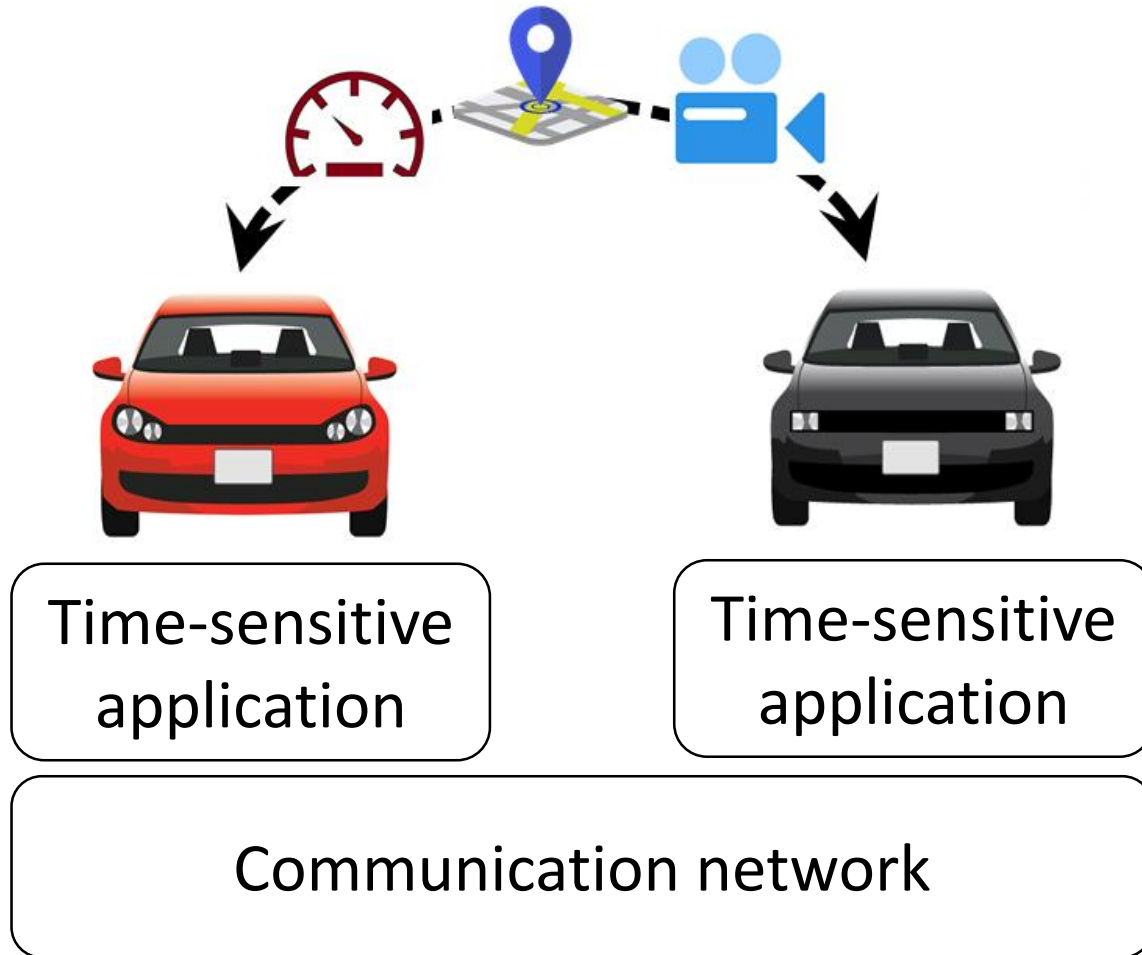
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# Sharing time-sensitive information



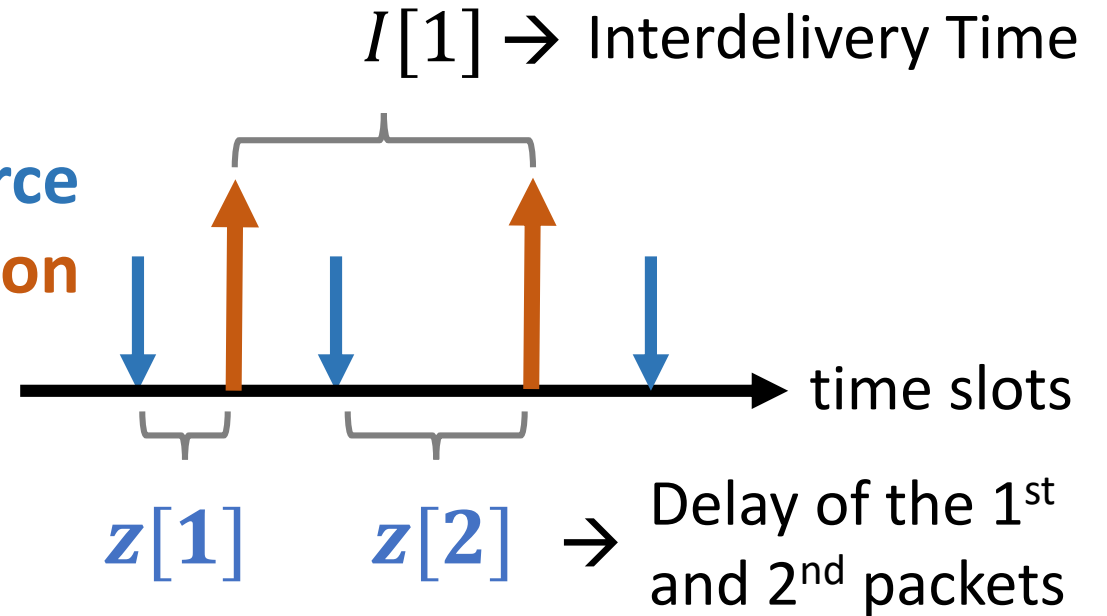
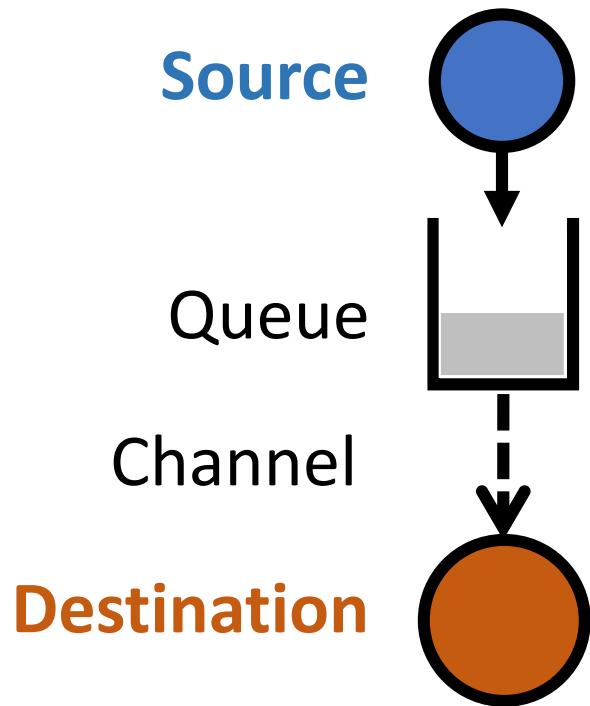
## Emerging applications:

- Autonomous vehicles (ITS)
- Swarm of drones
- Smart factory (Industry 4.0)
- Large-scale Monitoring System
- Shared Augmented Reality
- Immersive Gaming
- Distributed Computation (SGD)

⋮

# Age-of-Information (Aol)

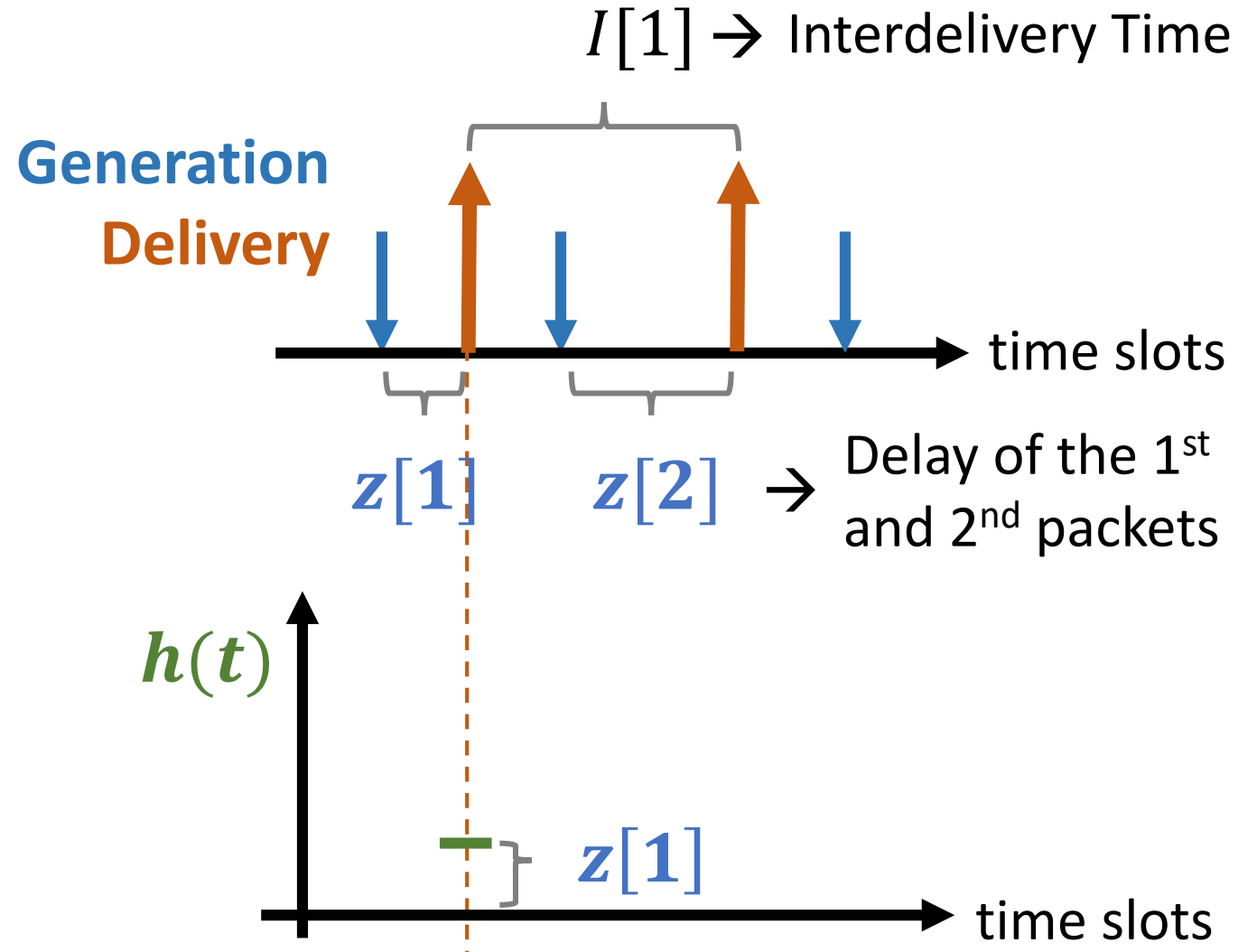
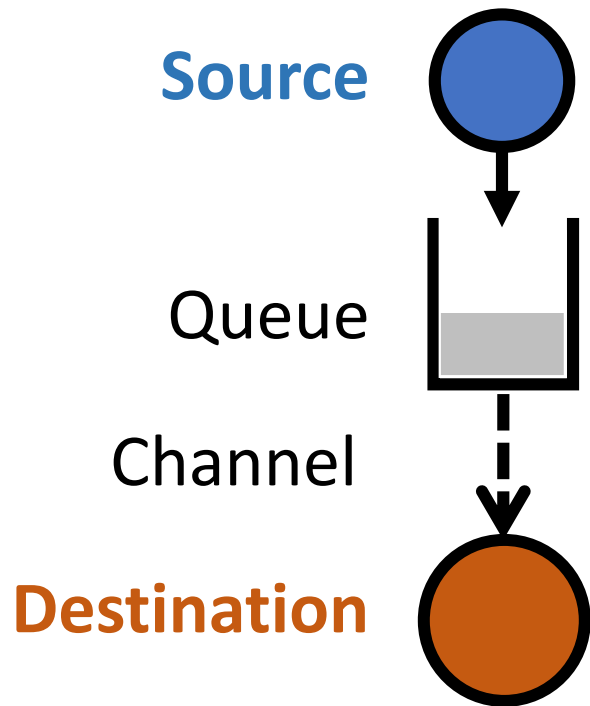
Packet generation at the source  
Delivery of packets to the destination



How **old** is the information  
at the **destination**?

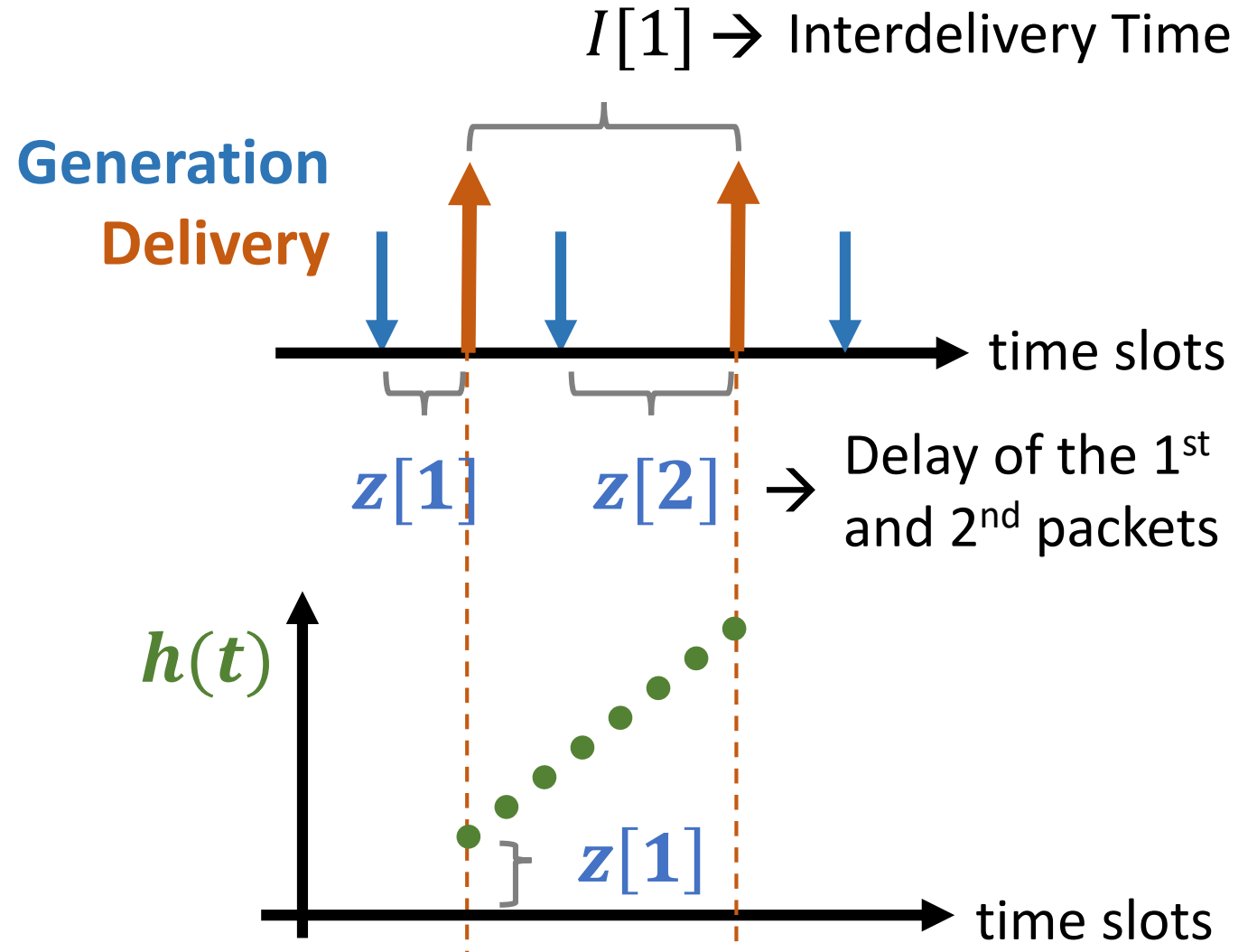
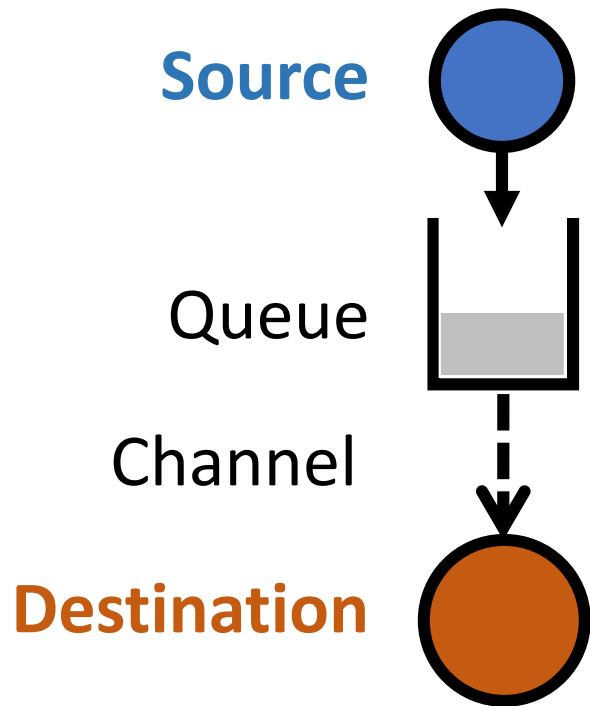
# Age-of-Information (AoI)

**AoI:** time elapsed since the generation of the freshest received packet



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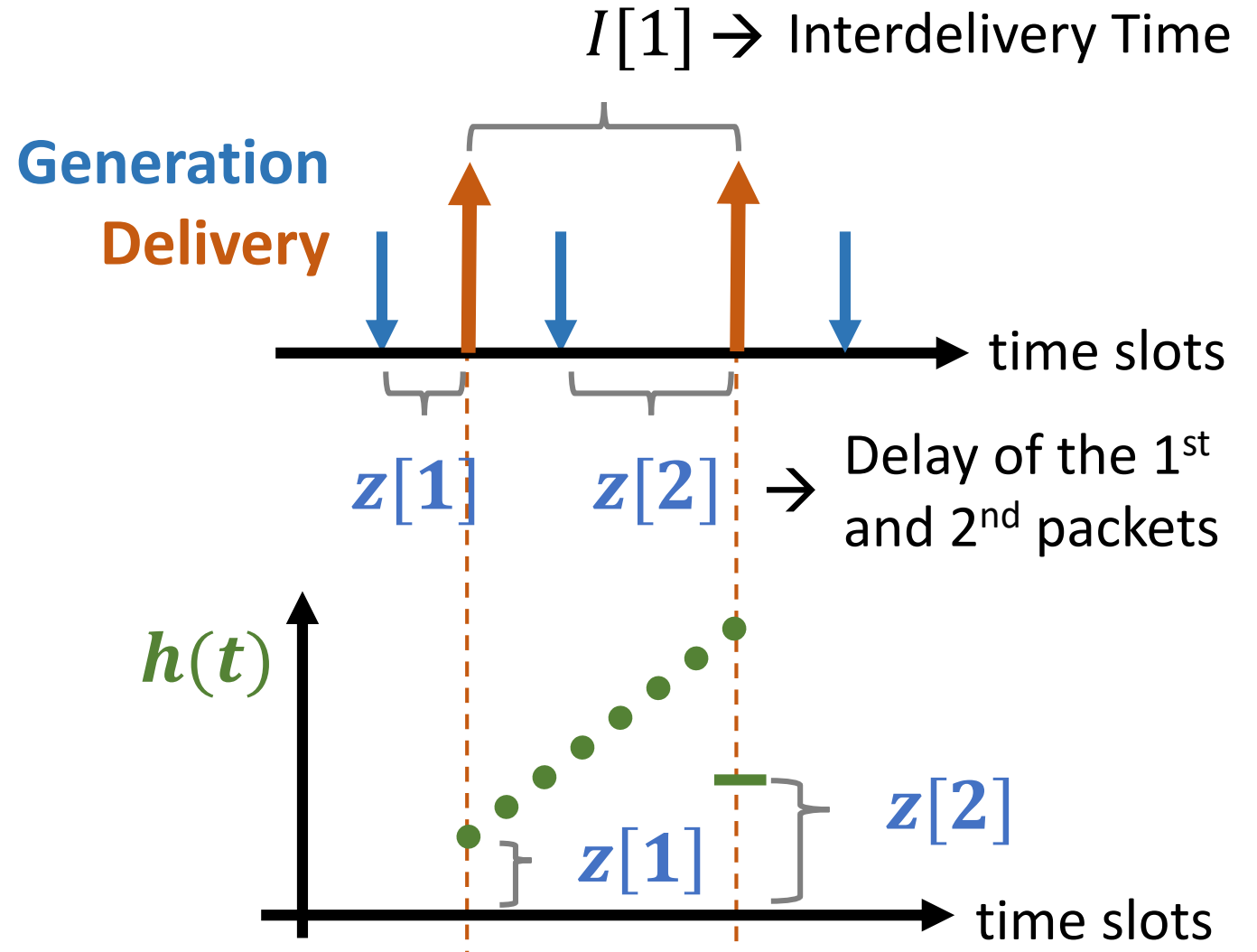
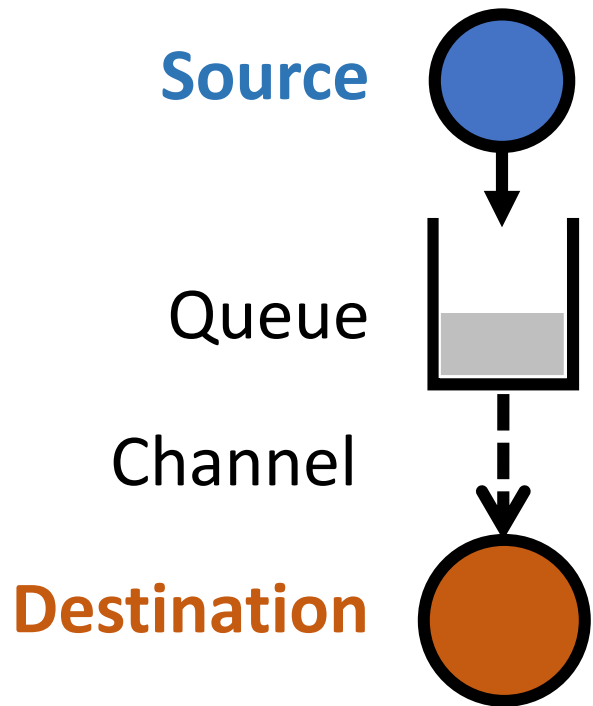
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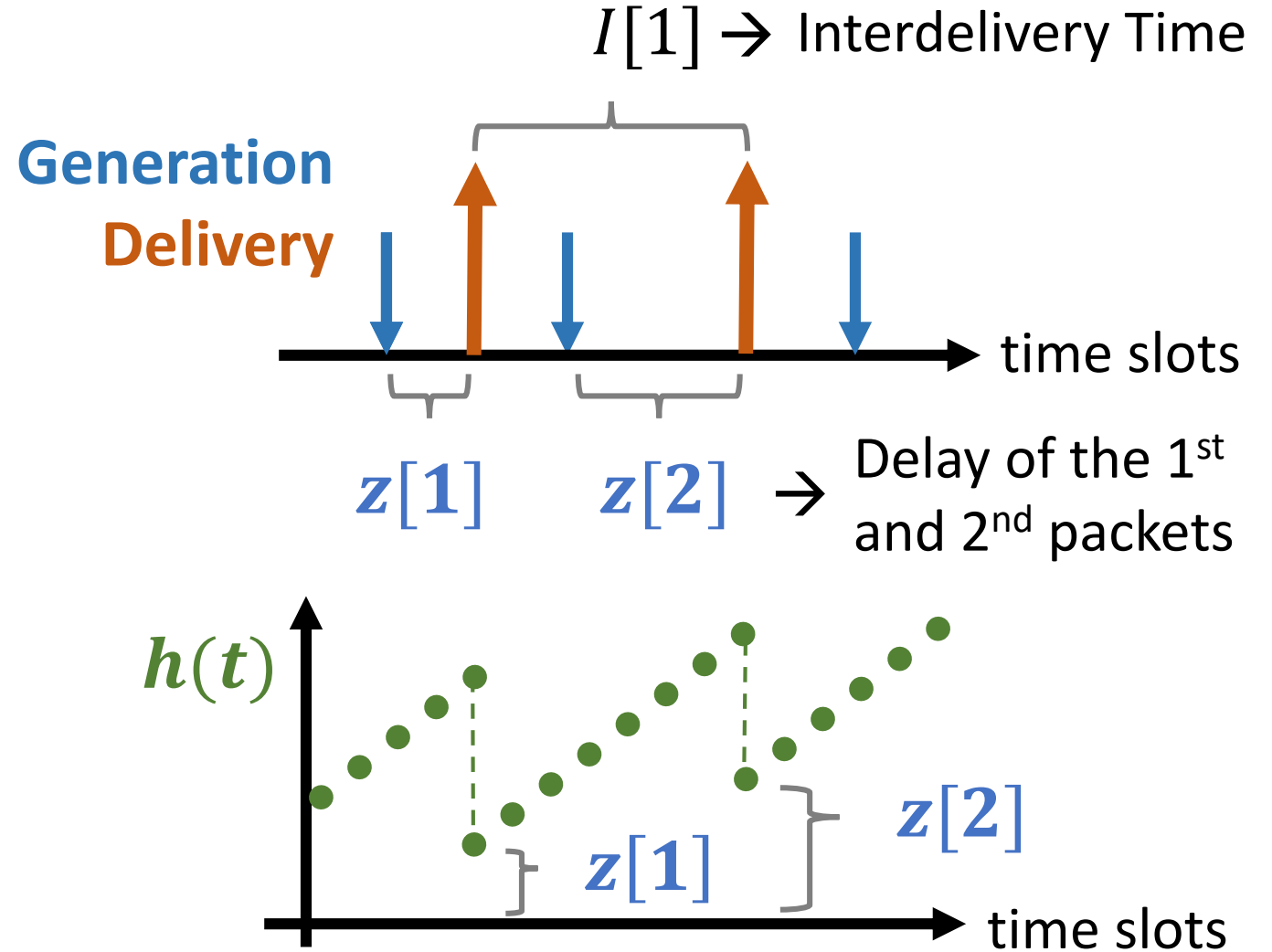
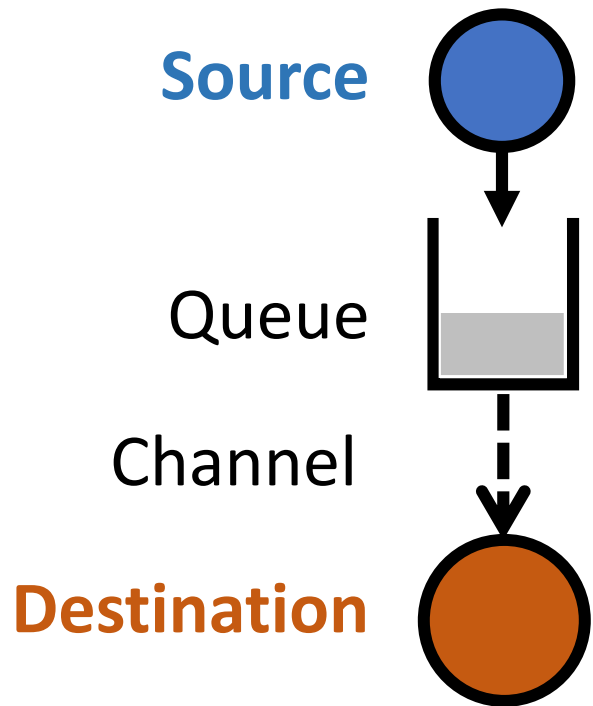
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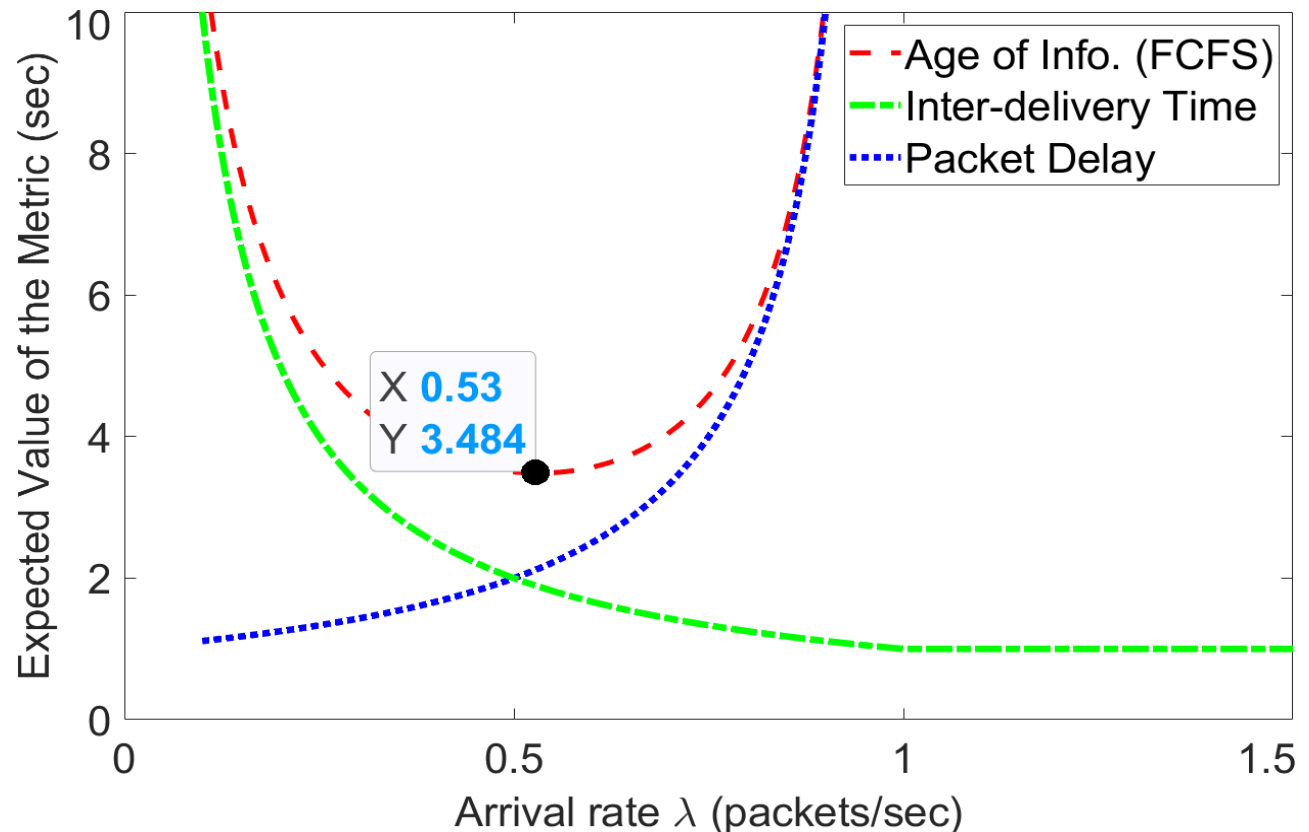
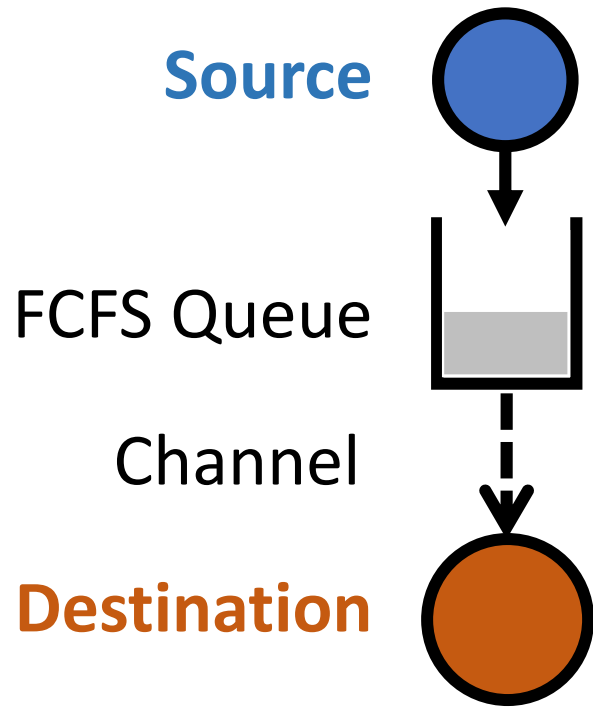
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# Aol, Delay, and Interdelivery time

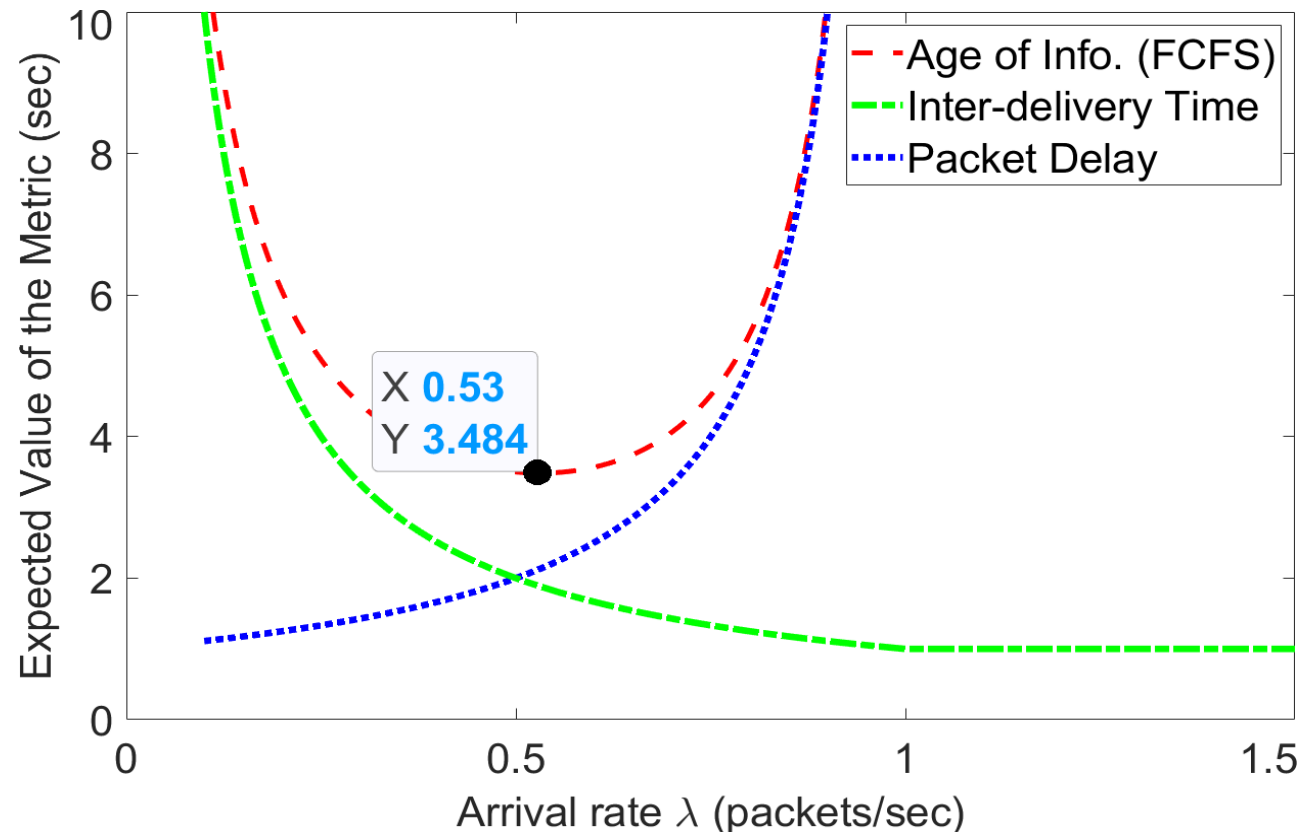
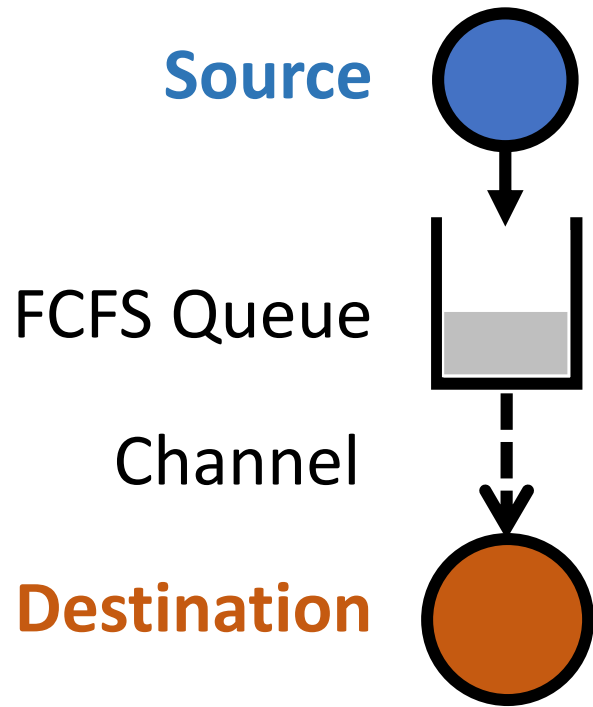
Example: M/M/1 queue using FCFS discipline

Controllable arrival rate  $\lambda$  and fixed service rate  $\mu = 1$  packet per second.



# Aol, Delay, and Interdelivery time

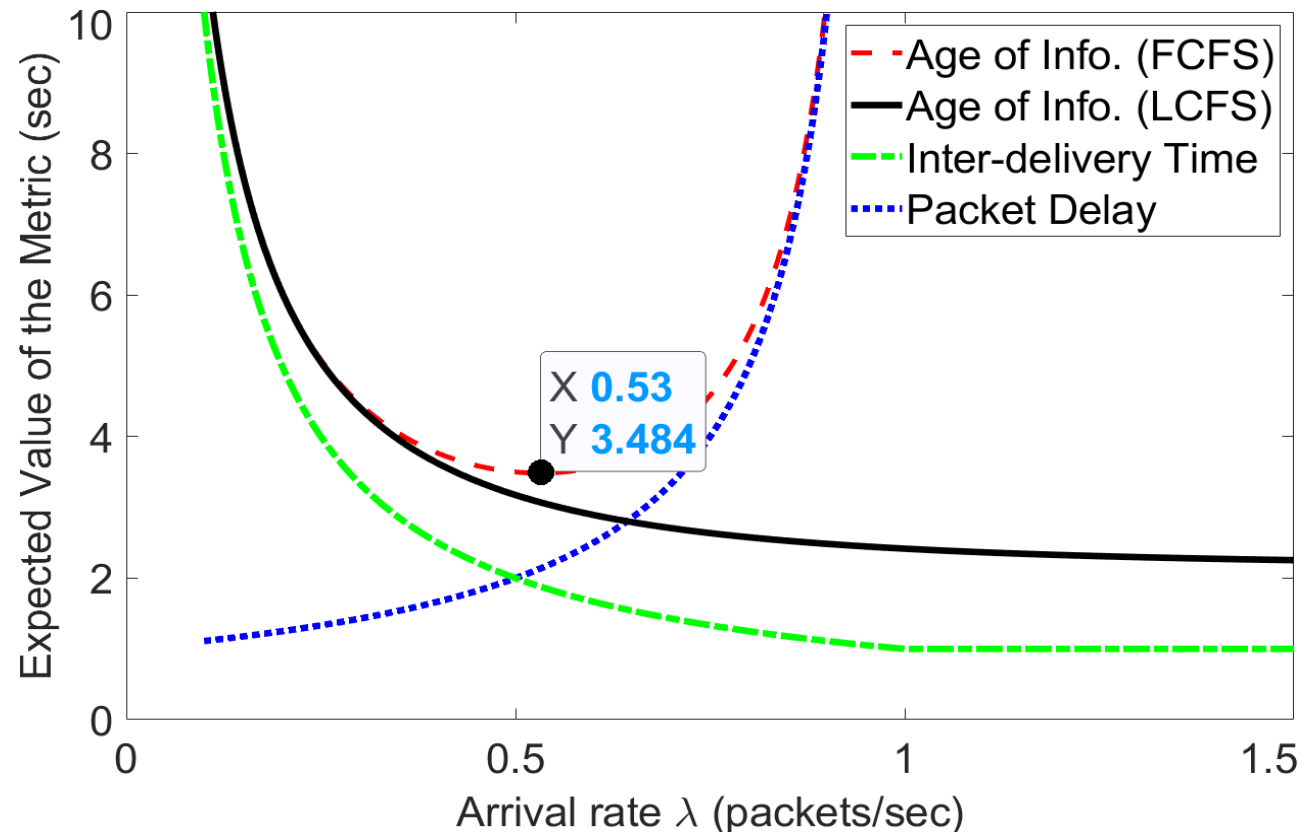
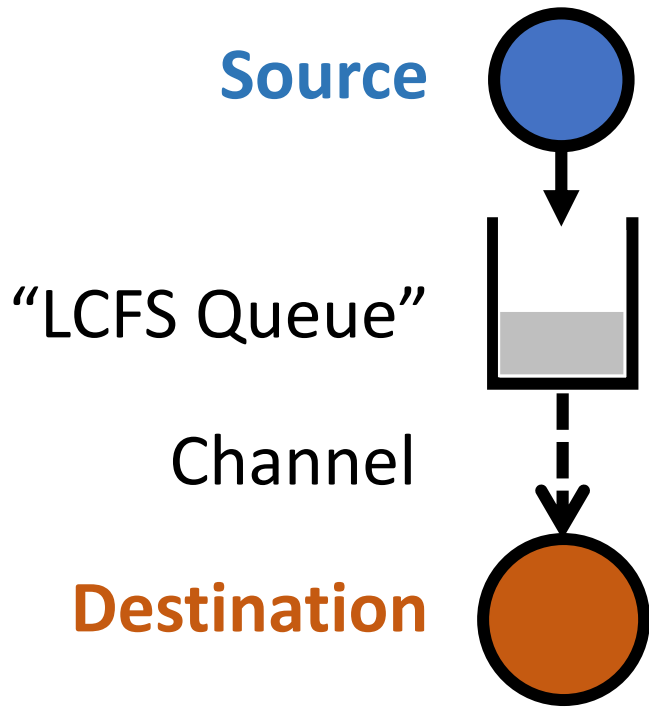
$$\lim_{T \rightarrow \infty} \frac{1}{T} \int_{t=0}^T h(t) dt = \mathbb{E}[h(t)] = \frac{1}{\lambda} + \frac{1}{\mu} + \frac{\lambda^2}{\mu - \lambda}$$



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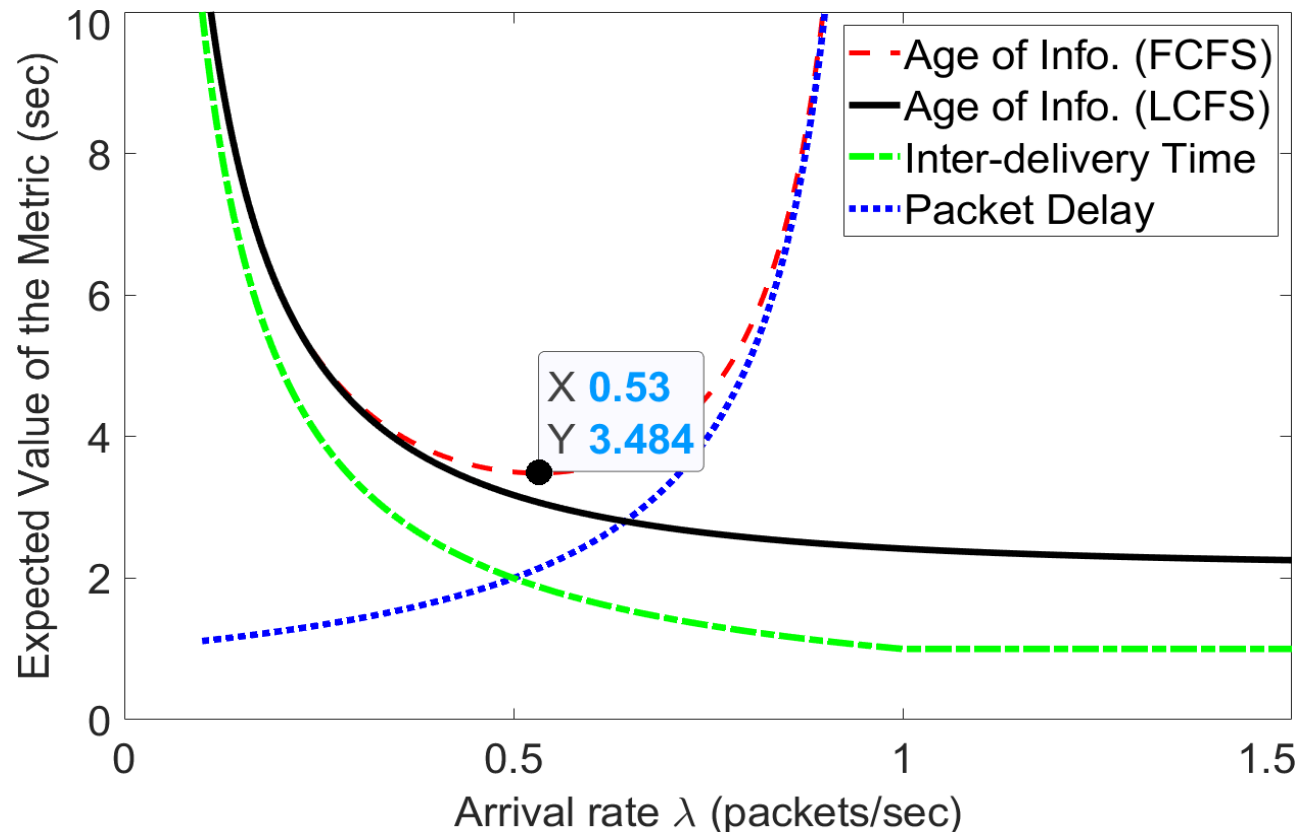
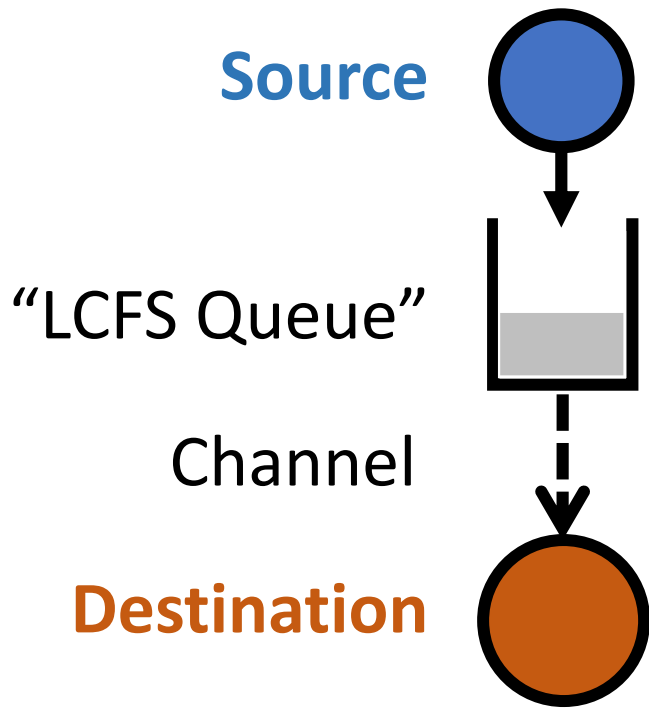
Example: M/M/1/2\* queue

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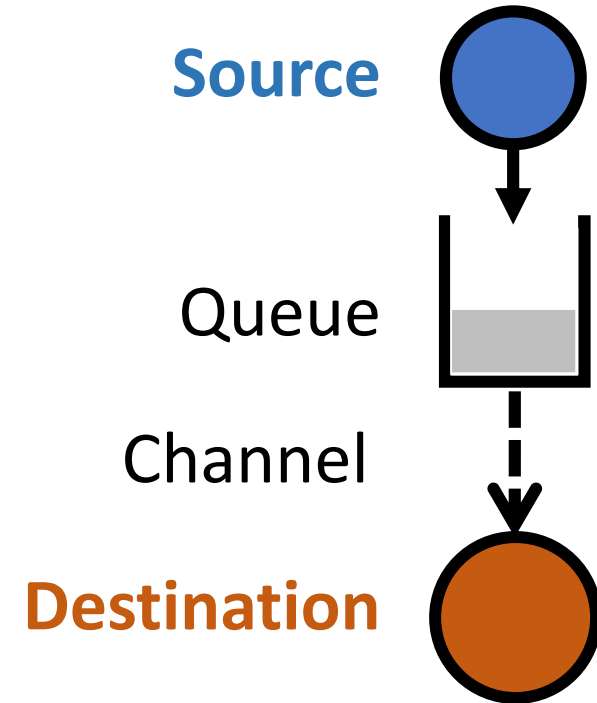
$$\lim_{T \rightarrow \infty} \frac{1}{T} \int_{t=0}^T h(t) dt = \mathbb{E}[h(t)] = \frac{1}{\lambda} + \frac{2}{\mu} + \frac{\lambda}{(\lambda + \mu)^2} + \frac{1}{\lambda + \mu} - \frac{2(\lambda + \mu)}{\lambda + \lambda\mu + \mu^2}$$



# Age-of-Information (Aol)

## Interesting problems in single queue systems:

- When to transmit data when sources harvest energy?
- Which is the best queueing discipline?  
Preemption? No preemption?
- Should we retransmit packets? Should we encode packets?



# Age-of-Information (Aol)

## **Other broad classes of interesting problems:**

- Wireless Communication Networks
- Caching Systems
- Networked Control Systems
- UAV-assisted Status Updates
  
- Systems Research... only a handful of papers...
- Operations Research... nothing in the literature yet...



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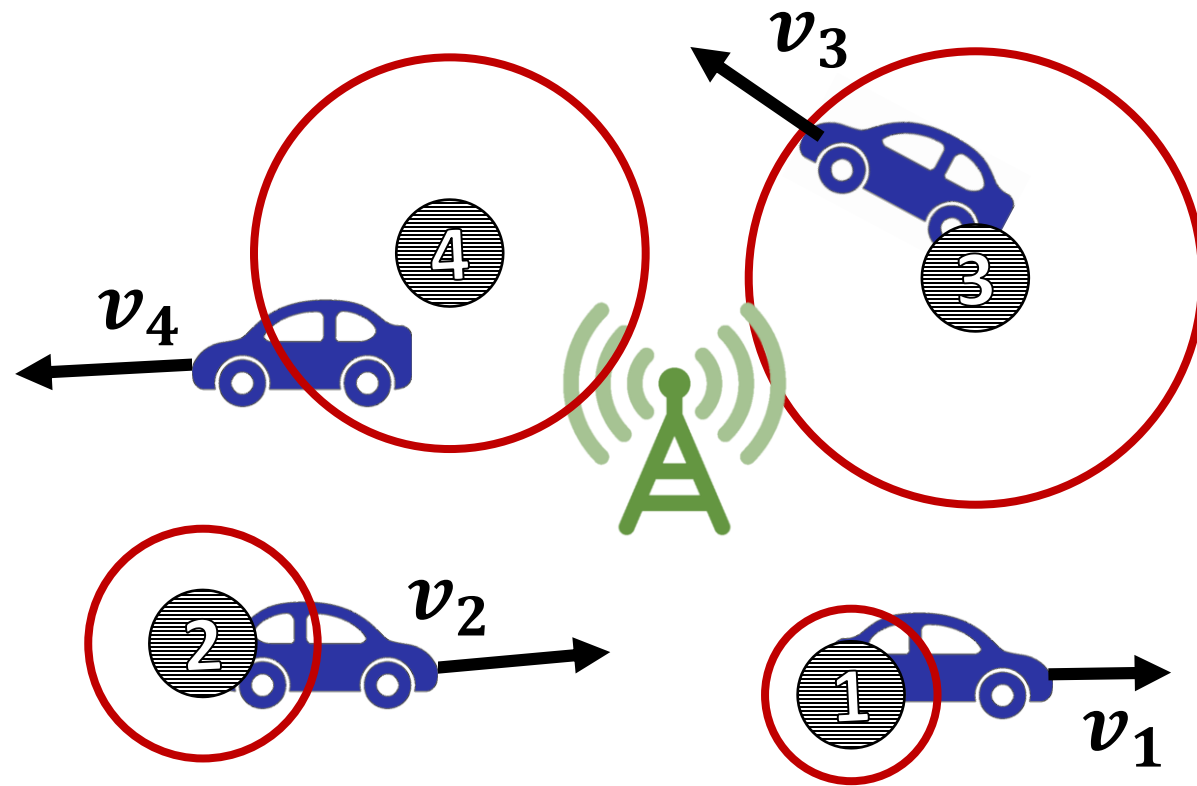
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# Monitoring system



## Legend



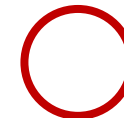
wireless base station



current position of nodes  
(cars, drones, robots, ...)

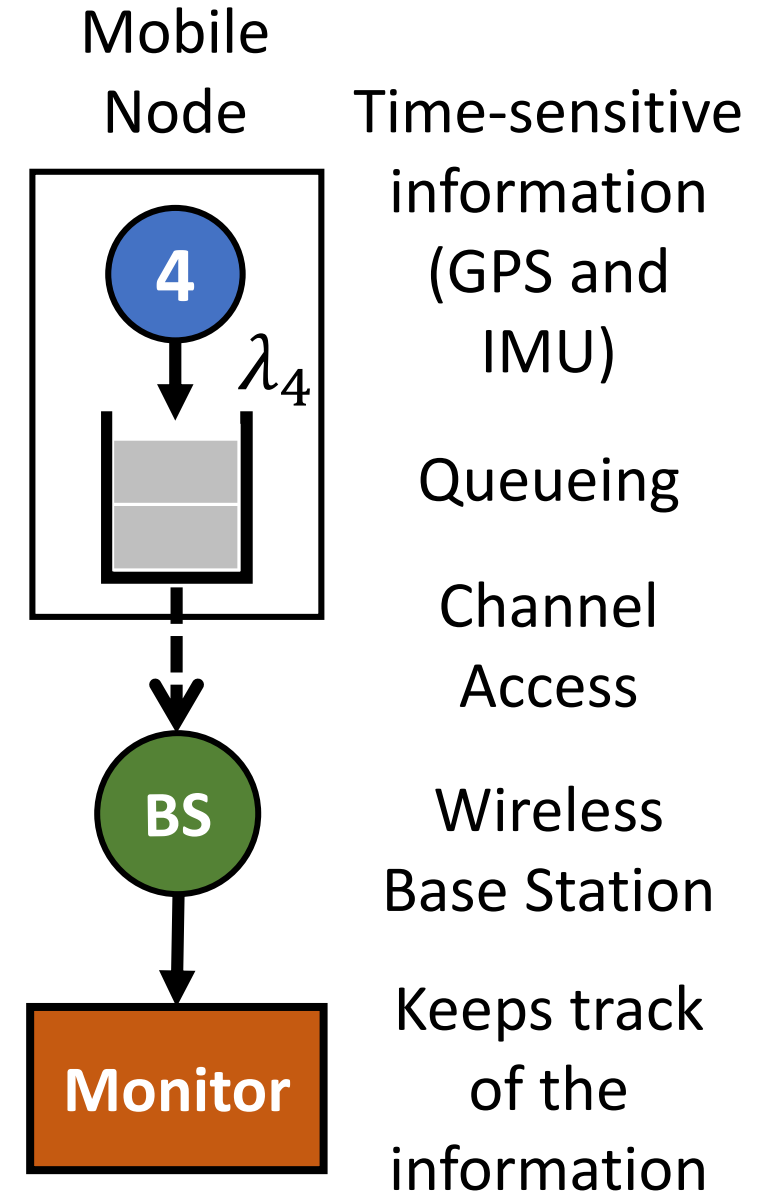
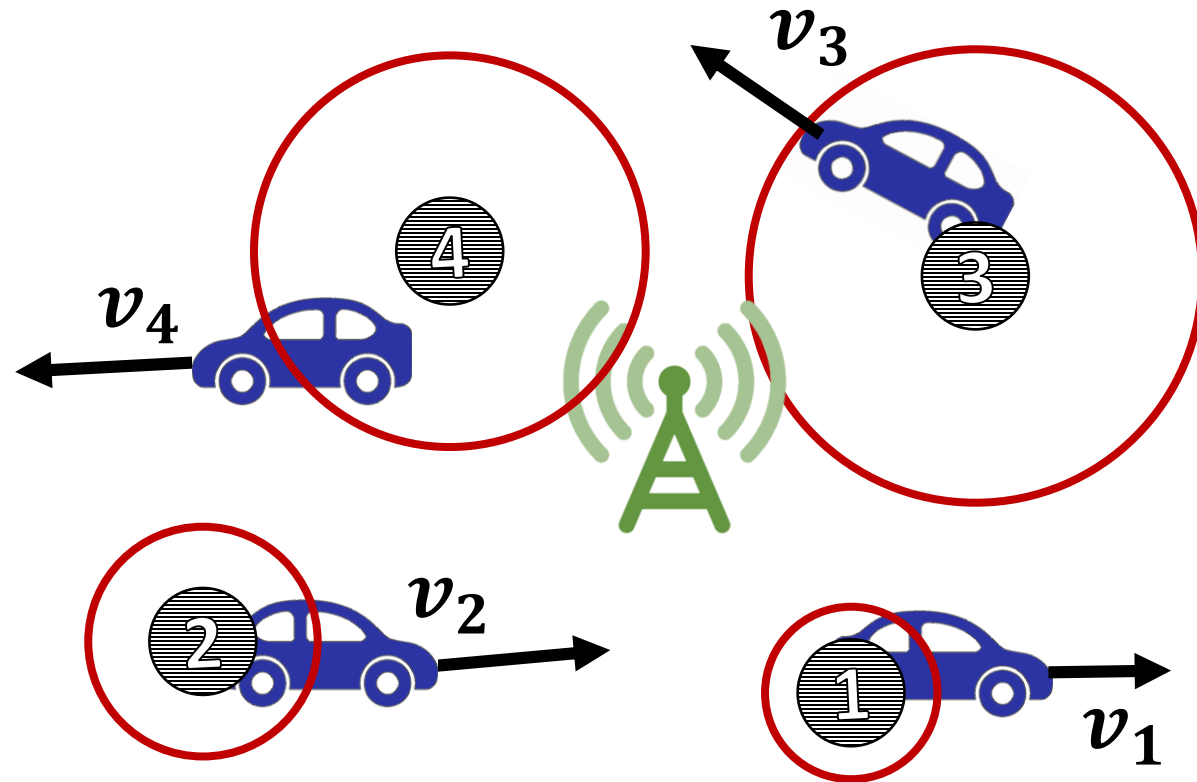


last known position  
(from last packet received)

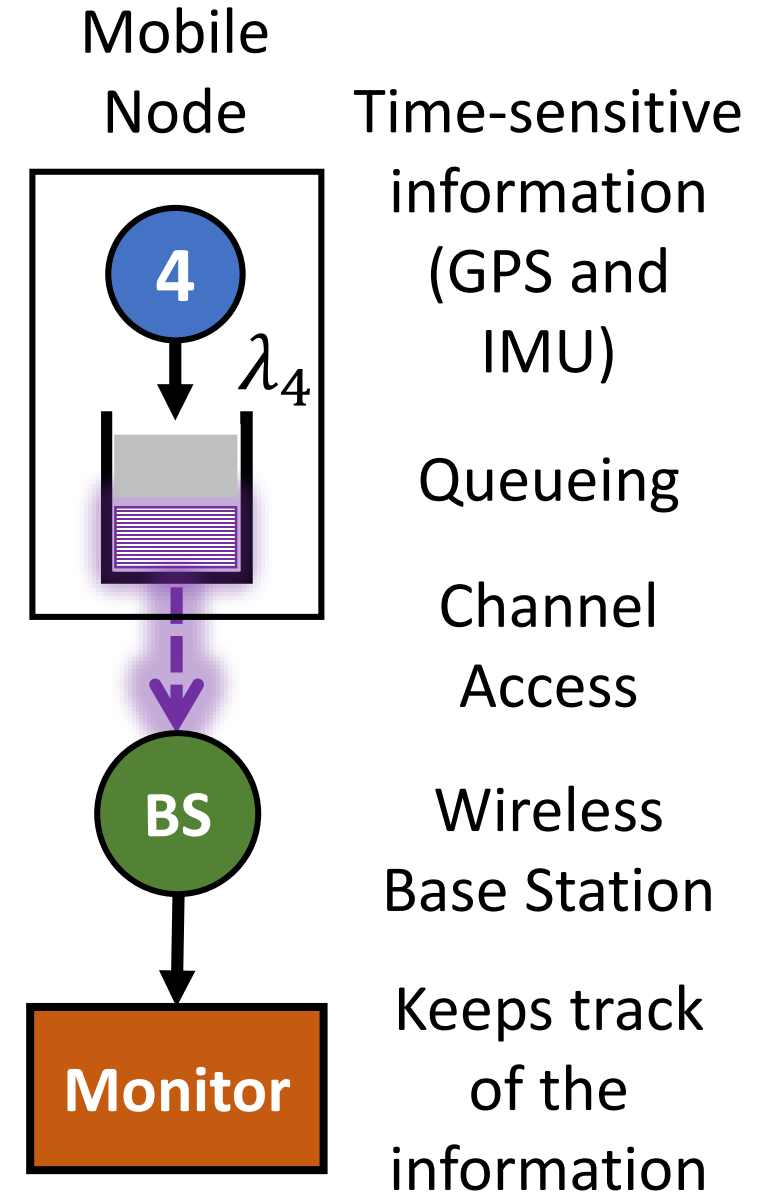
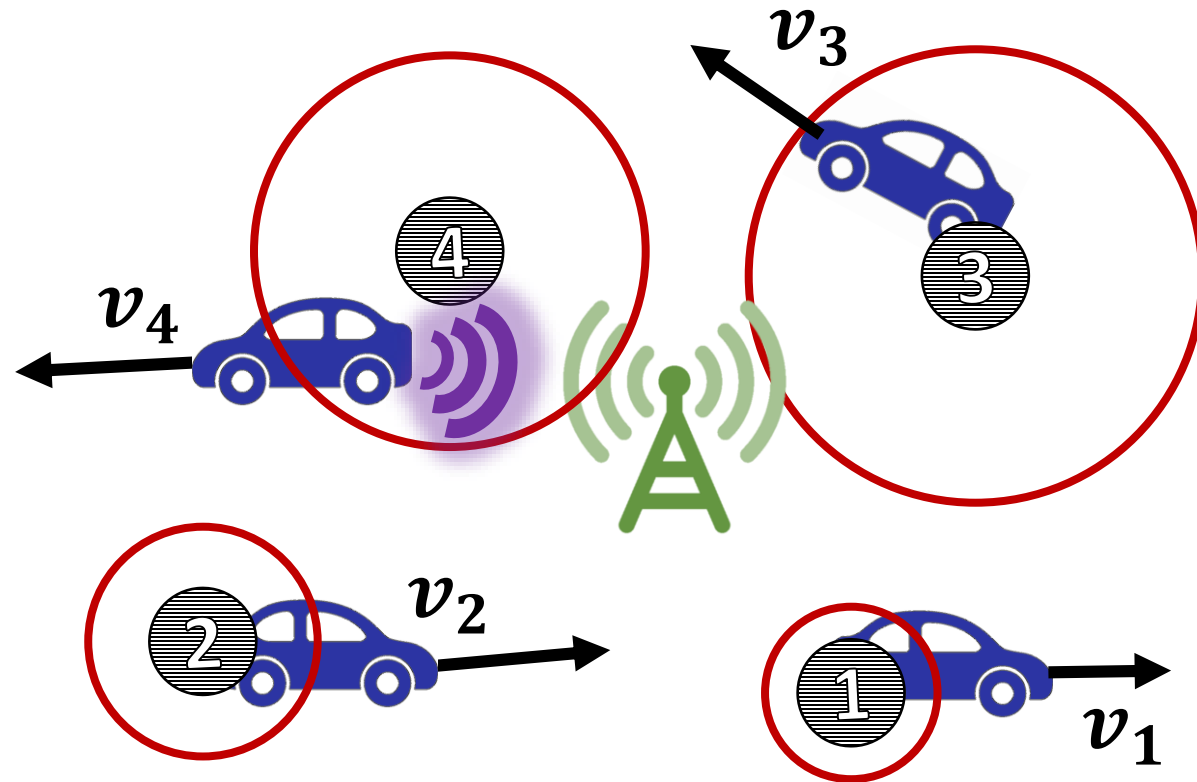


position uncertainty

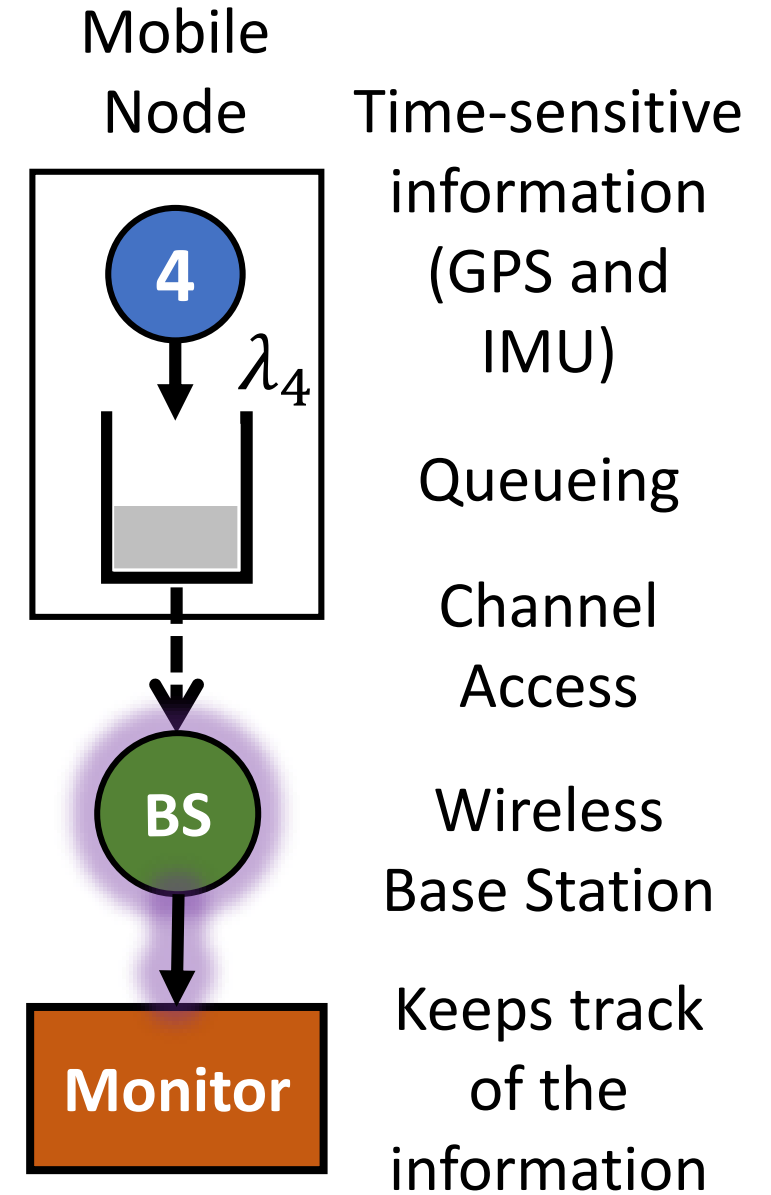
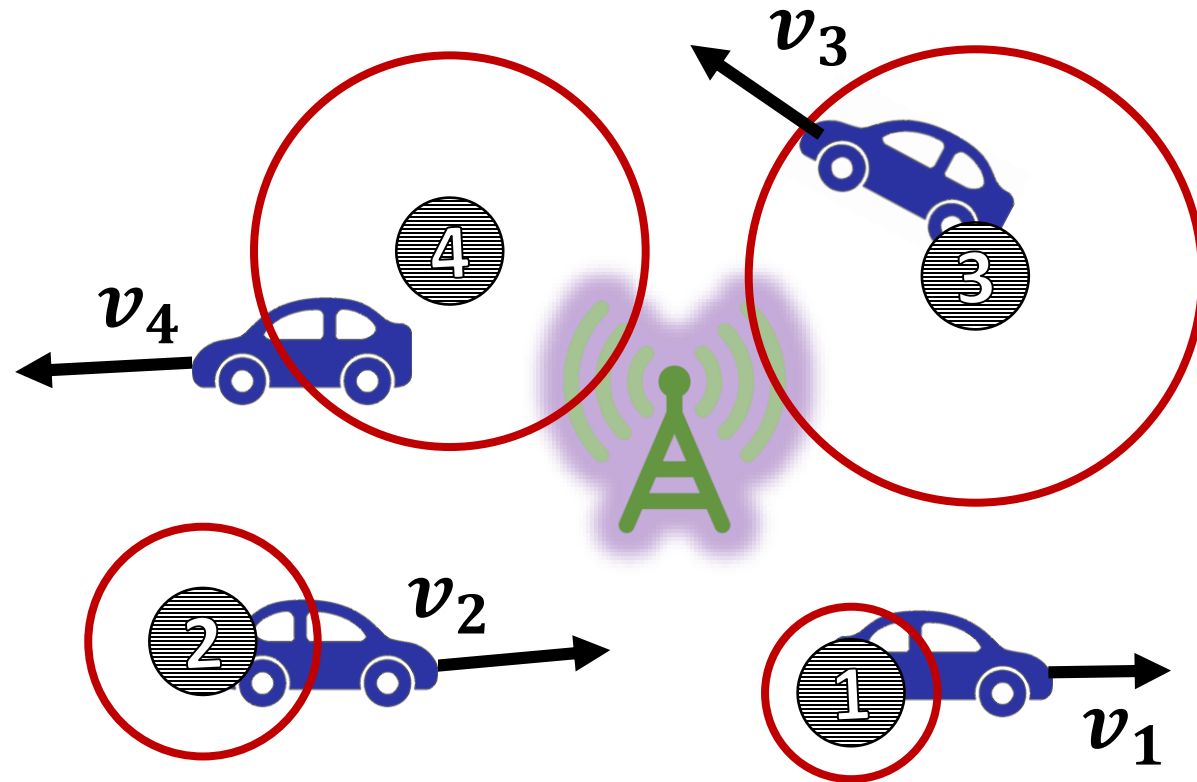
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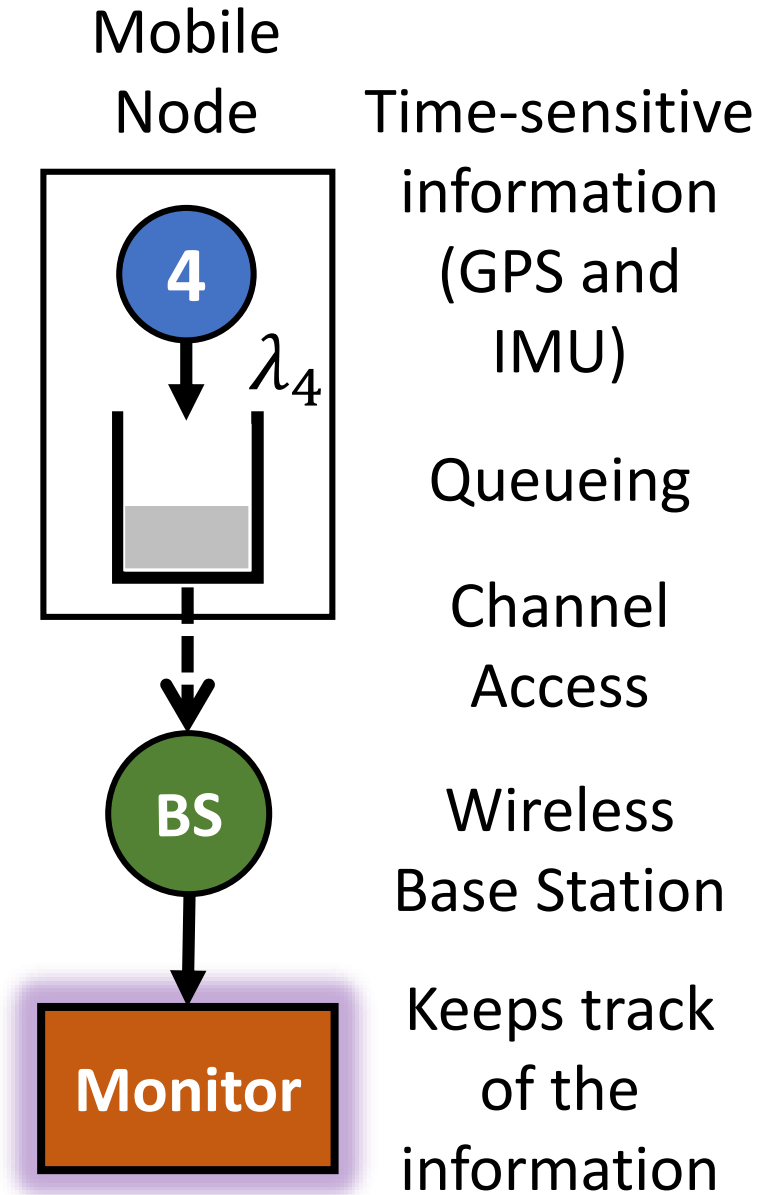
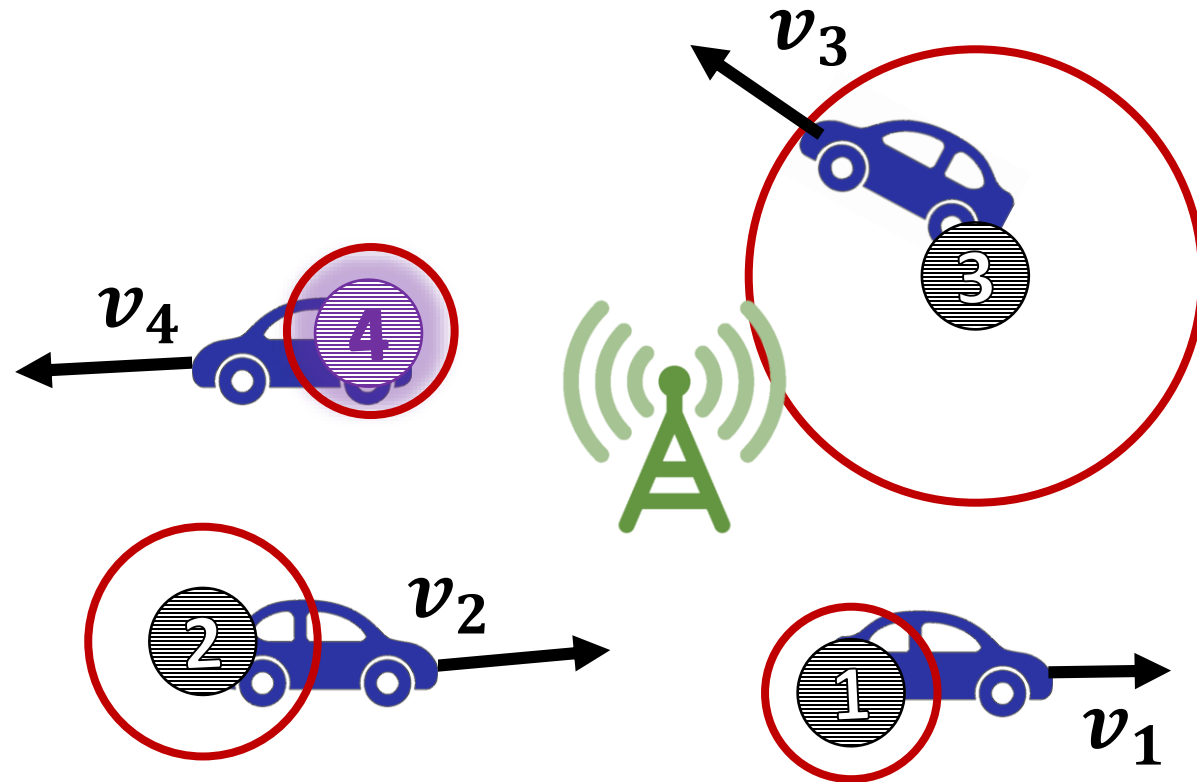
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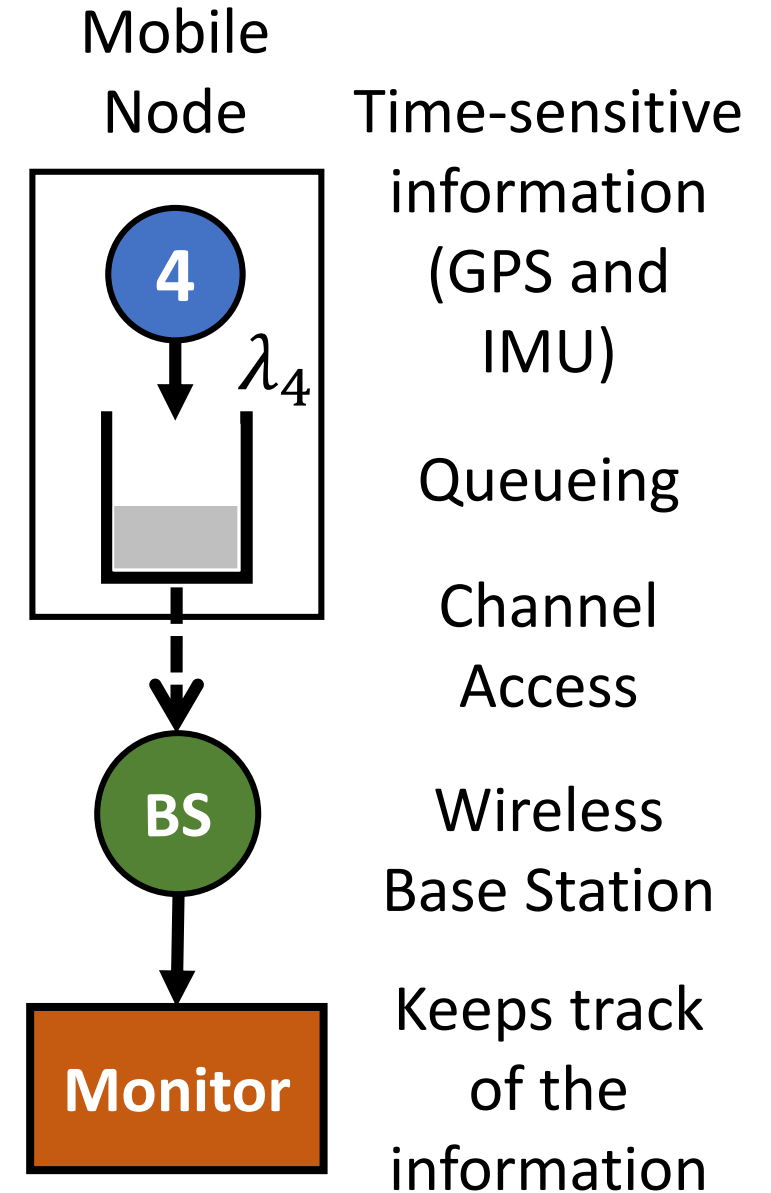
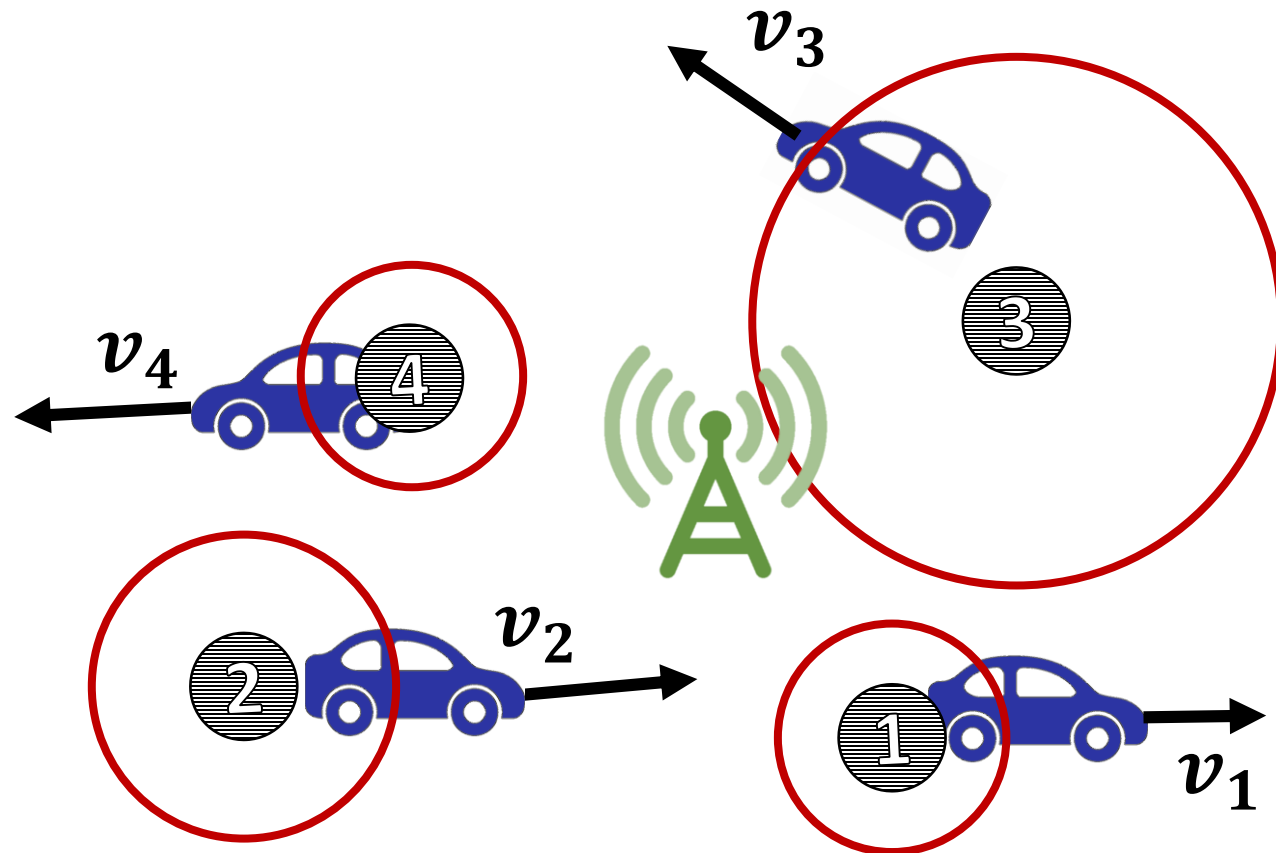
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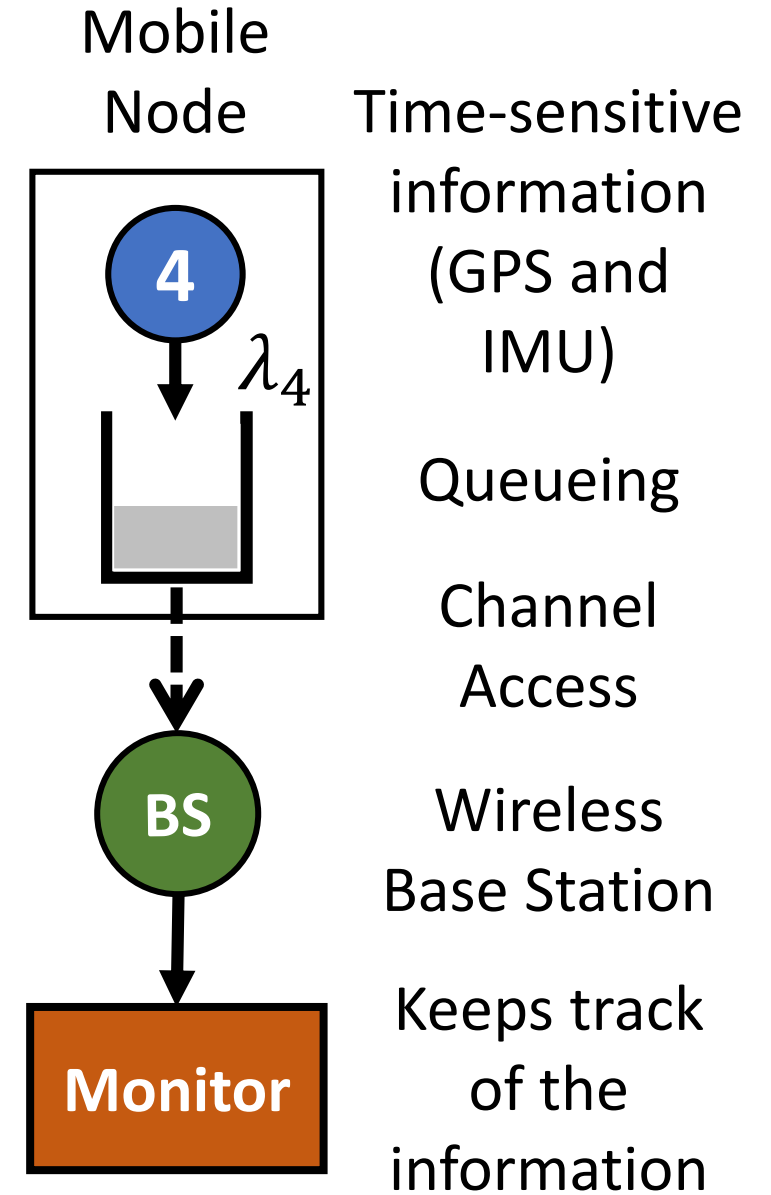
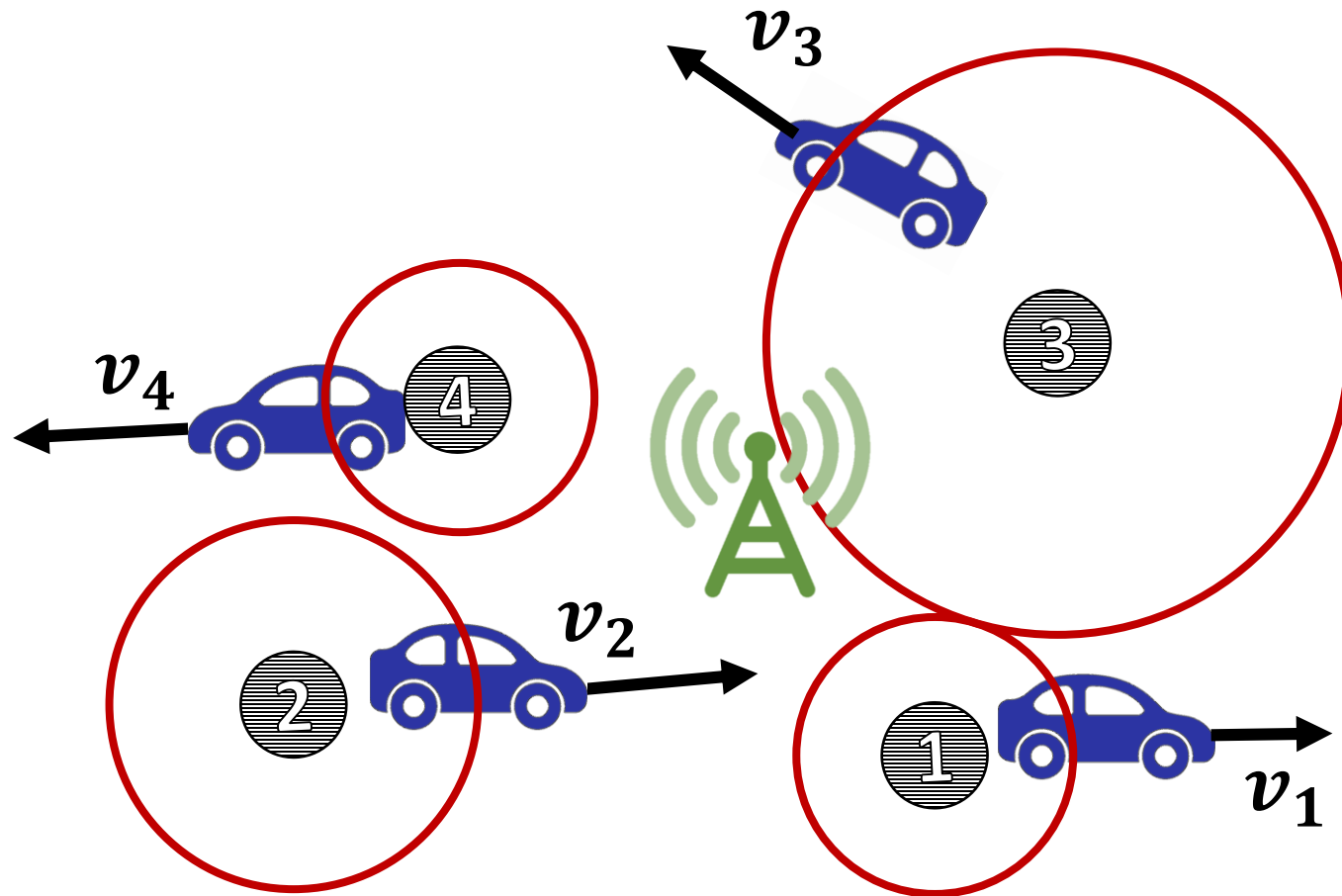
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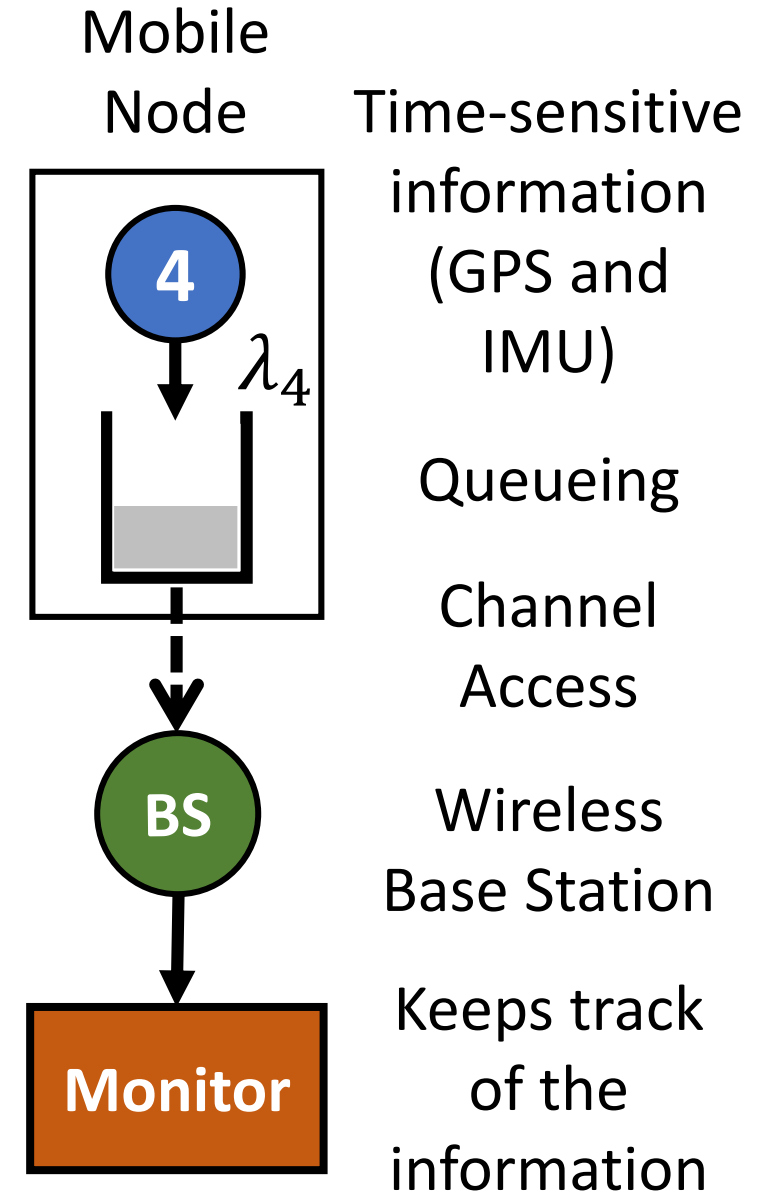
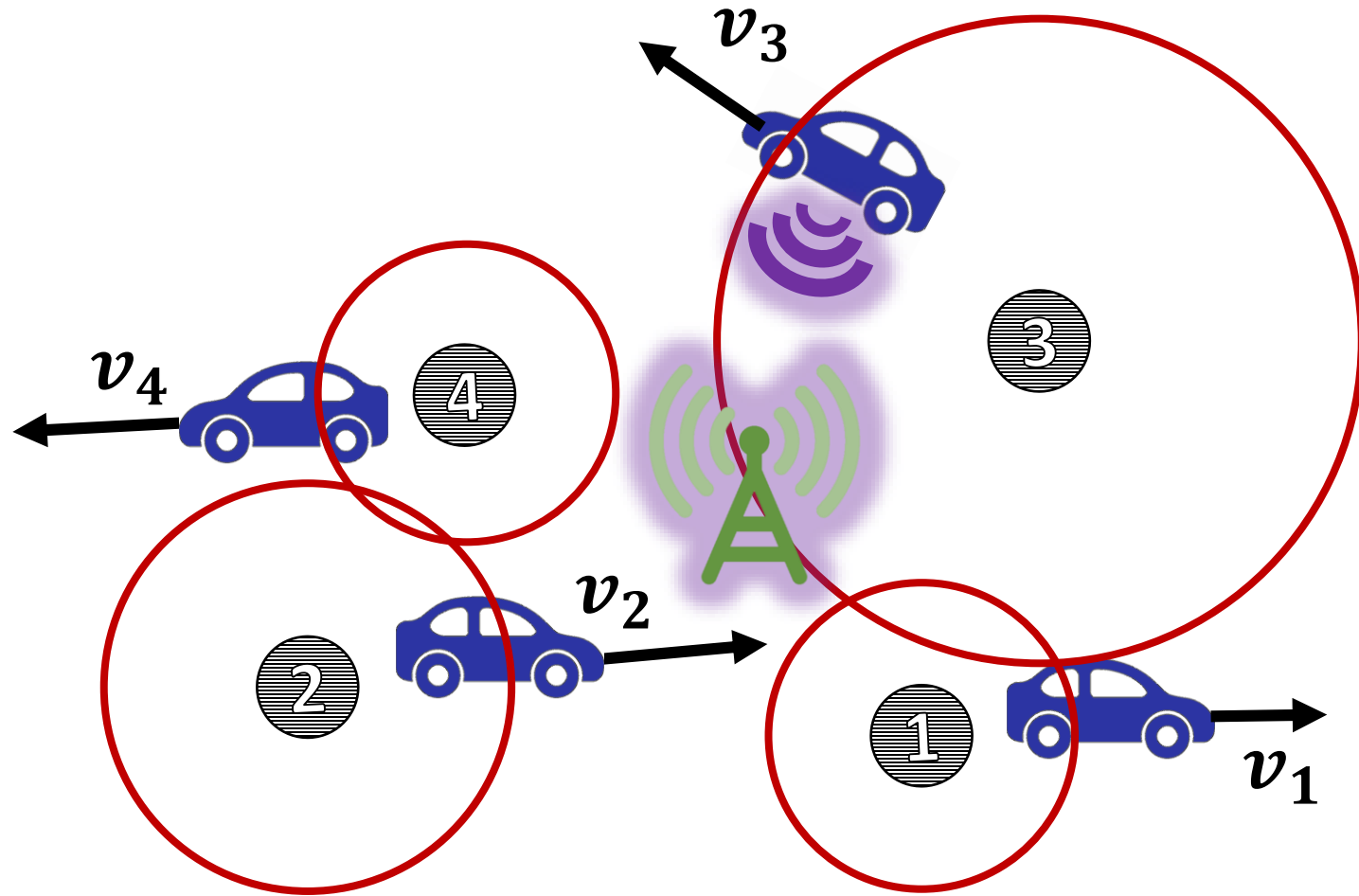


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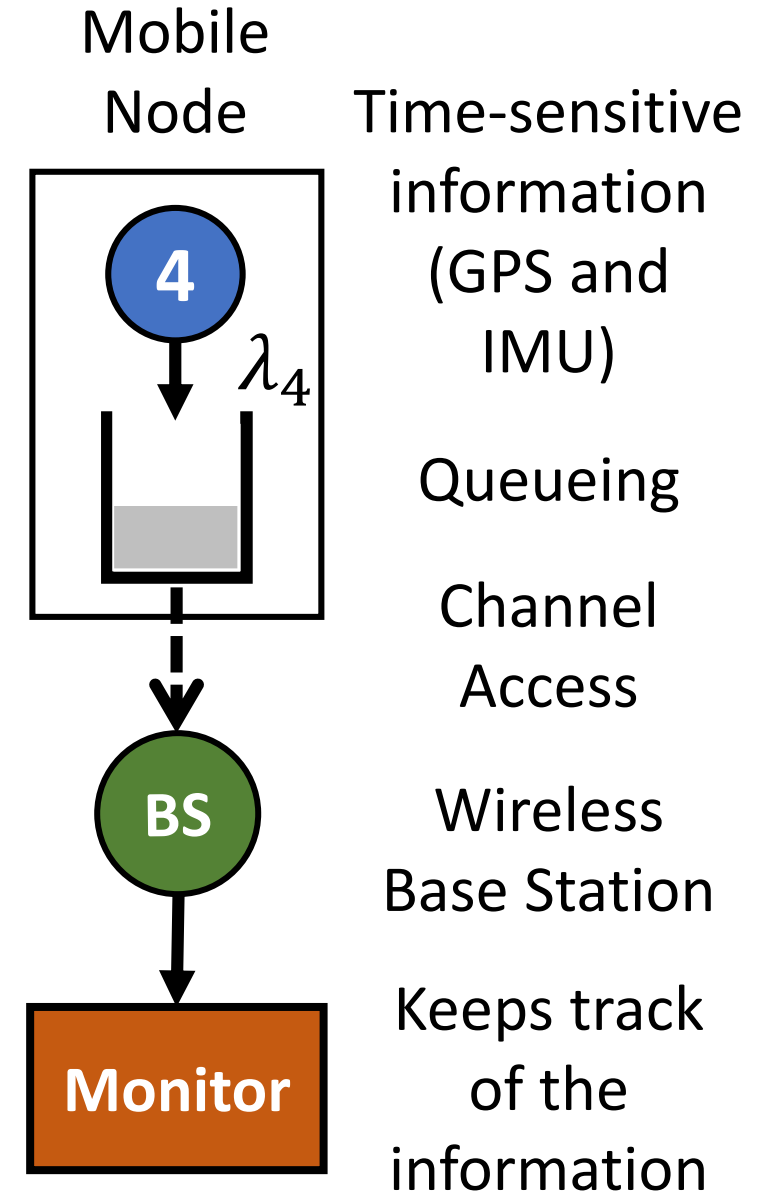
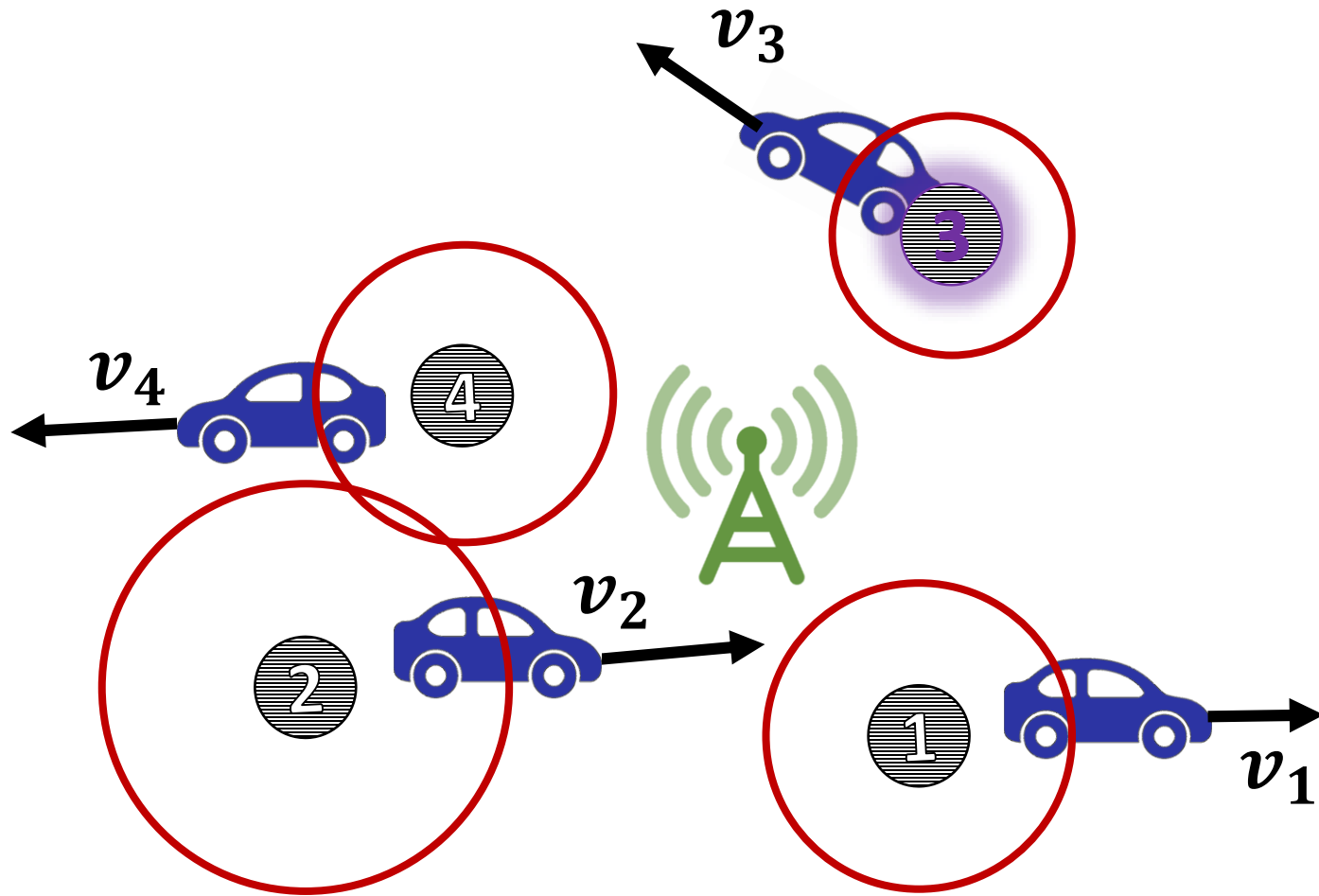




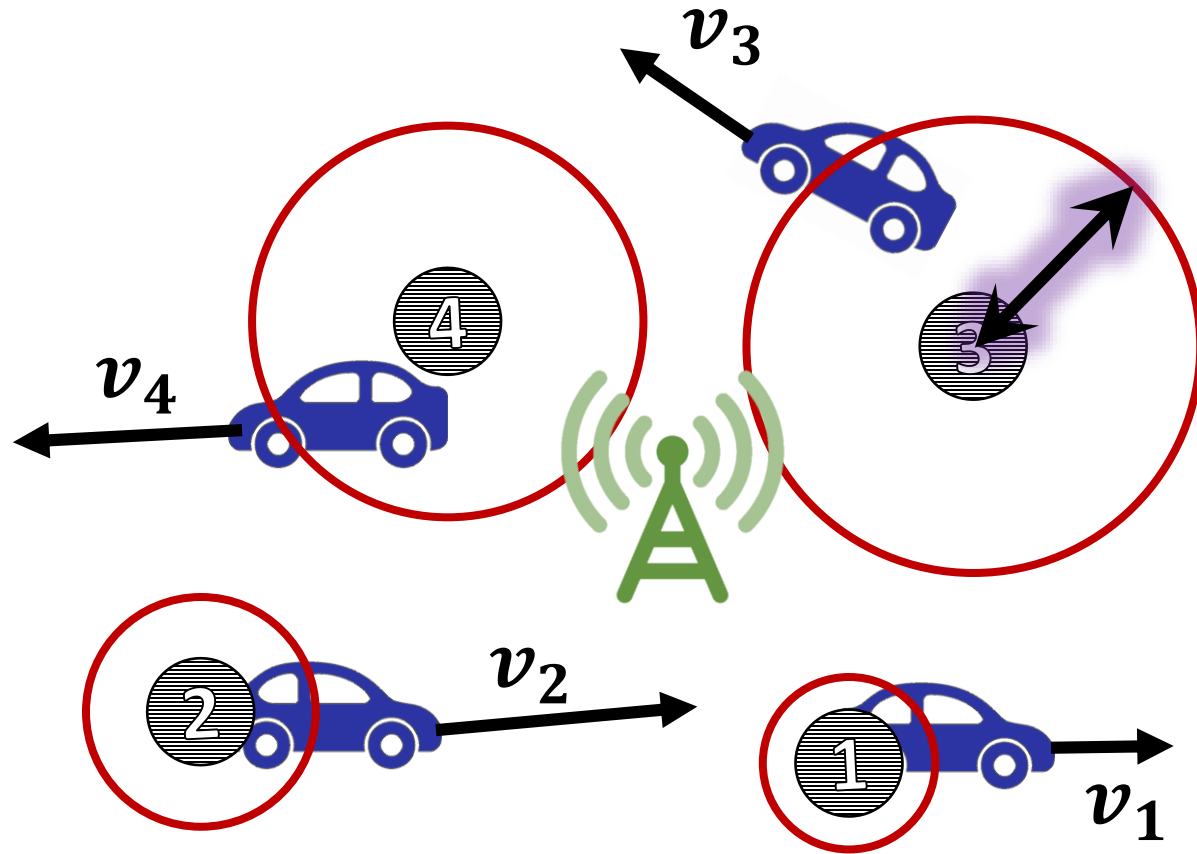
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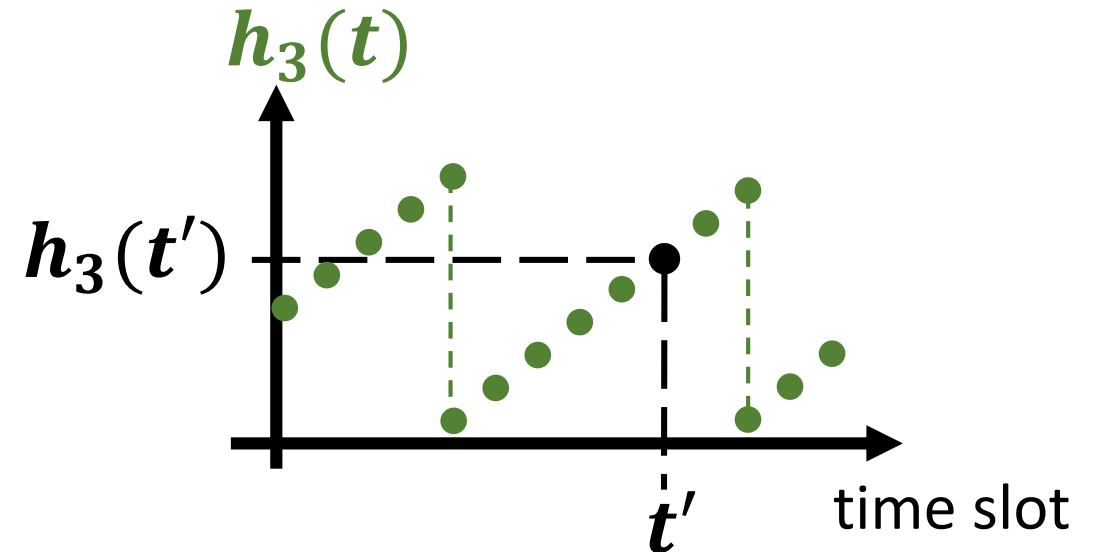
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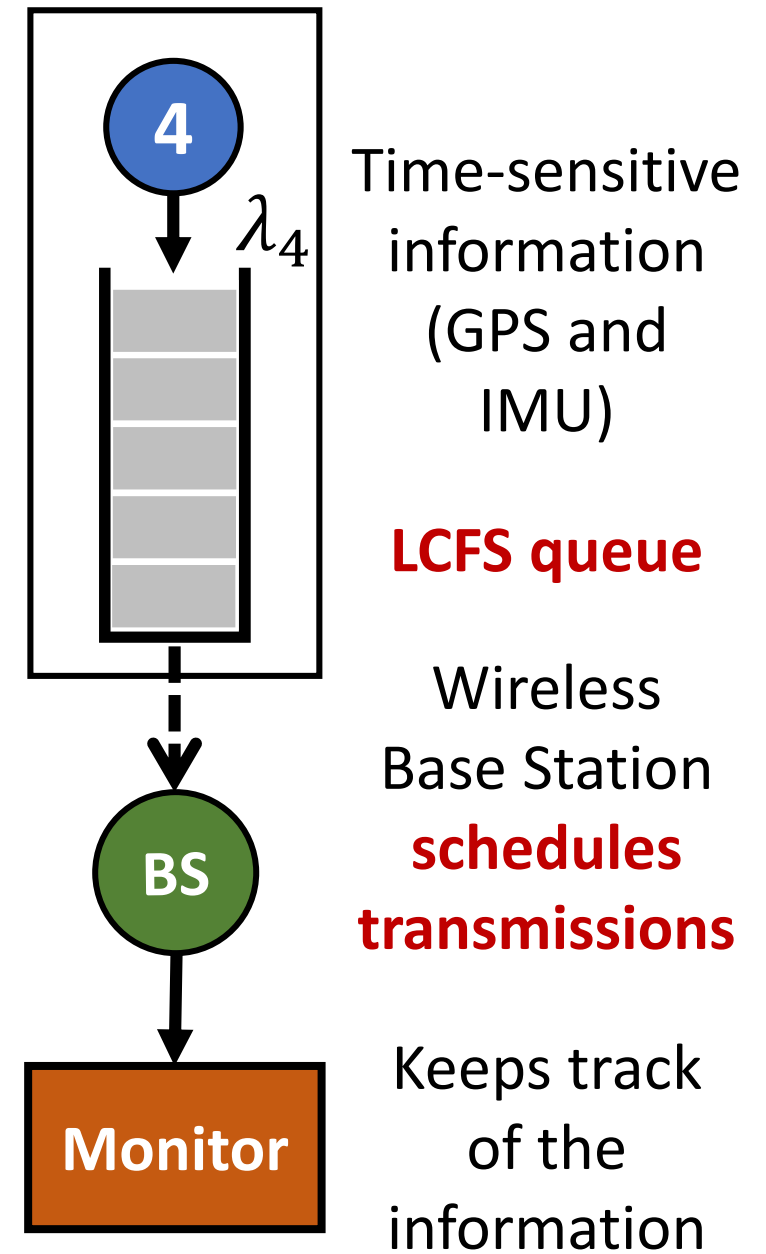
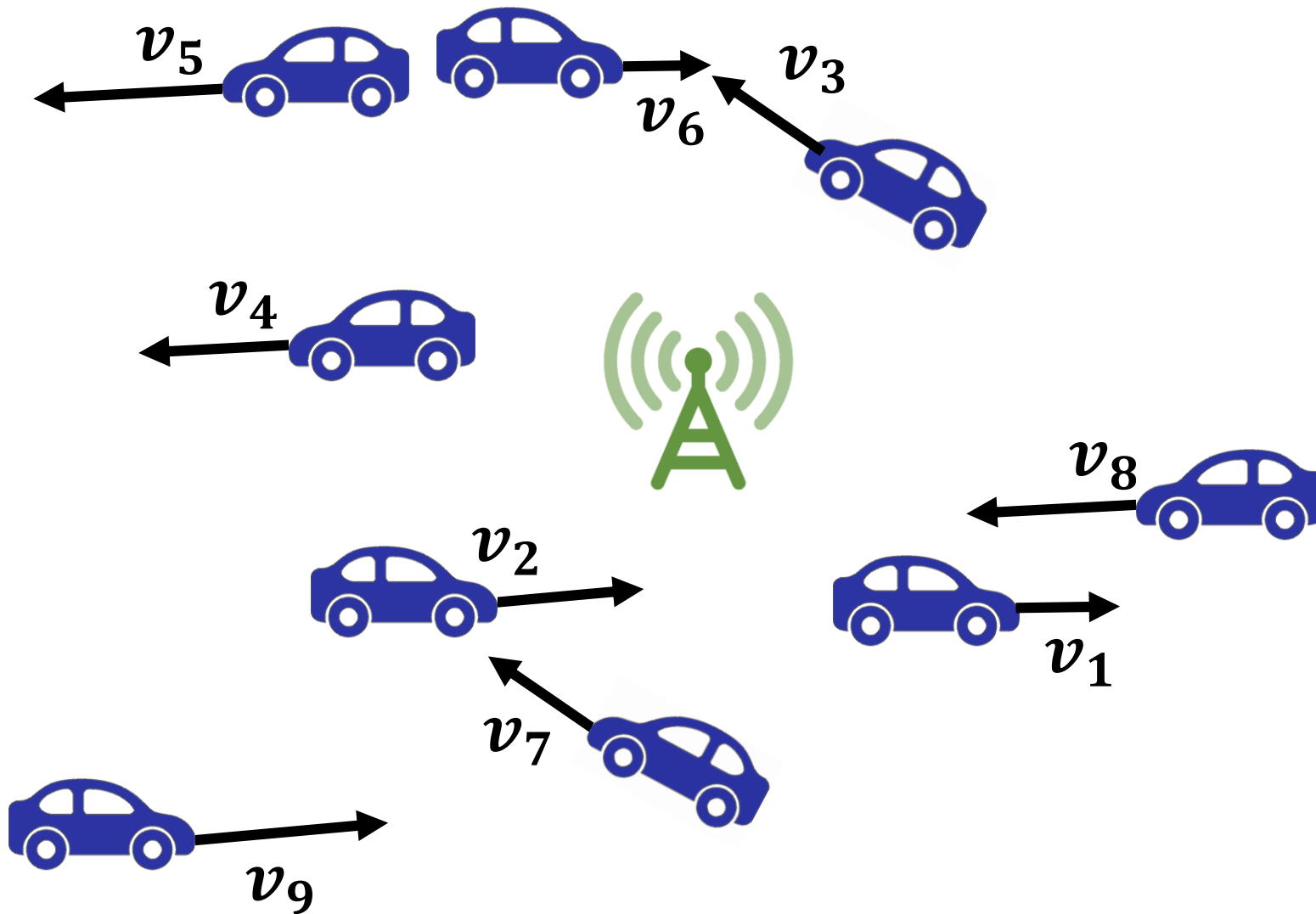
# Age-of-Information and Position Uncertainty



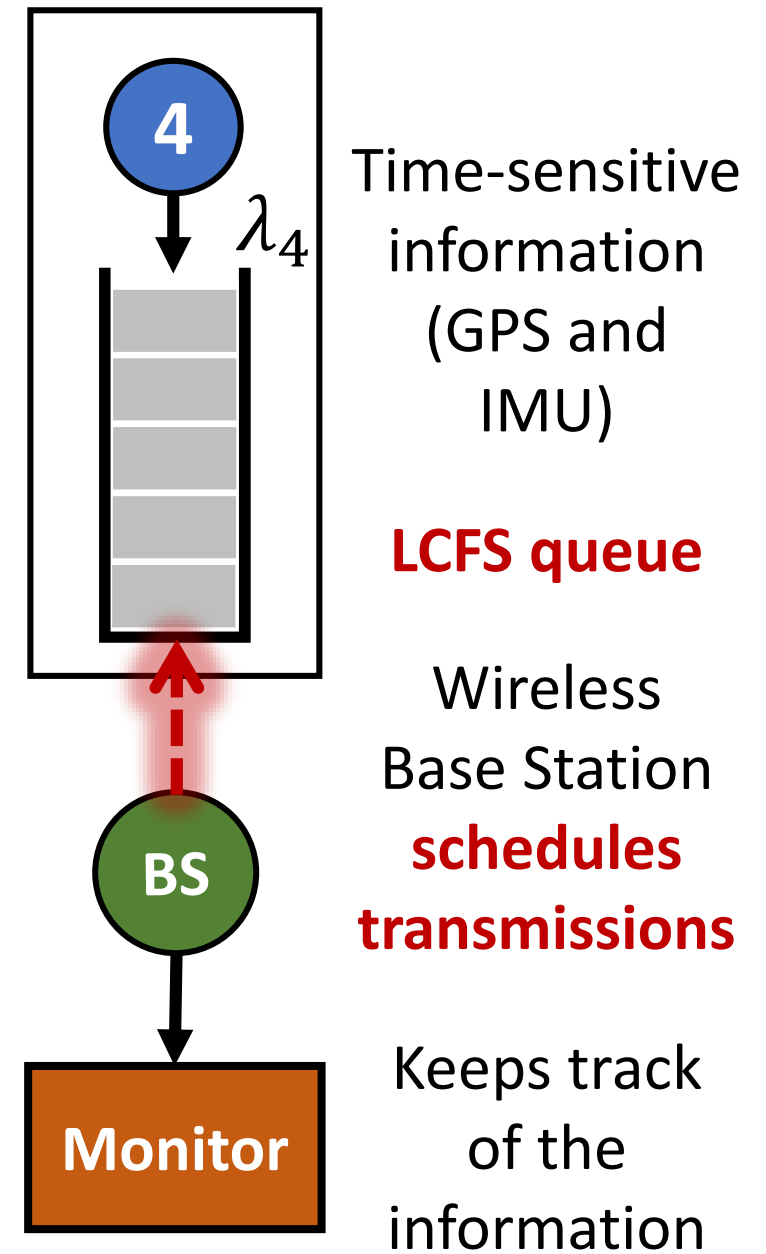
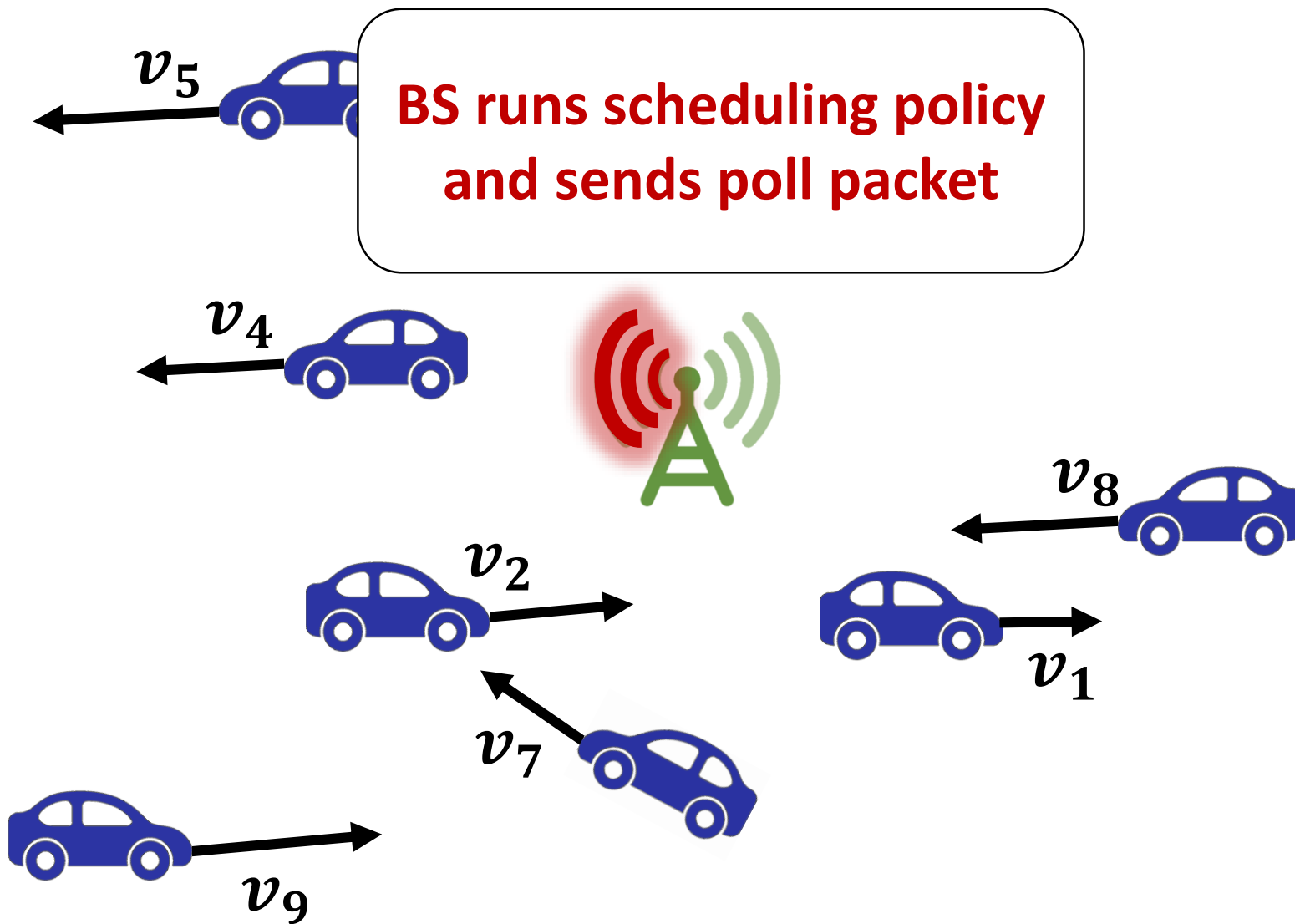
Position uncertainty of node 3 at slot  $t'$  is given by the radius  $v_3 h_3(t')$



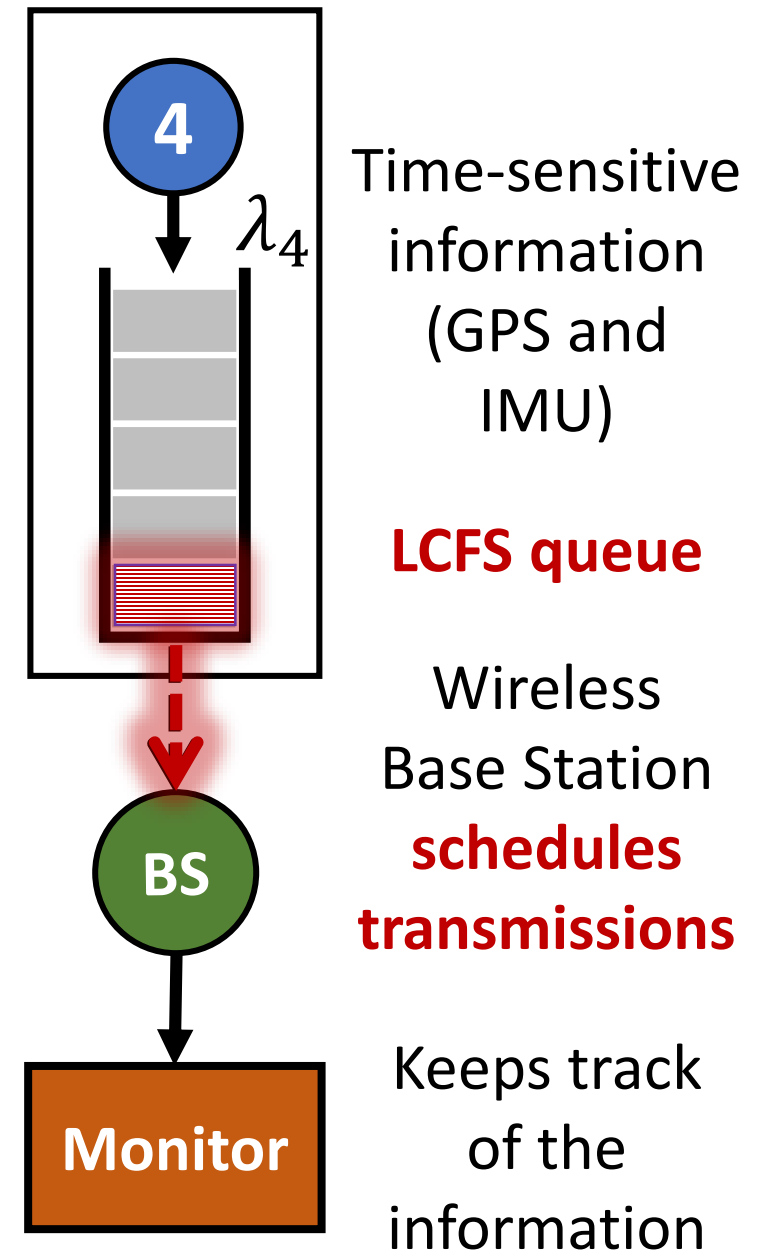
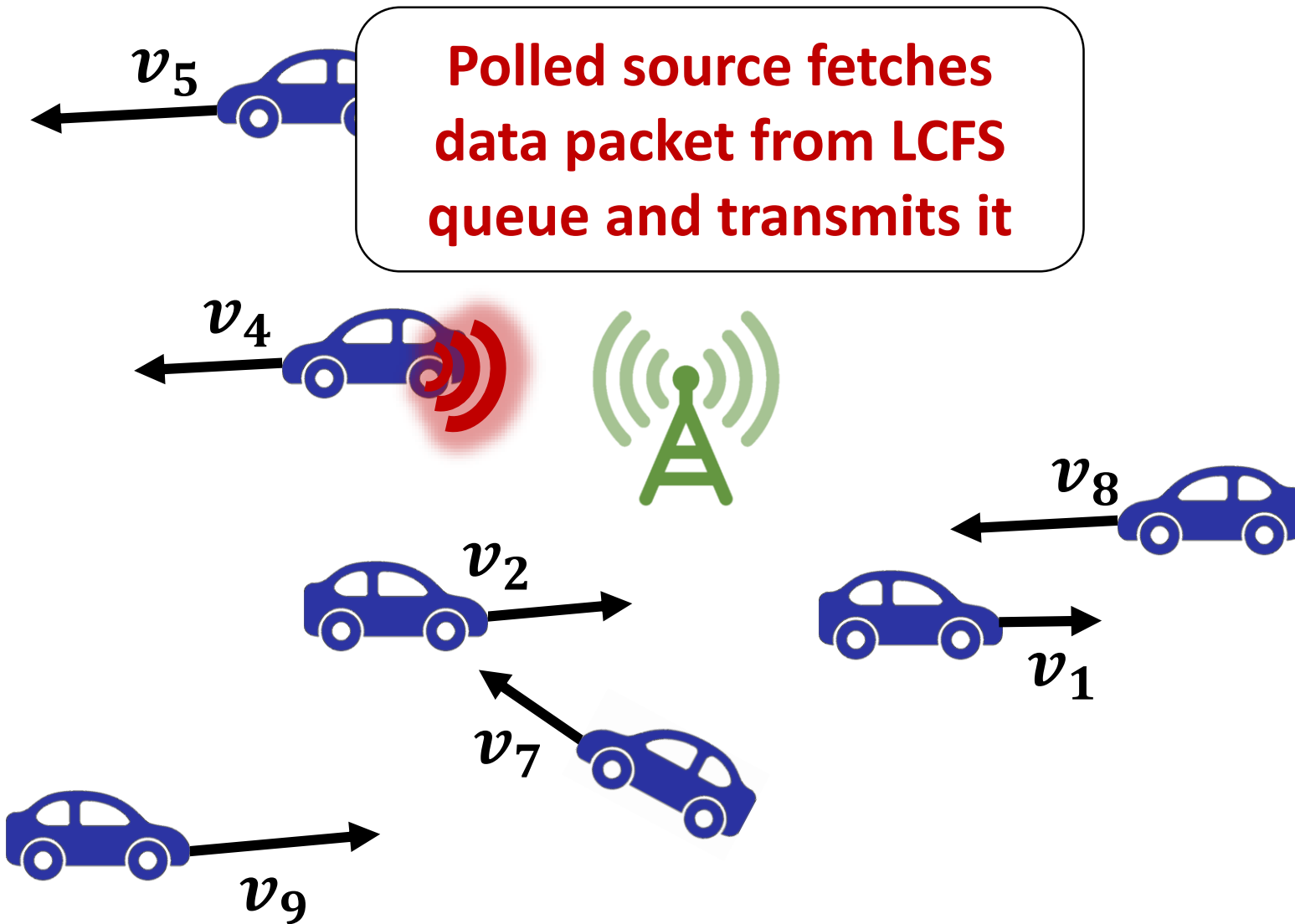
# Large-scale system using **WiFresh**



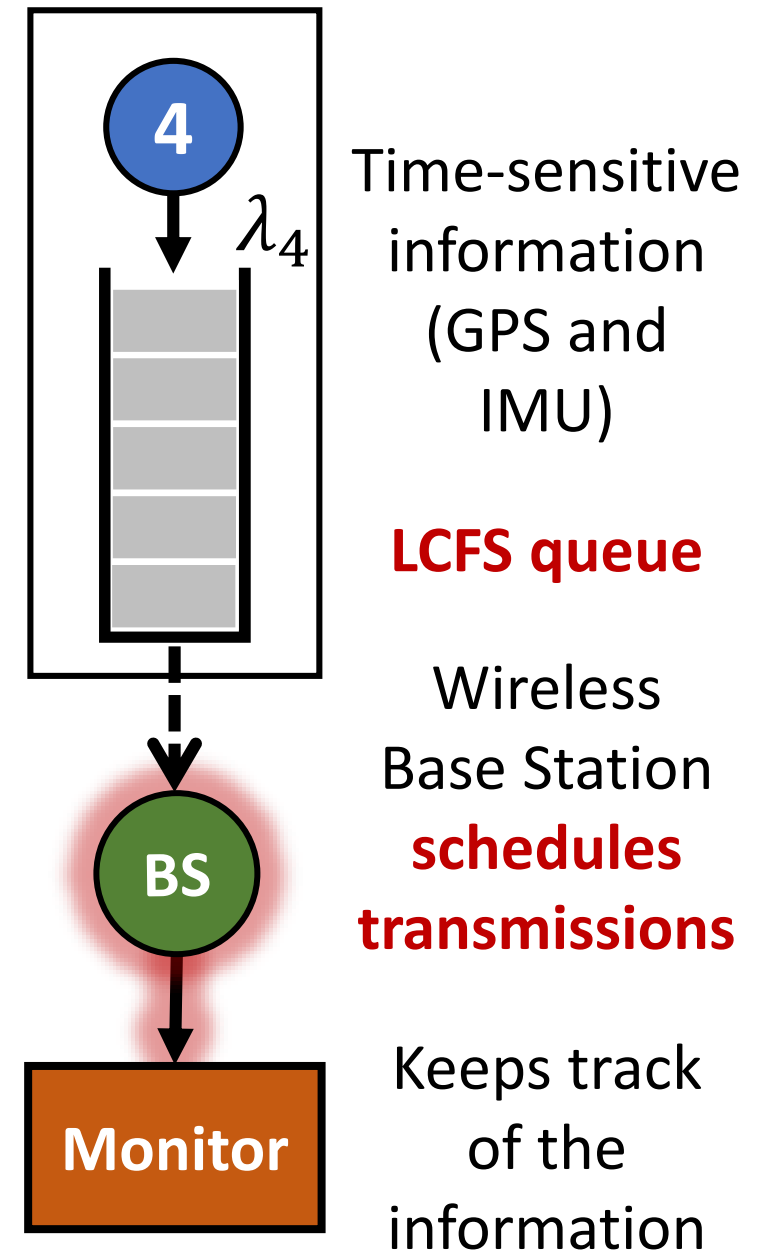
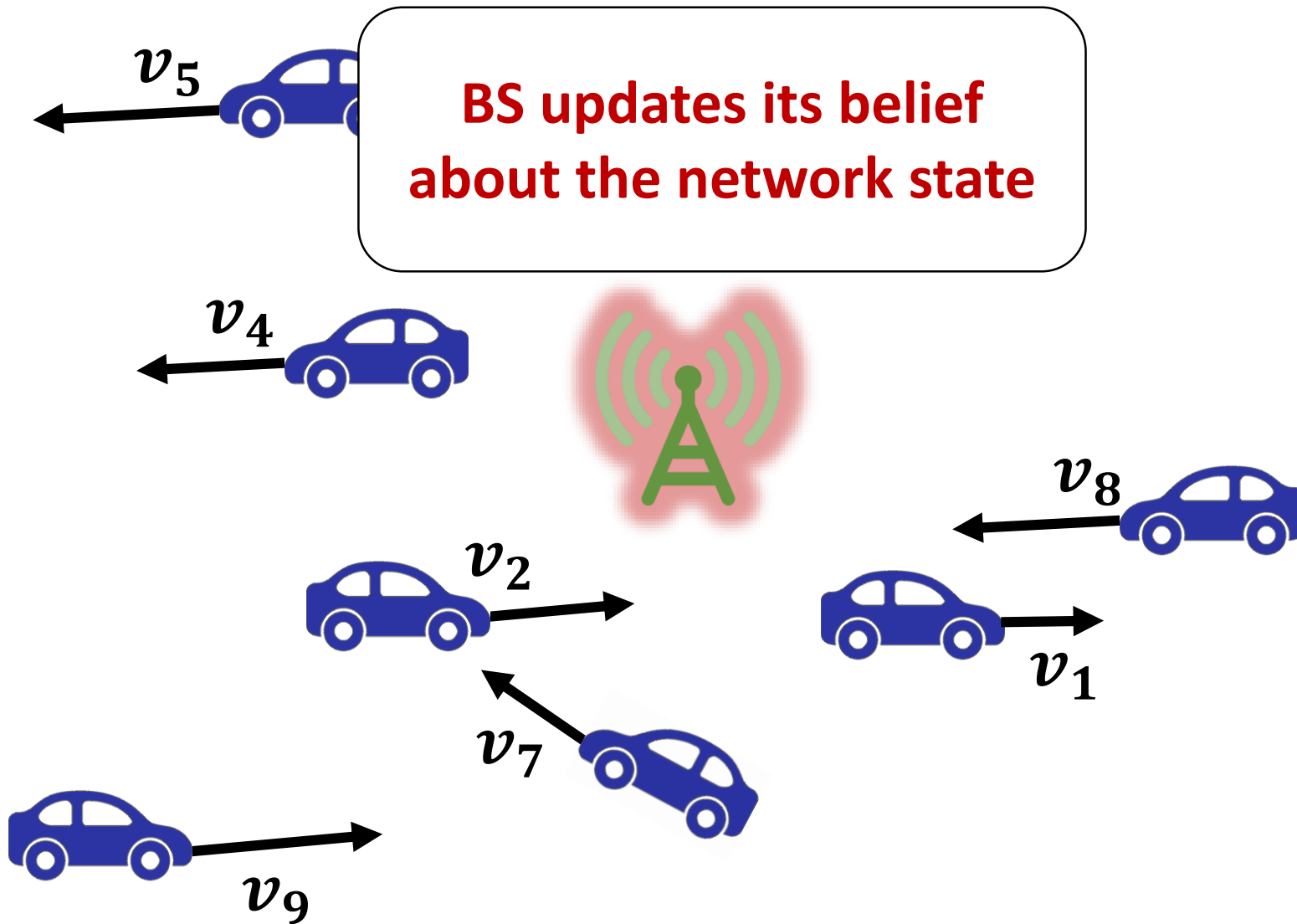
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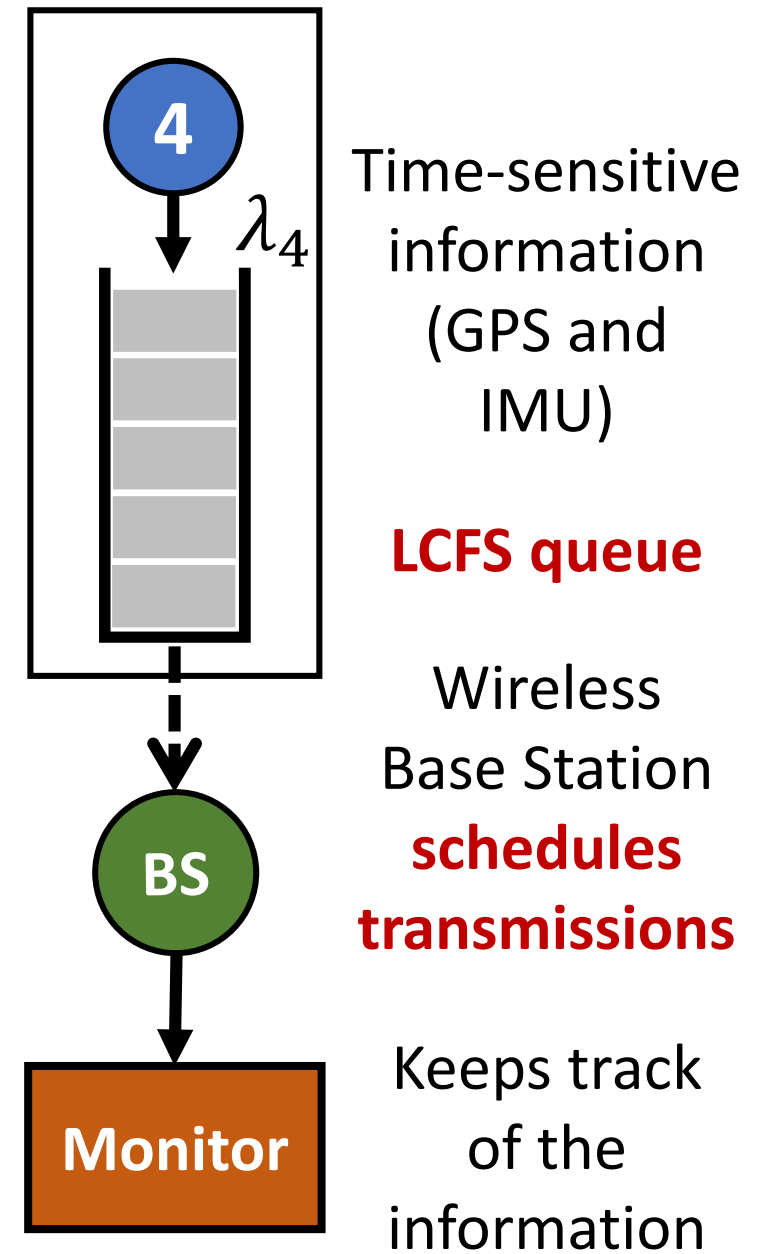
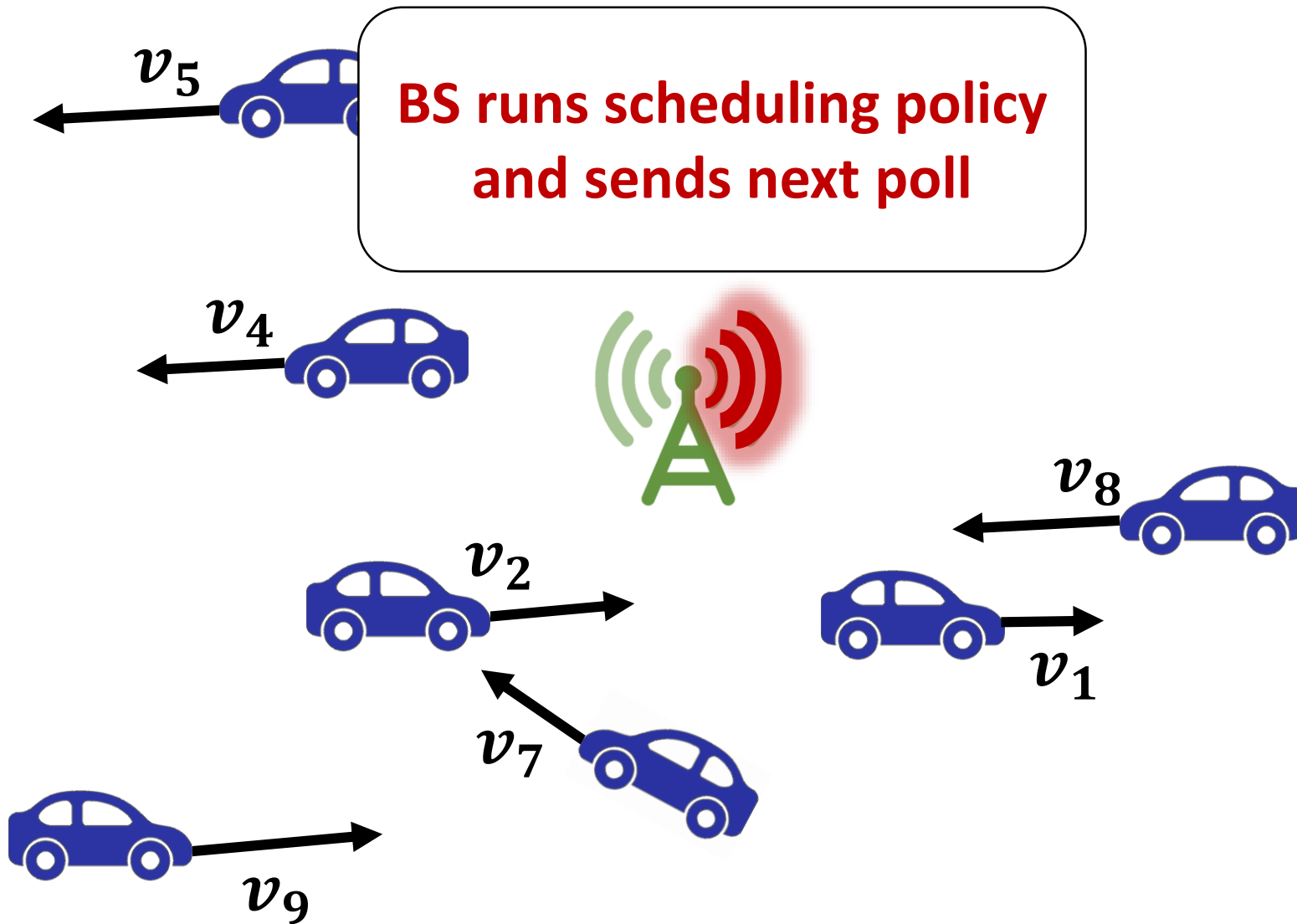
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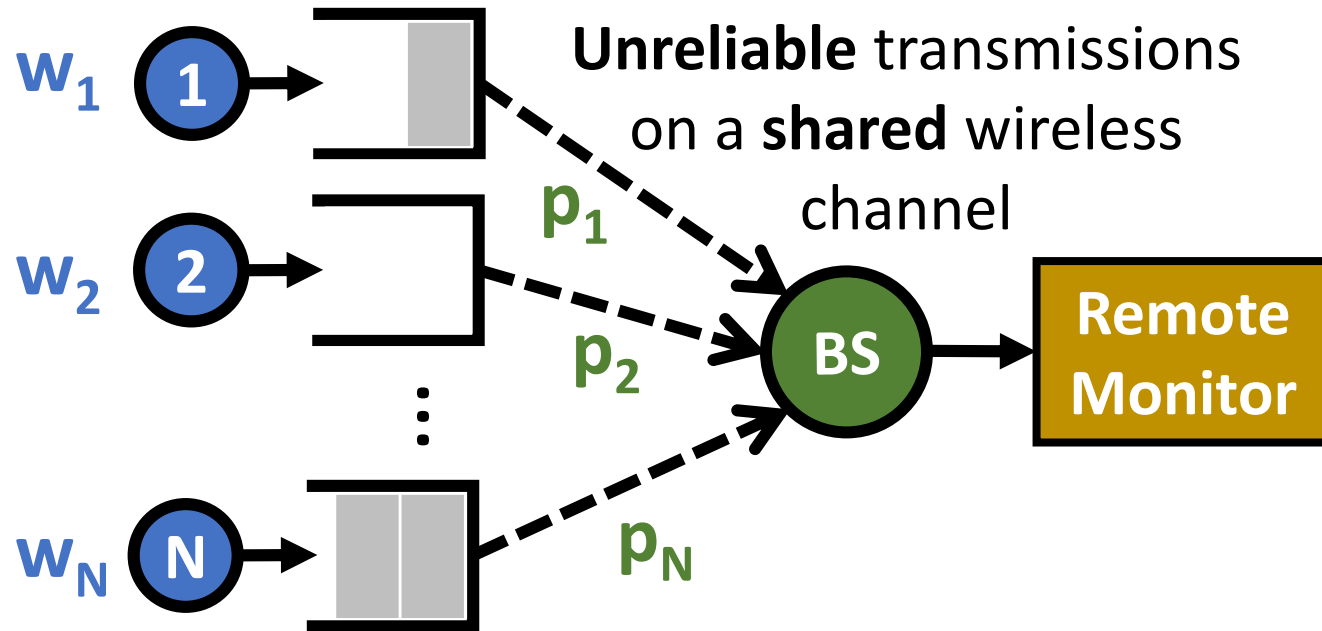




# Network Model

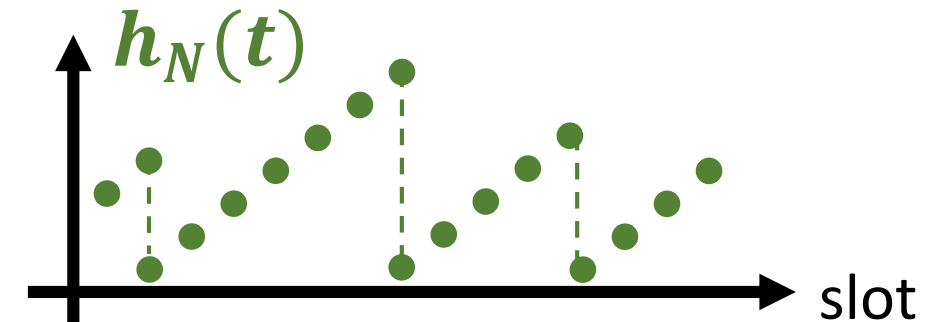
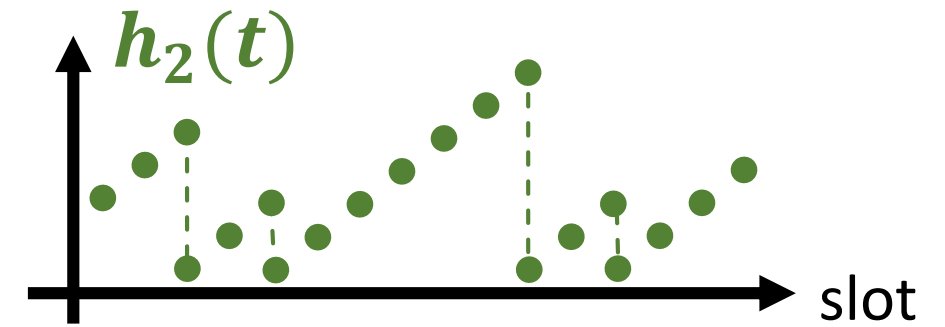
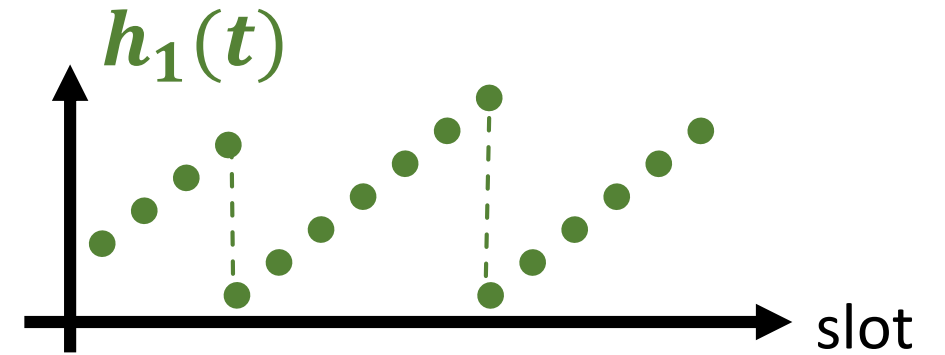
## Simplest model:

On-demand packet generation and LCFS queues



Weight  $w_i > 0$  represents **priority** of source  $i$

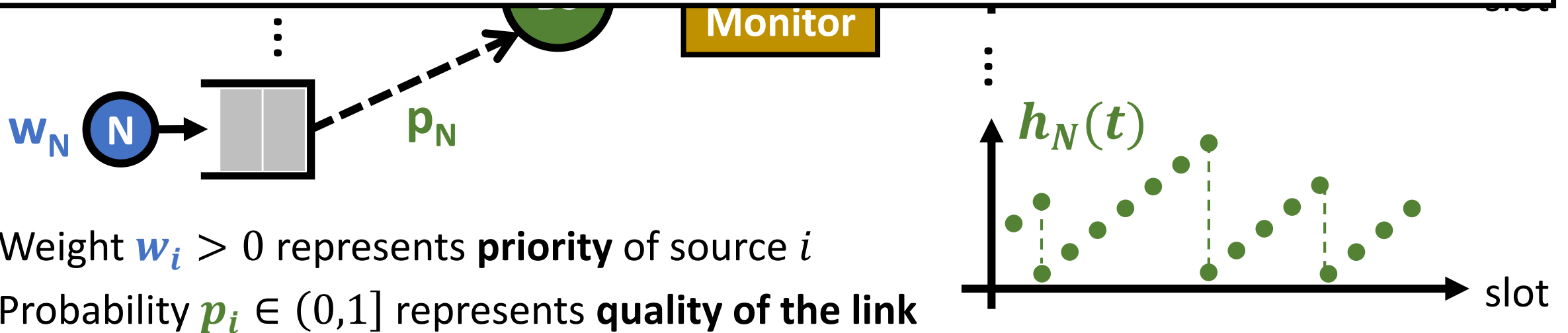
Probability  $p_i \in (0,1]$  represents **quality of the link**



# Network Model - Objective Function

**Goal:** find a **transmission scheduling policy**  $\pi^*$  that minimizes the Expected Weighted Sum Age-of-Information (**EWSAoI**):

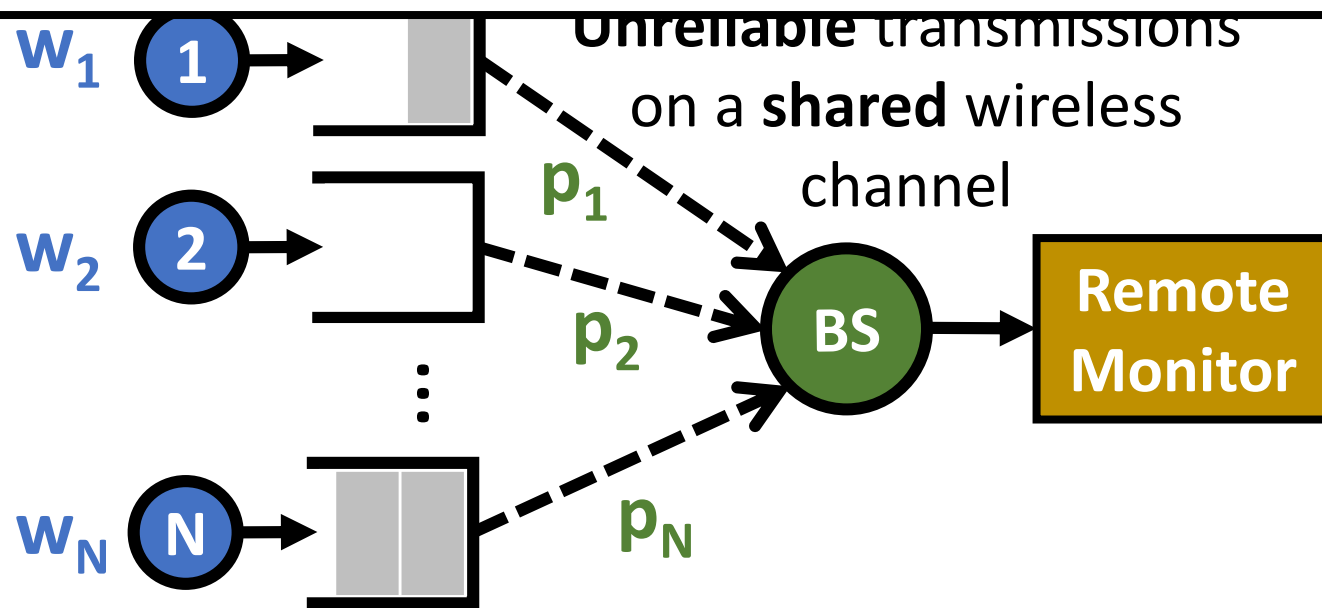
$$\mathbb{E}[J^*] = \min_{\pi \in \Pi} \left\{ \lim_{T \rightarrow \infty} \mathbb{E}[J_T^\pi] \right\}, \text{ where } \mathbb{E}[J_T^\pi] = \frac{1}{TN} \sum_{t=1}^T \sum_{i=1}^N w_i \mathbb{E}[h_i^\pi(t)]$$



# Summary of Theoretical Results

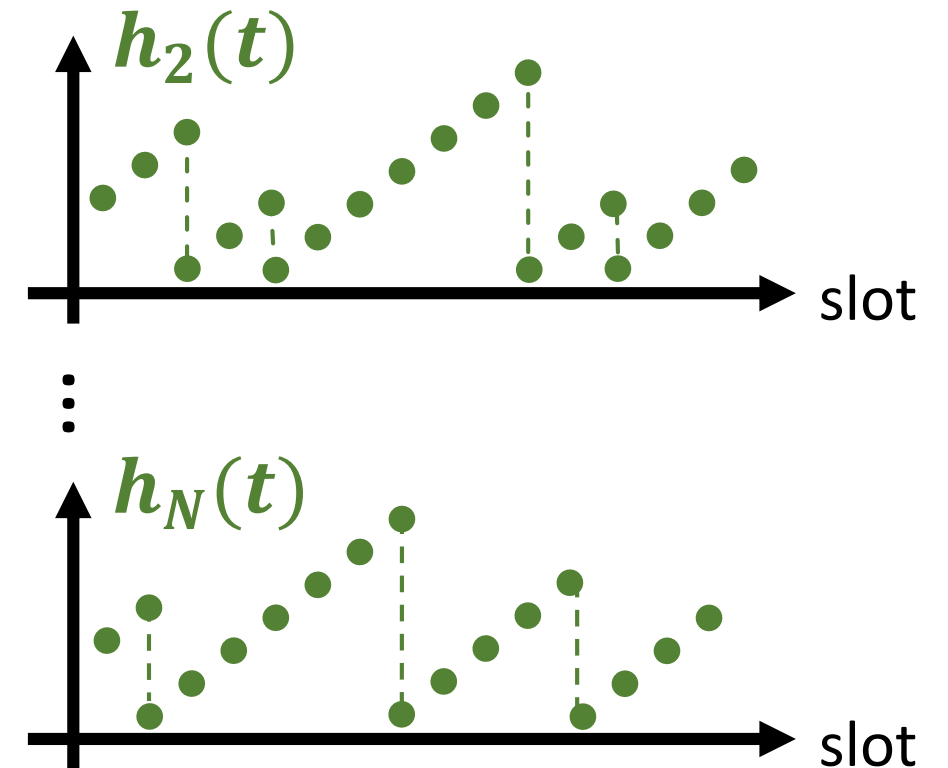
## Model:

On-demand packet generation and LCFS queues. Packets are always fresh.



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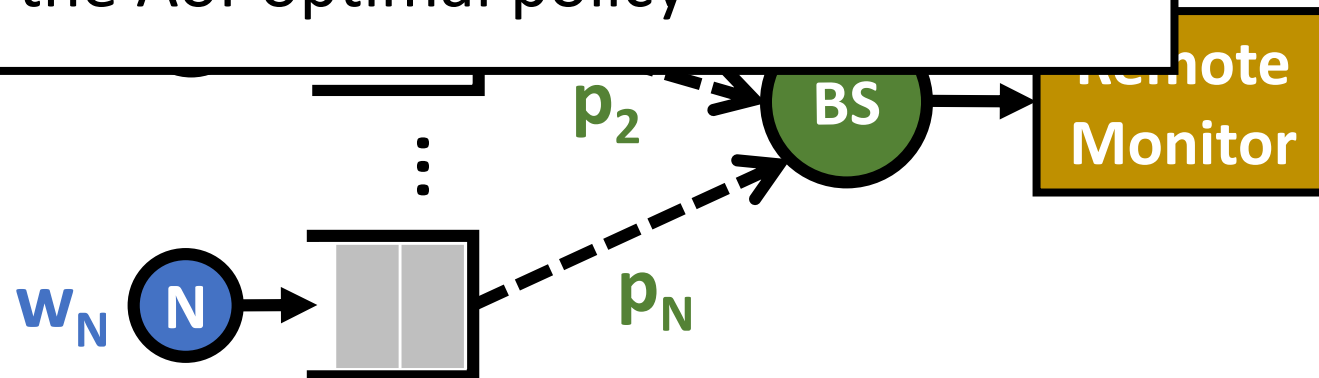


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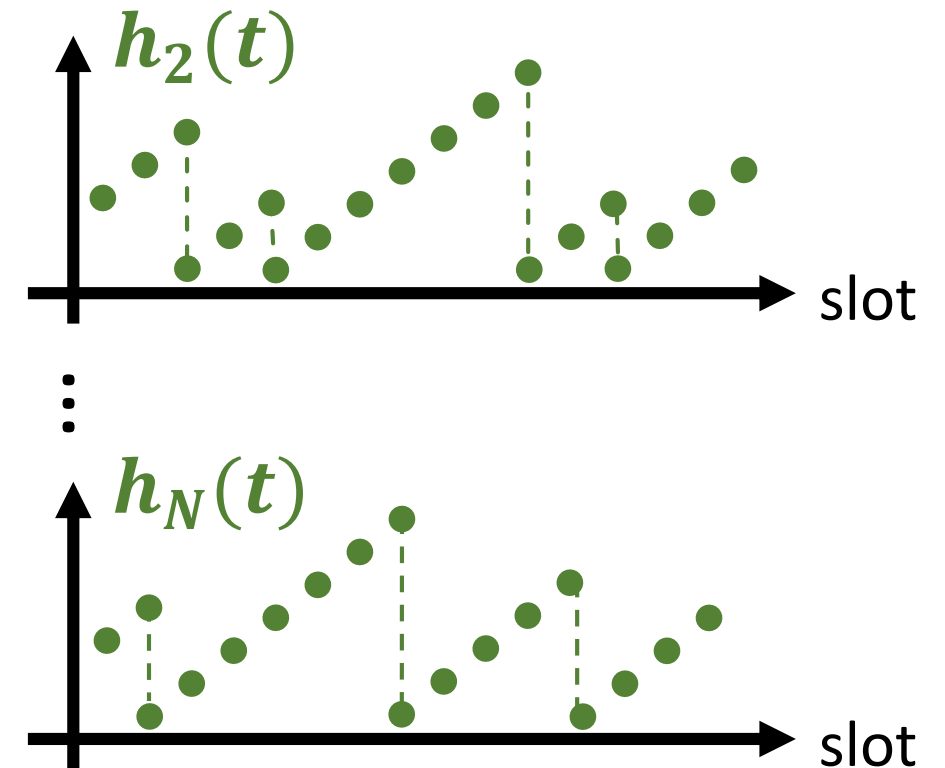
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Dynamic Programming to compute  
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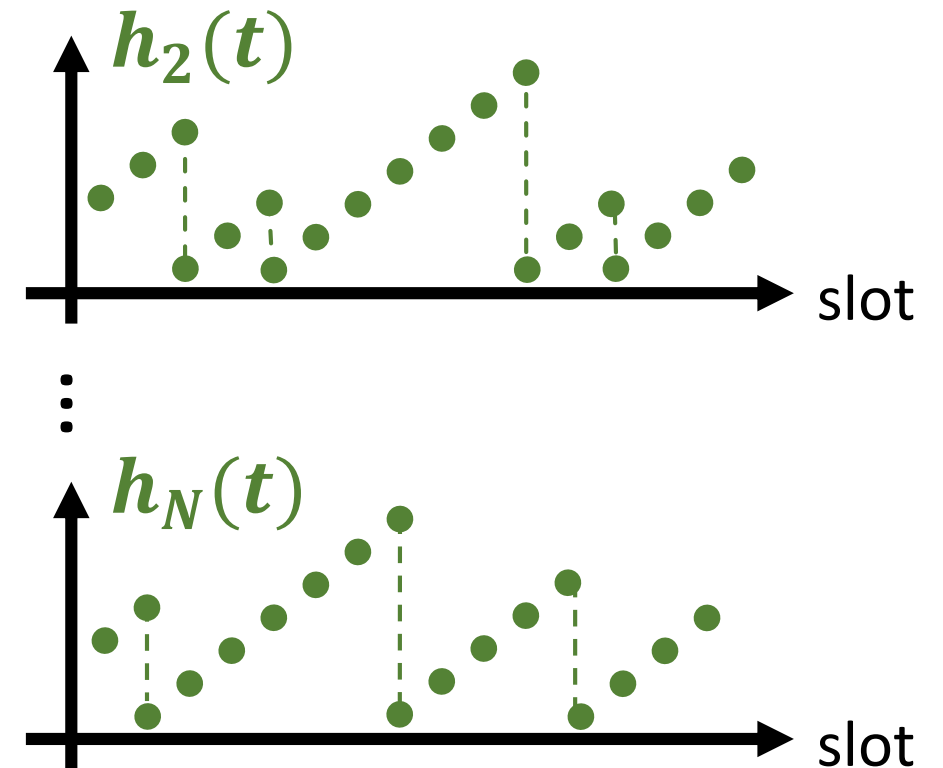
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**Greedy Policy** is Aol-optimal for networks with  $p_i = p$  and  $w_i = w$

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# Summary of Theoretical Results

## Model:

On-demand packet generation and LCFS queues. Packets are always fresh.

**Dynamic Programming** to compute the Aol-optimal policy

**Greedy Policy** is Aol-optimal for networks with  $p_i = p$  and  $w_i = w$

**Lower Bound:** for any given network with  $(N, w_i, p_i)$ :  $\lim_{T \rightarrow \infty} \mathbb{E}[J_T^\pi] \geq L_B$

where :

$$L_B = \frac{1}{2N} \left( \sum_{i=1}^N \sqrt{\frac{w_i}{p_i}} \right)^2 + \frac{1}{N} \sum_{i=1}^N w_i$$

# Performance Guarantees

- **Performance Guarantee for  $\pi$** : for any given network with  $(N, w_i, p_i)$

$$L_B \leq \mathbb{E}[J^*] \leq \mathbb{E}[J^\pi] \leq \beta^\pi L_B$$

- Three **scheduling policies** with performance guarantees:

Scheduling Policy	Technique	Optimality Ratio	Simulation Result
Optimal Stationary Randomized Policy	Renewal Theory	<b>2</b> -optimal	~ 2-optimal
Age-Based Max-Weight Policy	Lyapunov Optimization	<b>2</b> -optimal	close to optimal
Whittle's Index Policy	RMAB Framework	<b>8</b> -optimal	close to optimal

# Summary of results for this model

Scheduling Policy	Decision in slot $t$	Performance Guarantee
Greedy	highest $h_i(t)$	optimal when symmetric
Randomized	node $i$ w.p. $\propto \sqrt{w_i/p_i}$	2-optimal
Age-Based Max-Weight	highest $w_i p_i h_i^2(t)$	2-optimal
Whittle's Index	highest $w_i p_i h_i^2(t) + w_i p_i h_i(t) [ 2/p_i - 1 ]$	8-optimal

- For symmetric networks: **Whittle's**  $\equiv$  **Max-Weight**  $\equiv$  **Greedy** (all are optimal)

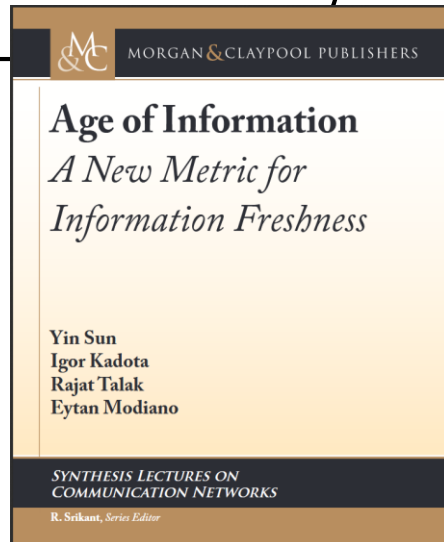


# Extensions

## In this presentation:

- Minimize EWSAoI
- LCFS queue
- Sources generating packets on-demand

[Book'19]



Sources generating packets periodically

[IEEE Allerton'16] [IEEE/ACM ToN'18]

Minimize EWSAoI subject to throughput constraints

[IEEE INFOCOM'18 best paper award]  
[IEEE/ACM ToN'19]

- Sources generating packets stochastically
- Analysis for different queueing disciplines

[ACM MobiHoc'19 best paper finalist]  
[IEEE TMC'20]

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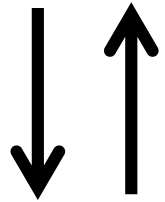
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# WiFresh - Implementation



**CPU:** System initialization, configuration, and creating log files.



information exchange



**FPGA:** Clock-Driven (10MHz) code for generating packets, accessing the wireless channel, and managing time.

## Software Defined Radio NI USRP 2974

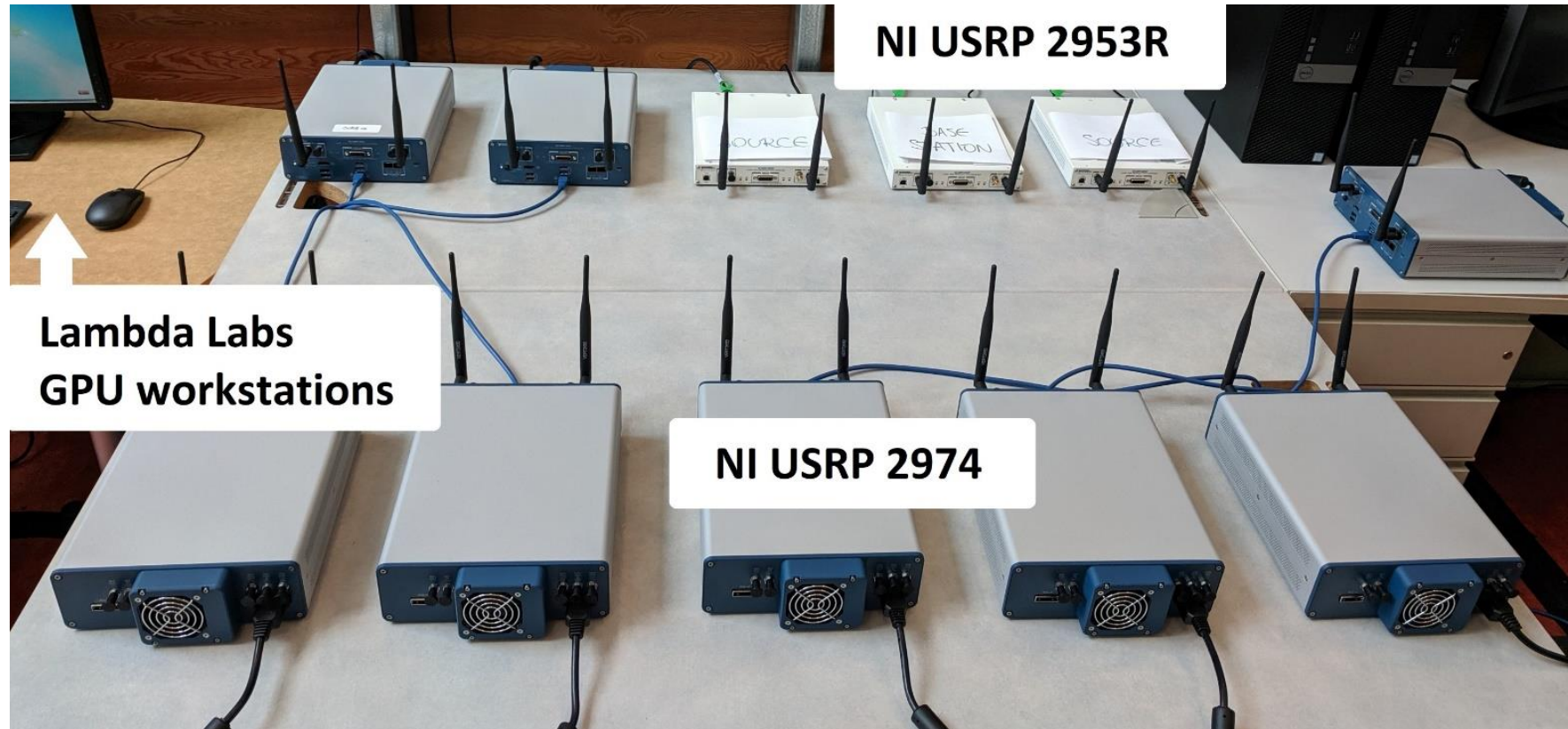


### **New functions at the FPGA:**

- Polling with Max-Weight
- LCFS queue
- Time-stamp processing
- Estimating parameters

# WiFresh - Video

- Ten sources generating packets of 150 bytes with frequency of  $\lambda = 3k$  packets per second.



Base  
Station

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- Age-of-Information and Applications

## 2. Theoretical Results: scheduling policies with performance guarantees

- Using Renewal Theory, Stochastic Dominance, RMAB framework, and others.

## 3. System Deployment: validation in real operating scenarios

- Using Software Defined Radios

**Thank you!!**

contact: [igor.kadota@columbia.edu](mailto:igor.kadota@columbia.edu)

webpage.: <http://www.igorkadota.com>